



# Joint Gravitational Wave and Electromagnetic Observation of Neutron Star- Black Hole Coalescing Binaries: A New Method to Constrain Neutron Star Radius

Stefano Ascenzi

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Co-authors: N. De Lillo, C. J. Haster, F. Ohme, F. Pannarale

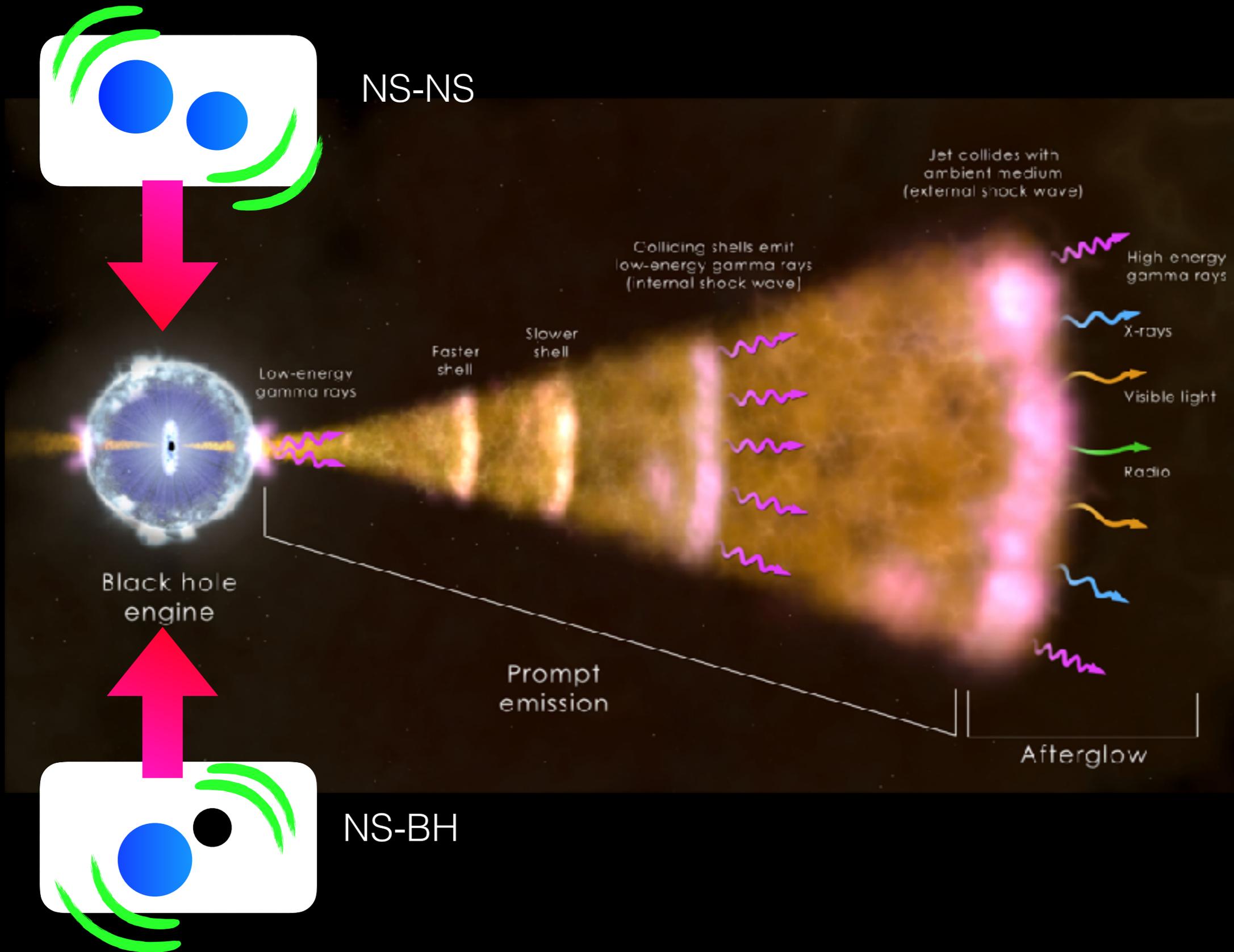
Collaborators: E. Brocato, V. Fafone, V. Ferrari, S. Marassi, S. Piranomonte



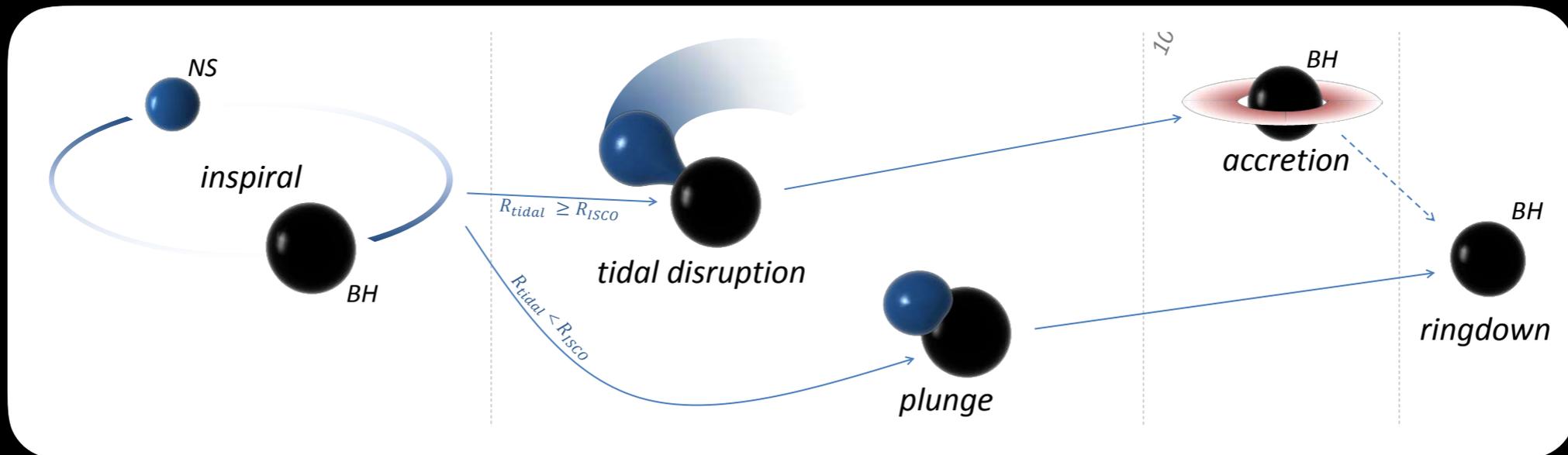
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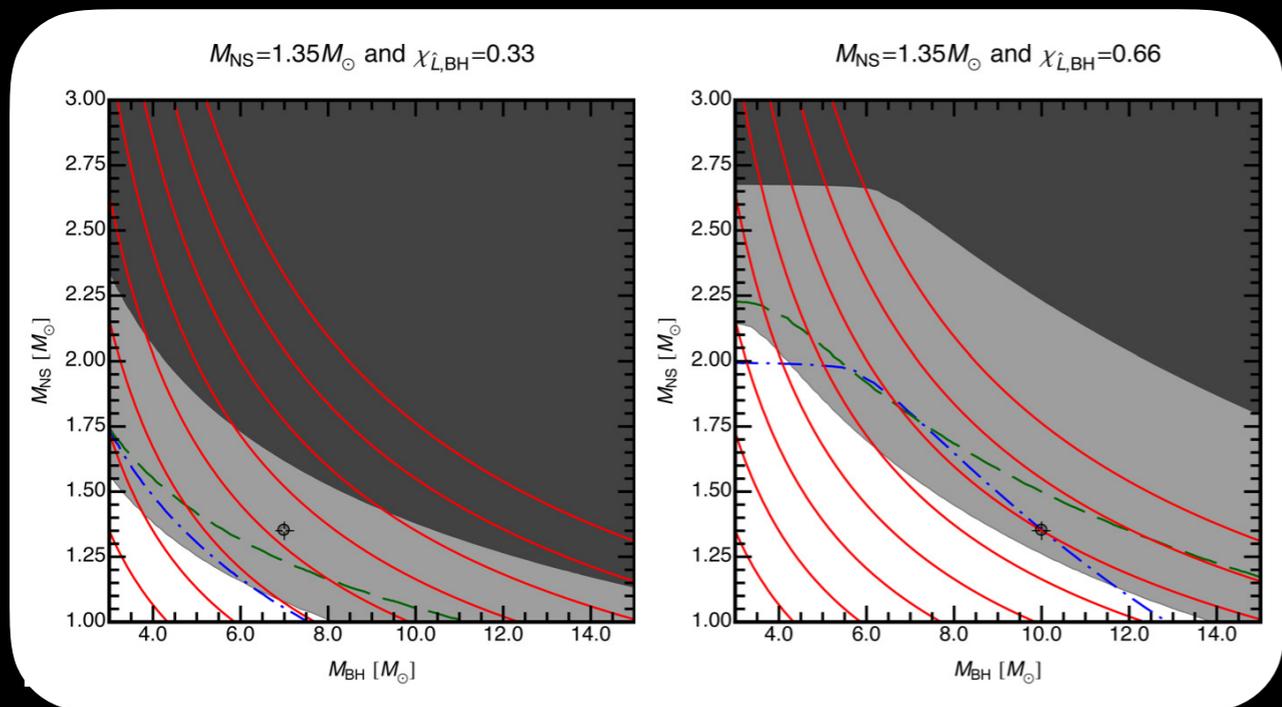
# Short Gamma Ray Burst



# NS-BH Merger



(Bartos 2012)



● No Remnant   ● EoS dependent   ● Remnant for all EoS

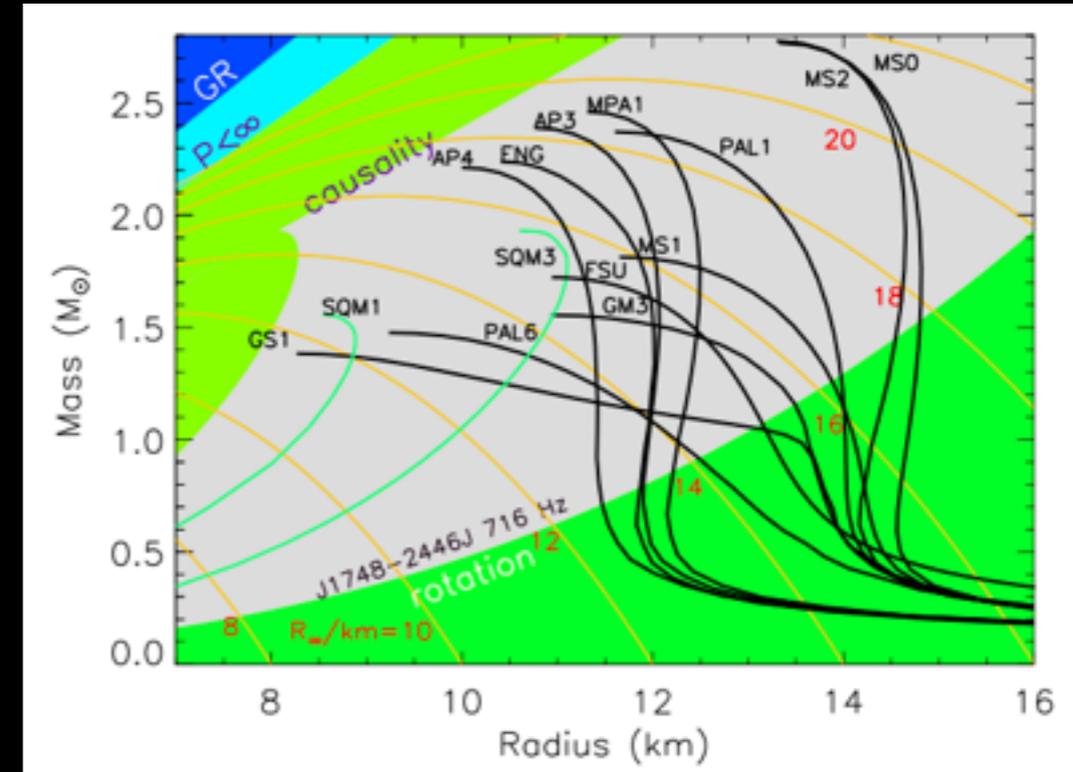
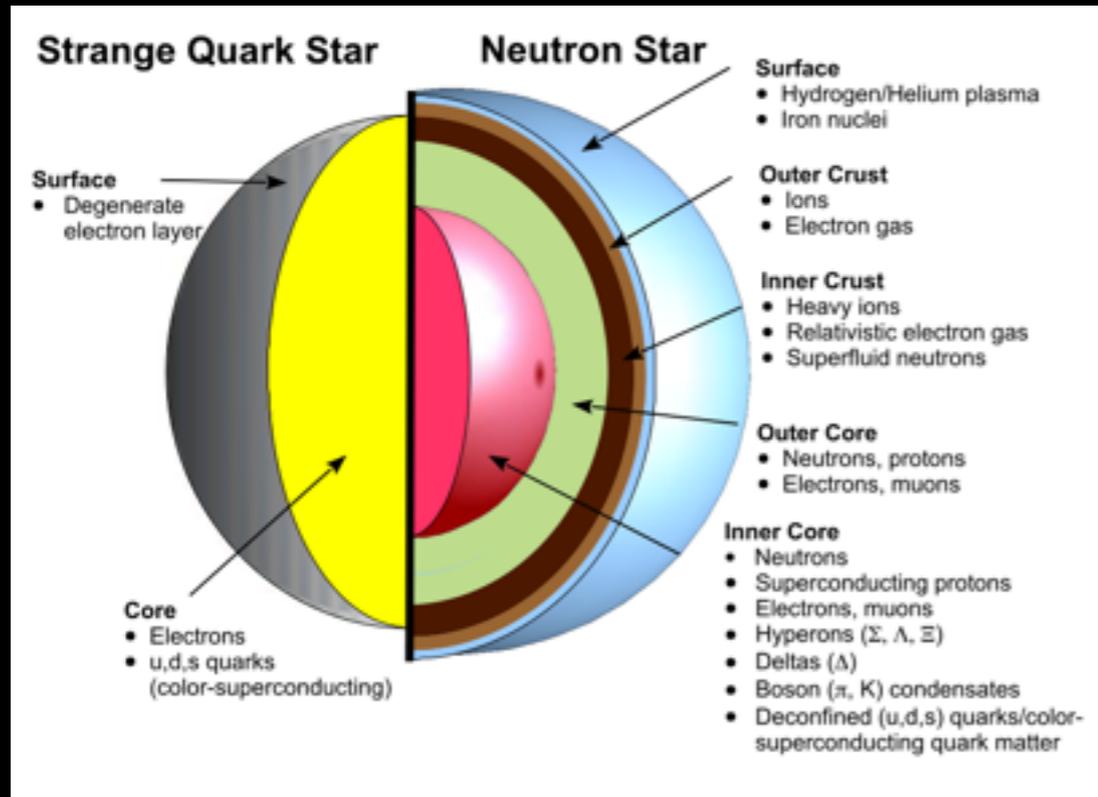
(Pannarale & Ohme 2014)

**Optimal scenario for EM counterpart**

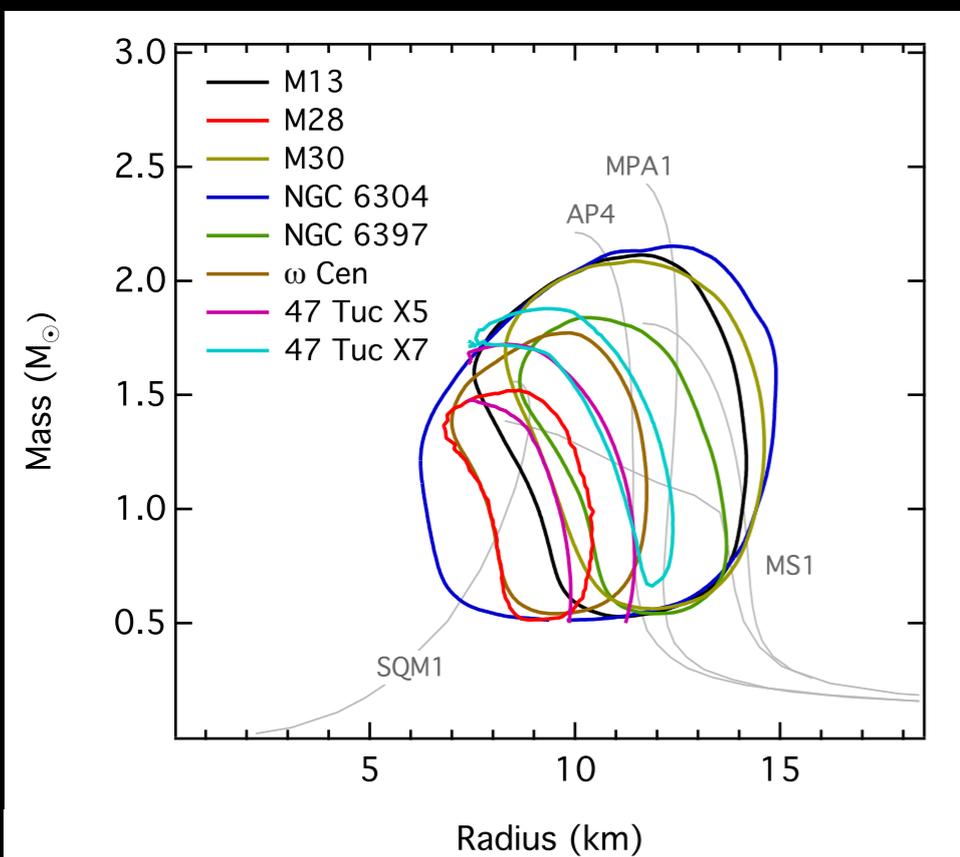


- Low mass, highly spinning BH
- Large NS radius (stiff EoS)

# NS Radii and EoS



(Lattimer & Prakash 2015)

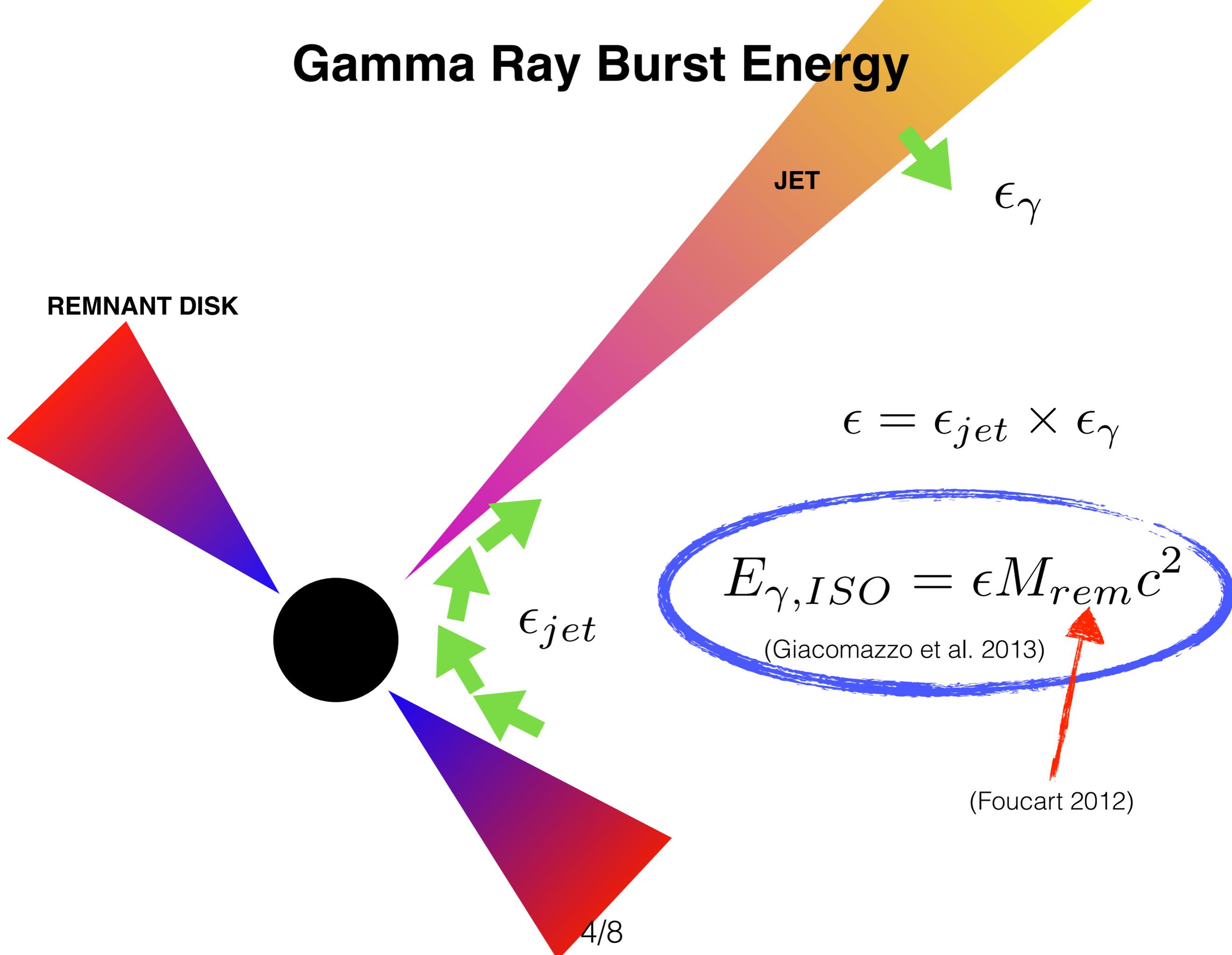


(Ozel & Freire 2016)

NS Radii are poorly constrained!

Constraints on NS EoS due to mass and radii measurements of quiescent LMXB

# Gamma Ray Burst Energy



# Method

Observations (GW+EM)

Prior Distribution

Sampling  
on GW  
posterior  
from PE

Sampling  
on  
 $\epsilon$

$$E_{\gamma, \text{ISO}} = \frac{\epsilon}{f_b(\theta)} M_{\text{rem}}(M_{\text{NS}}, M_{\text{BH}}, \chi_{\text{BH}}, R_{\text{NS}})$$

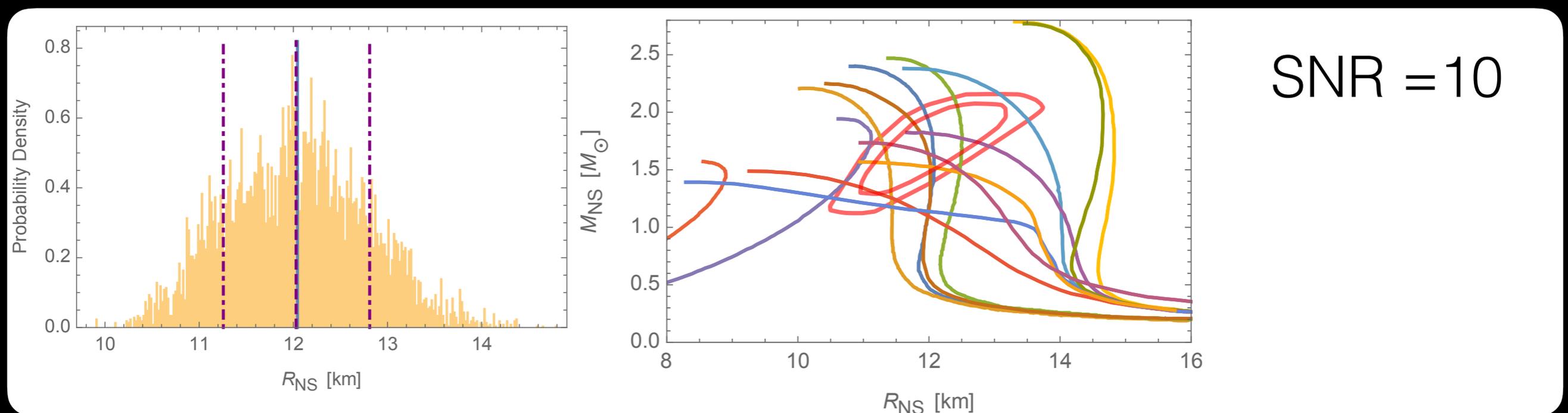
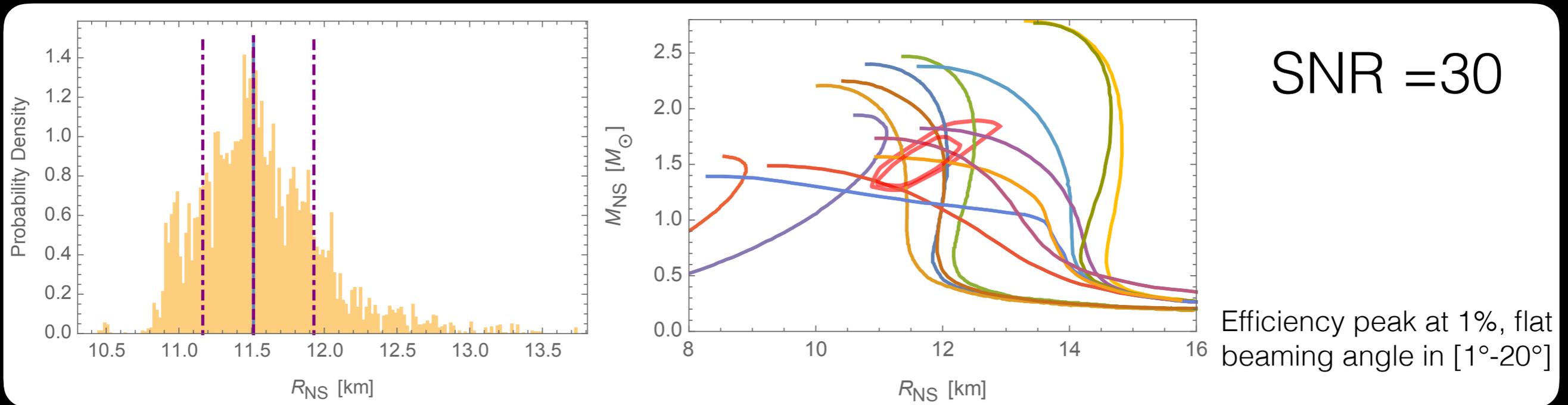
sGRB  
Energy

Sampling  
on  
 $\theta$

Posterior on  
 $R_{\text{NS}}$

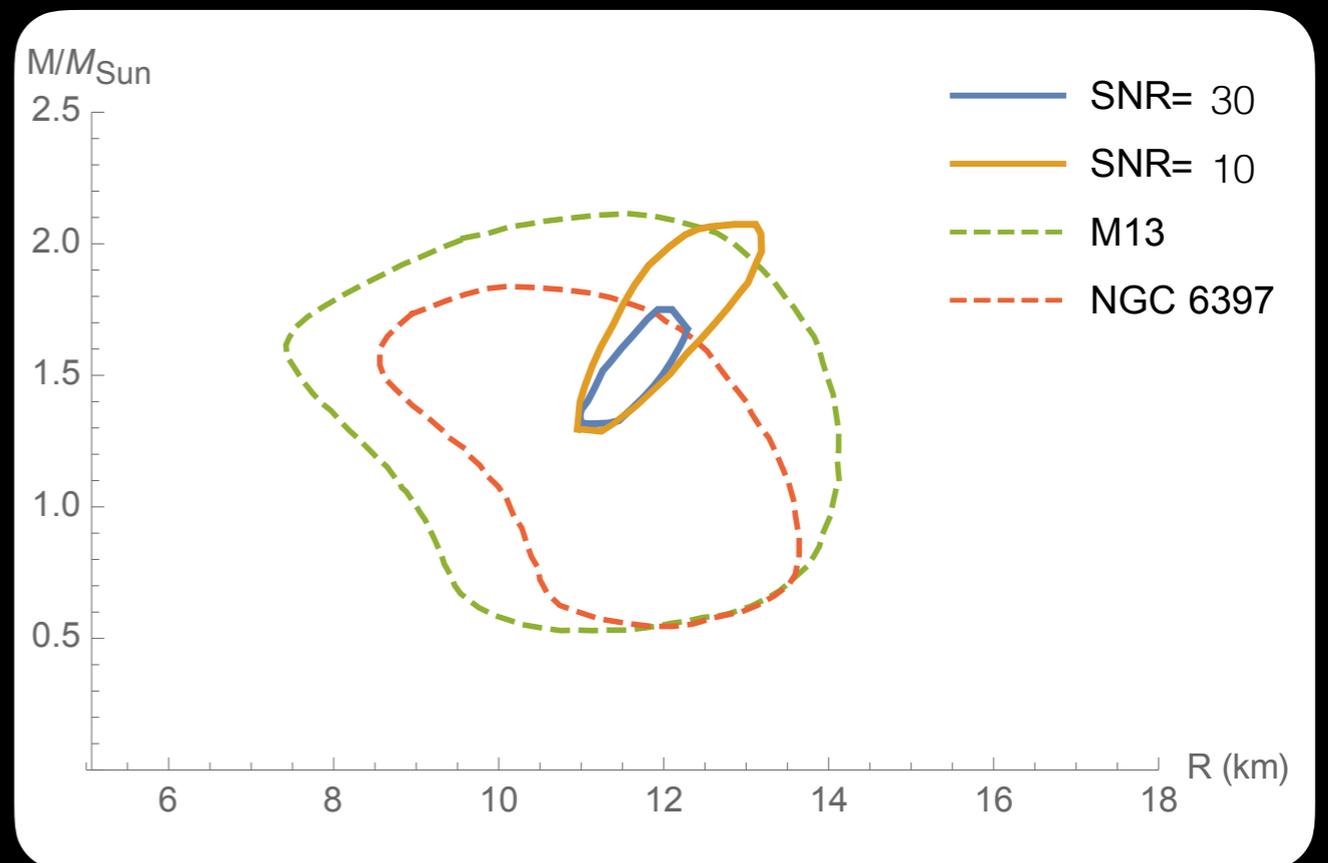
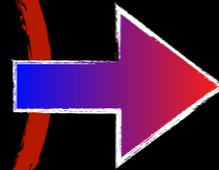
# Results

Parameters of Injection:  $M_{BH} = 4.84 M_{\odot}$   
 $M_{NS} = 1.35 M_{\odot}$   $E_{\gamma,ISO} = 10^{50} \text{ erg}$   
 $\chi_{BH} = 0.48$



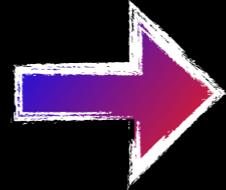
# Comparison with other methods

Comparison between our results (those in previous slides) and results from observation of two qLMXBs



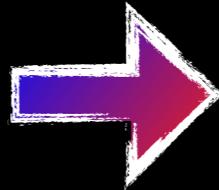
# Conclusions

Summary



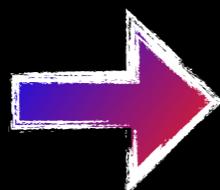
- Coalescing NS-BH binaries are promising LIGO-Virgo sources
- They are also possible progenitors of sGRB
- We developed a method to measure NS radii using a sGRB-GW joint detection.

Cons



- **Model dependent** method (but this is a common drawback)
- **Low rate of joint detection** with present facilities (but **NOT with third generation interferometers!**)

Pro



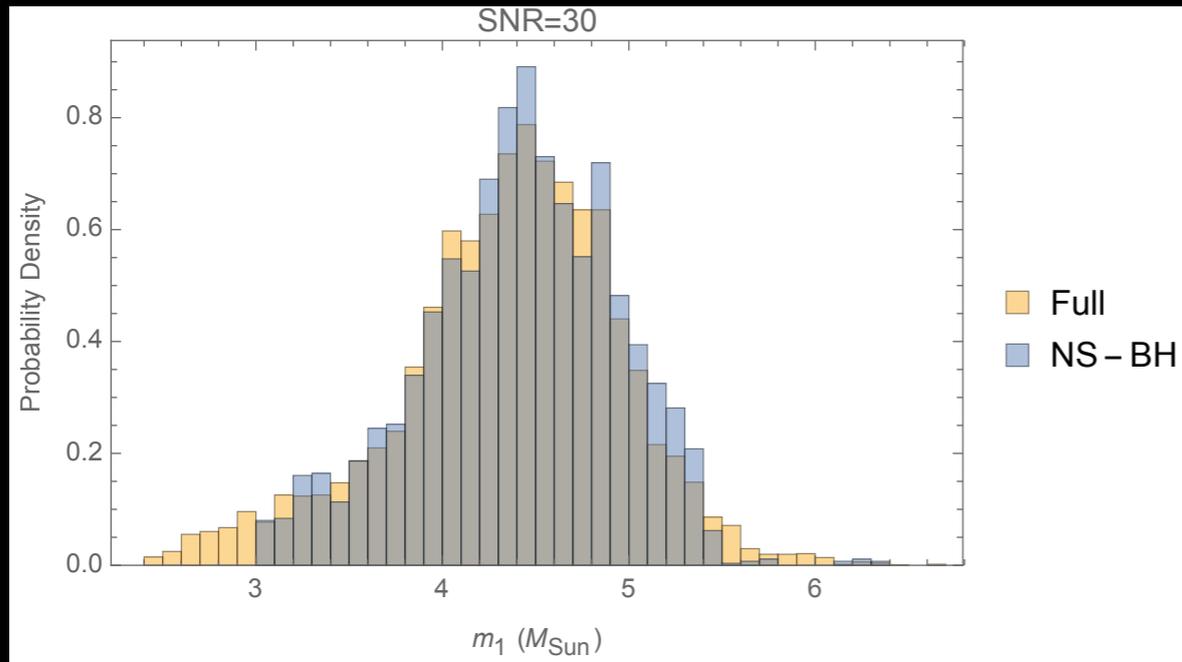
- **Radically different** from other methods, **enables cross-checks** with other methods.
- For realistic SNR we are below to **7% of accuracy**

**Thank you for your attention!**



# Prior/Posterior Distribution from GW Parameter estimation

$m_1$



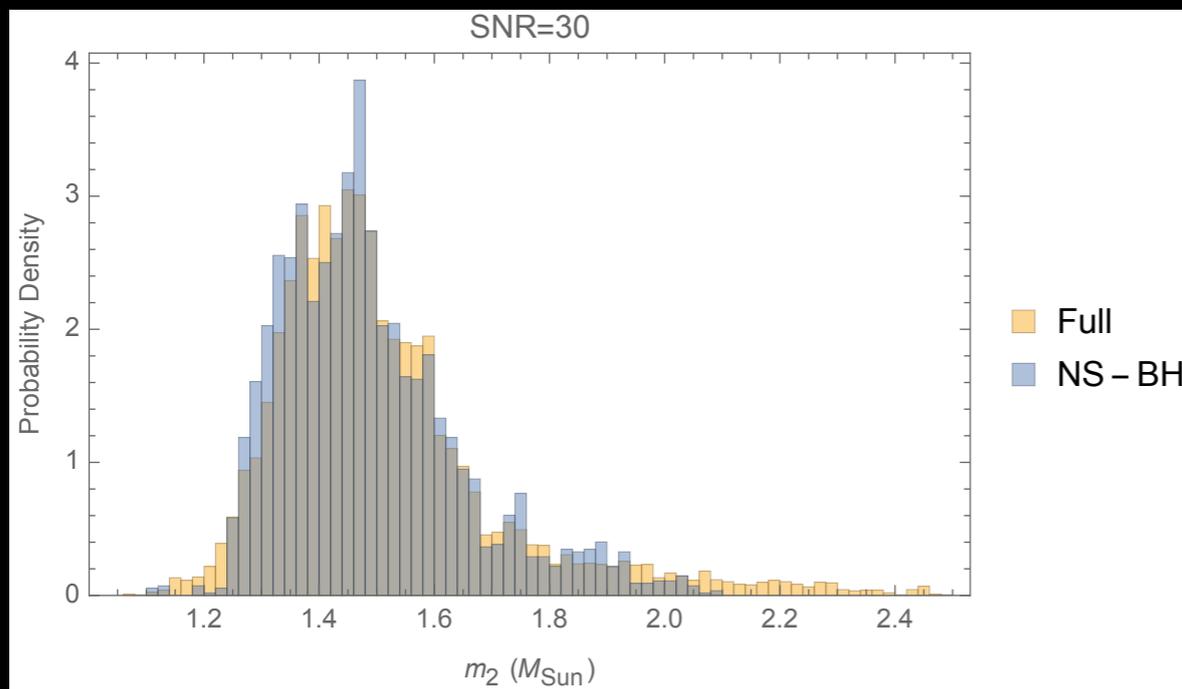
$$m_1 = 4.84 M_{\odot}$$

$$m_2 = 1.35 M_{\odot}$$

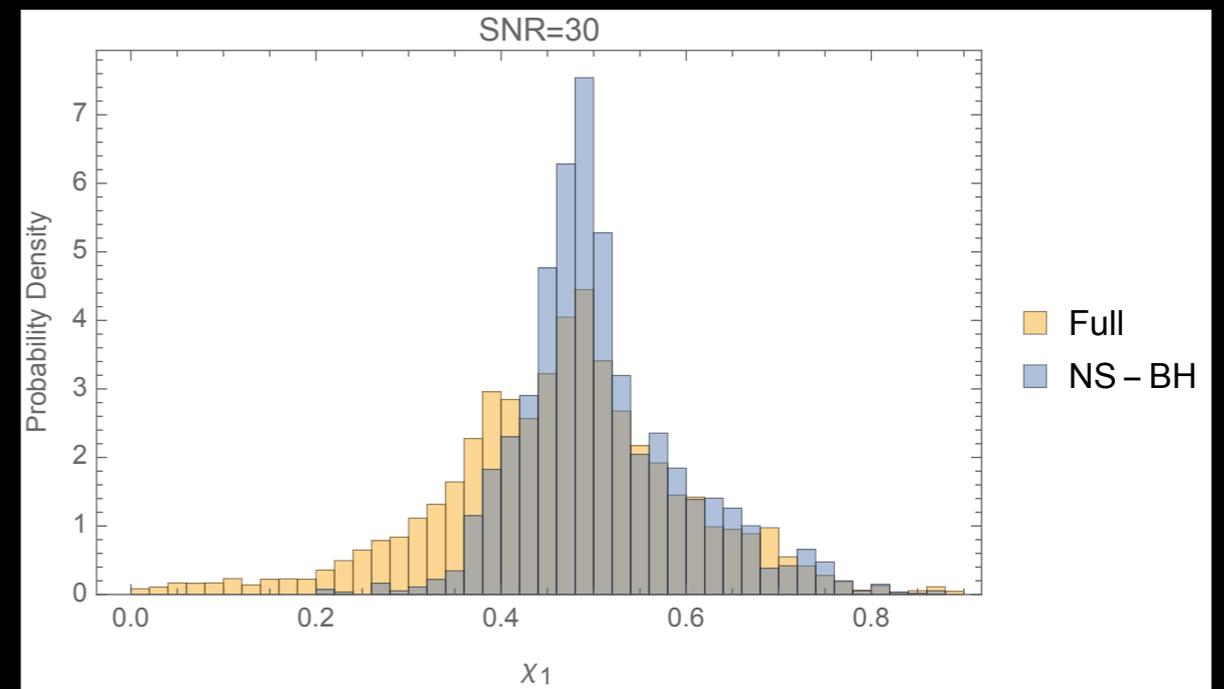
$$\chi_1 = 0.48$$

$$\text{SNR} = 30$$

$m_2$



$\chi_1$

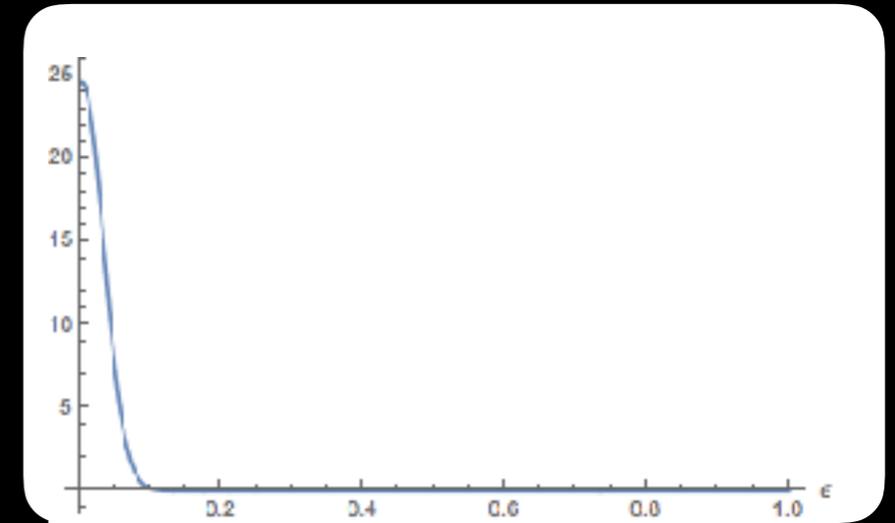


# Prior Distribution for the free parameters

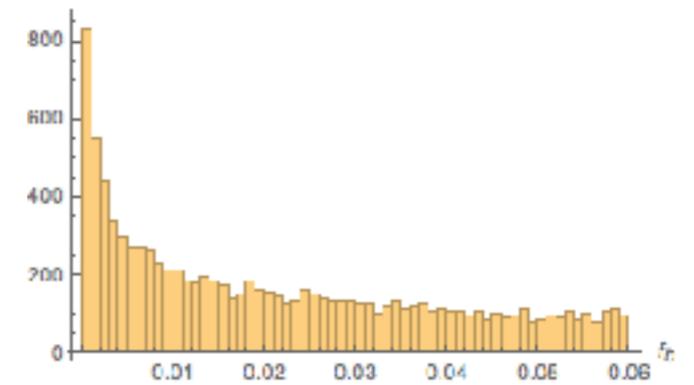
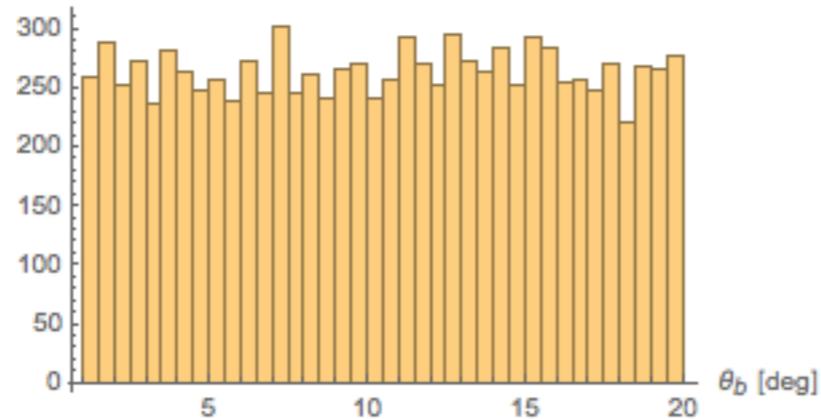
$\epsilon$

$$p(\epsilon) = N \times \exp\left[-\frac{(\epsilon - \mu)^2}{2\sigma^2}\right] \Theta(\epsilon)$$

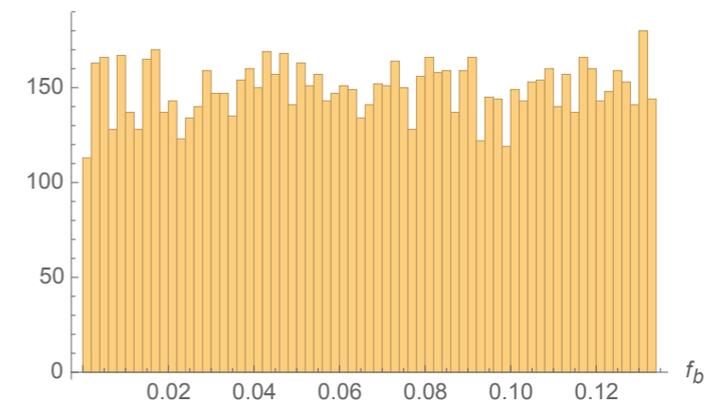
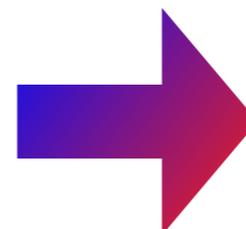
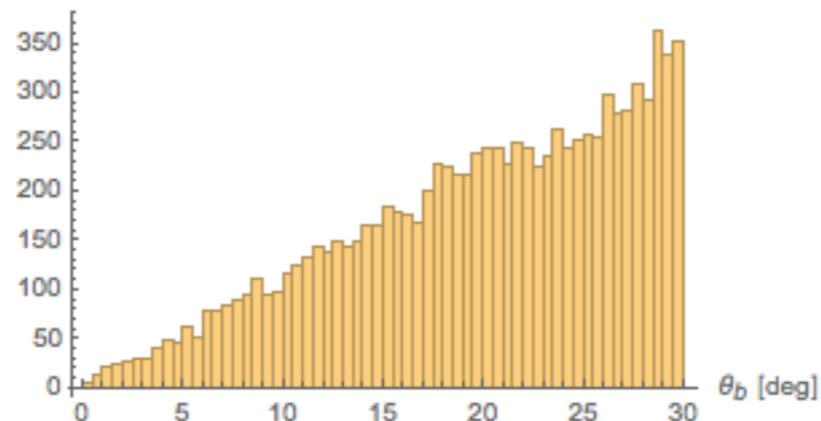
$\theta_b$



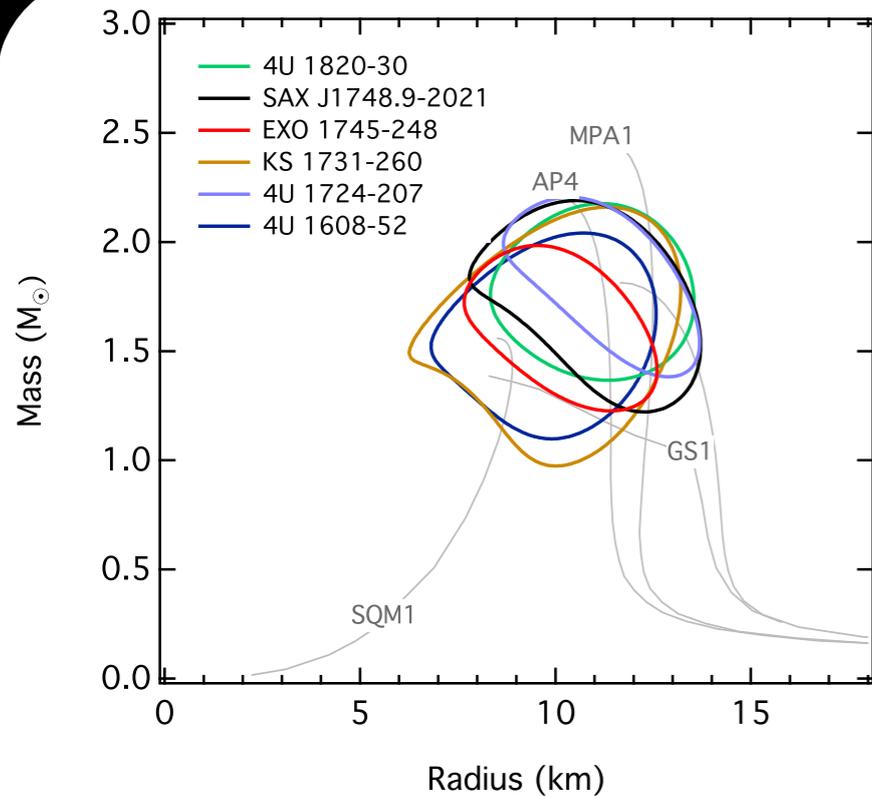
Flat beaming angle in  
[1°-20°]



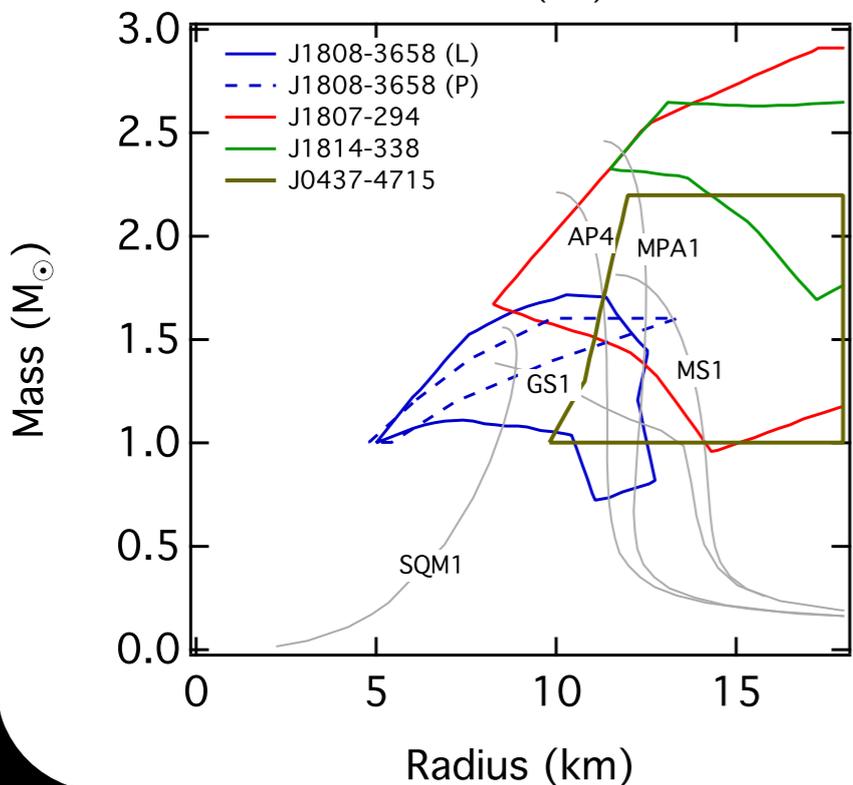
Flat cos beaming angle in  
[cos(30°)-cos(1°)]



# Measuring NS Radii



← NS with  
thermonuclear  
bursts

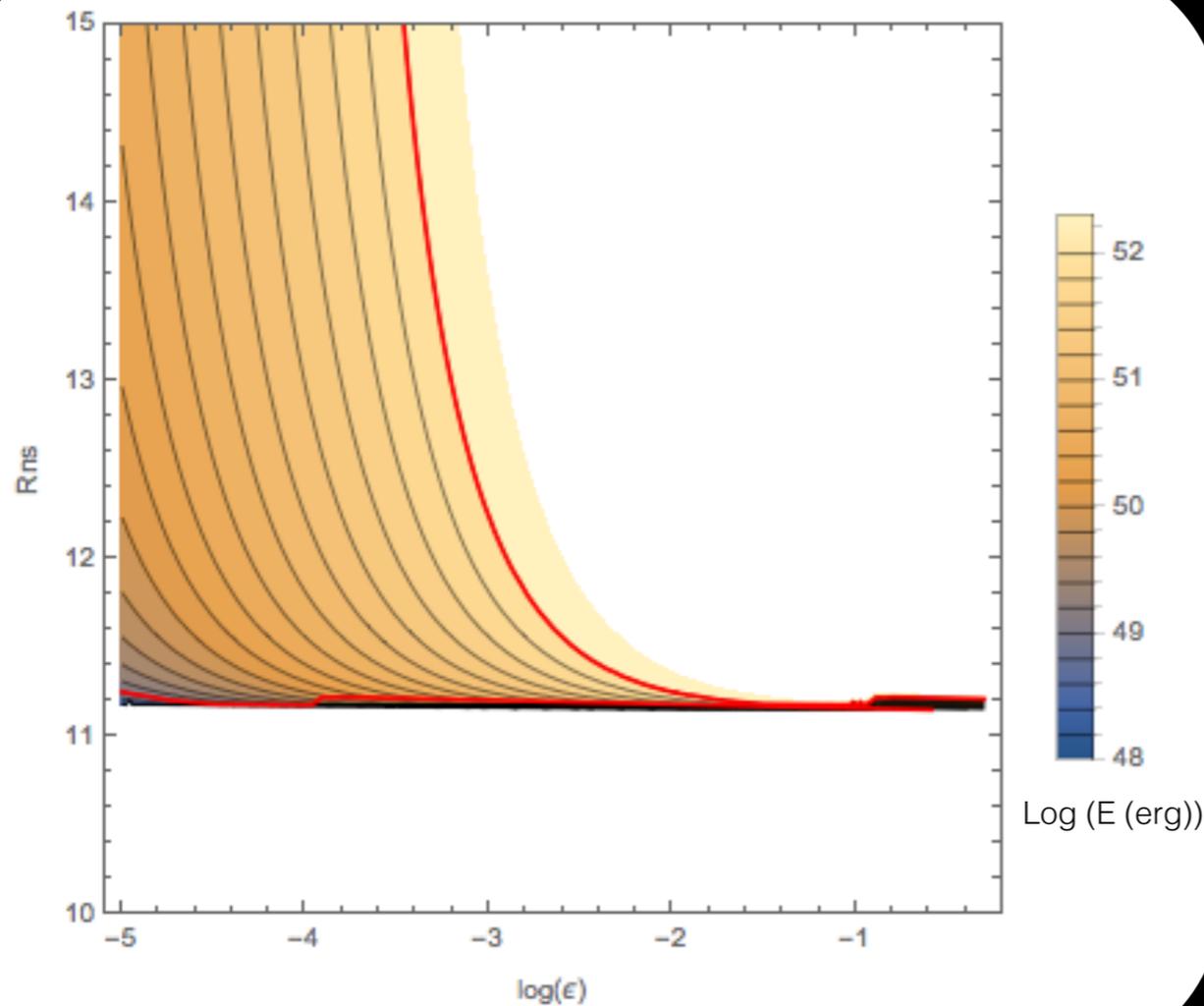


← Accreting Pulsars

## Common Drawbacks

- Source distance required
- ISM absorption required
- Low (multipolar) source magnetic field required
- Model dependency (spacetime geometry, stellar atmosphere, hot spots geometry)
- Absolute X-ray flux calibration

# Efficiency-Radius degeneracy



There is a degeneracy between the radii and the efficiency, but for “sufficiently low” energy this degeneracy is mitigated

$$R_{NS} = \frac{2\alpha(3q)^{1/3} M_{NS} + \beta R_{ISCO}}{\alpha(3q)^{1/3} - \frac{E_\gamma}{\epsilon M_{NS}^b}}$$

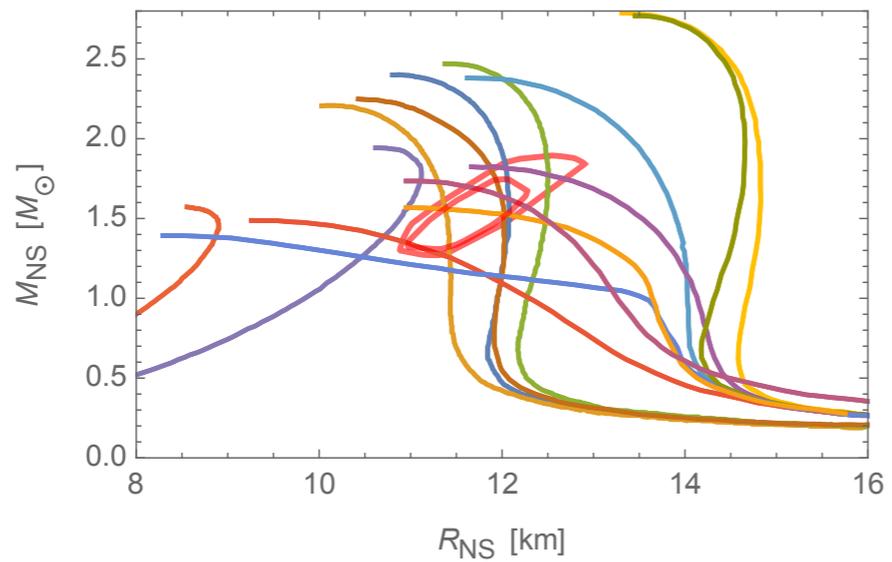
$$E_\gamma = 10^{50} \text{ erg}$$

$$\epsilon \gg 10^{-3}$$

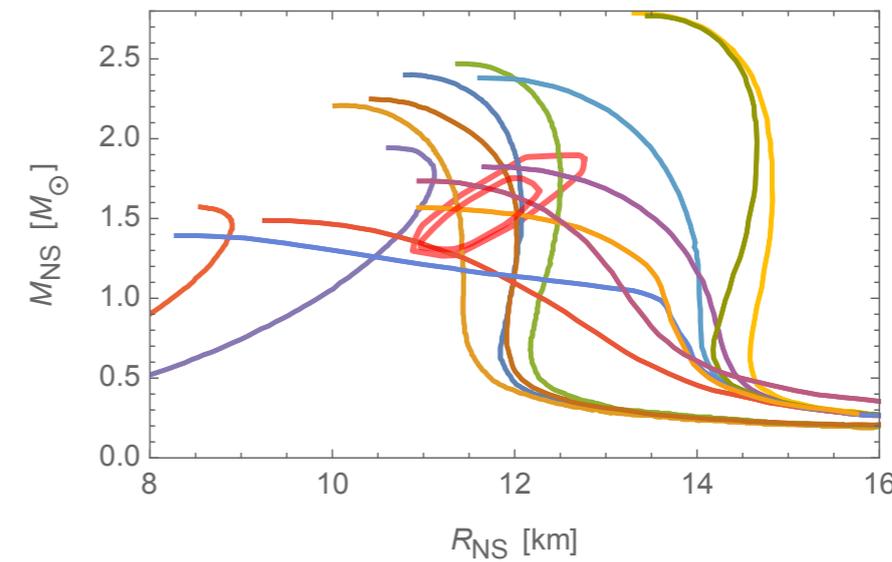
“Sufficiently low” means that this ratio has to be negligible

# More Results...

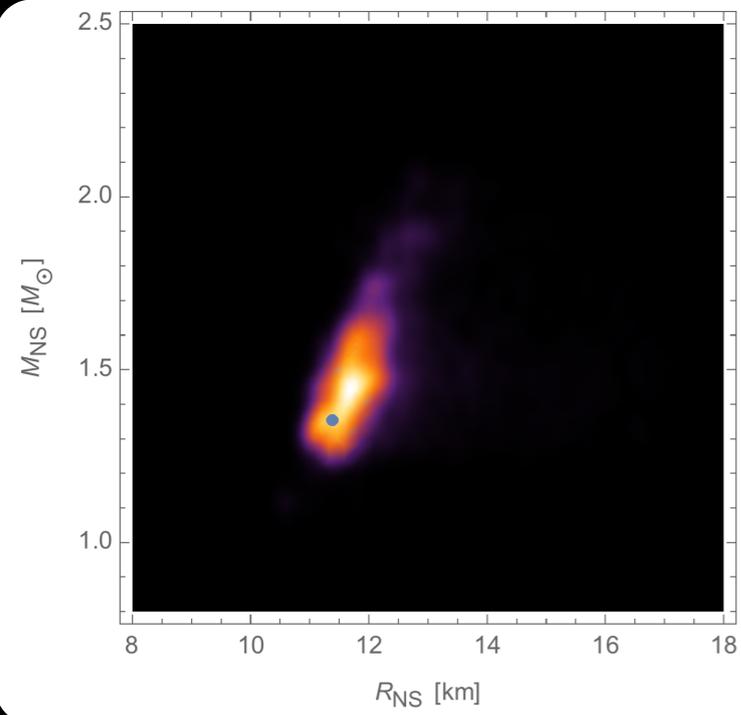
SNR = 30



Flat beaming angle in  $[1^\circ-20^\circ]$   
 $E_{\gamma,ISO} = 10^{50} \text{ erg}$

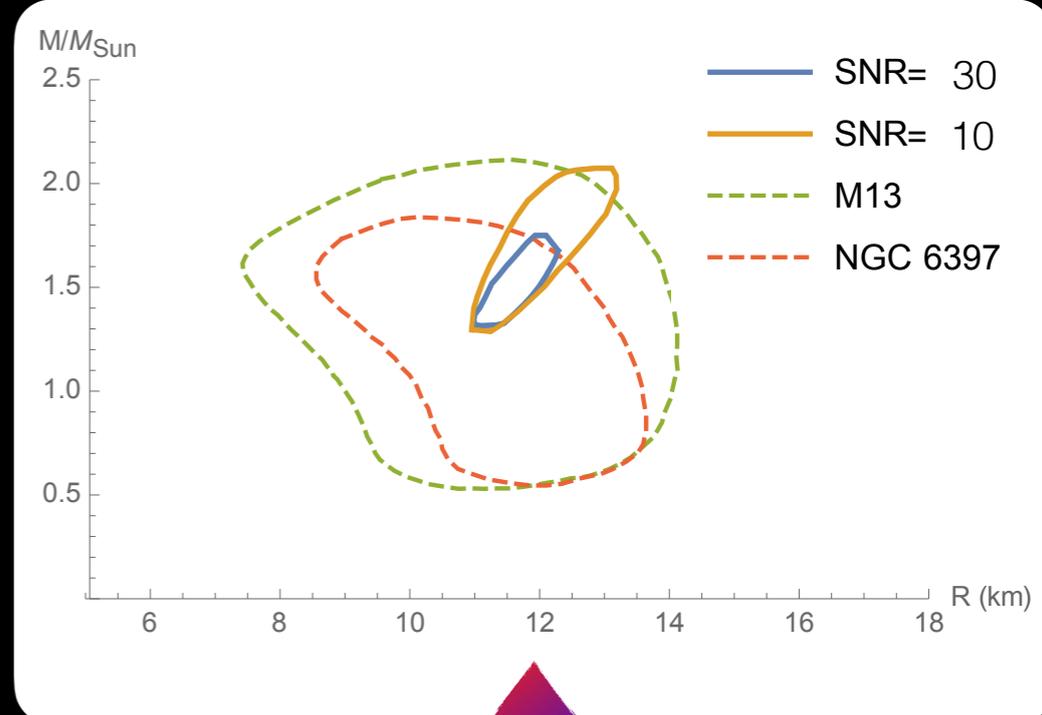
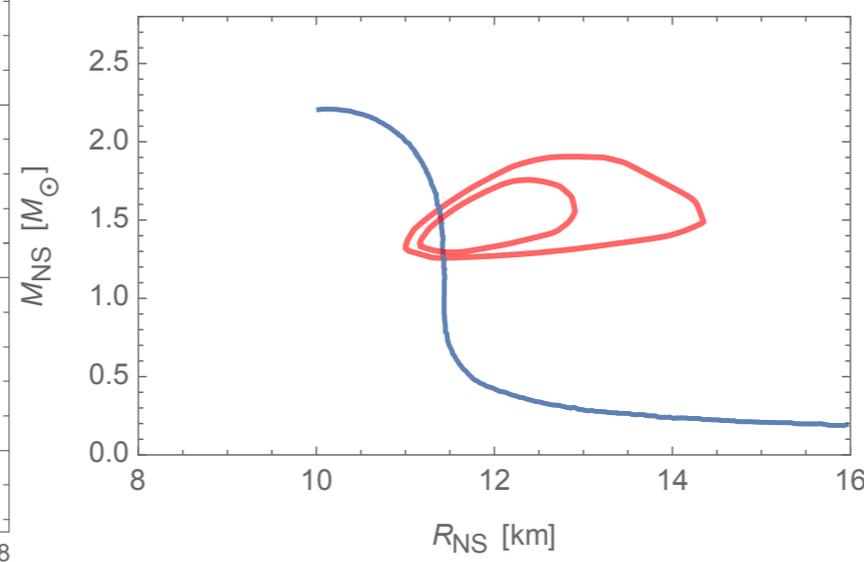


Flat cos beaming angle in  $[\cos(30^\circ)-\cos(1^\circ)]$   
 $E_{\gamma,ISO} = 10^{50} \text{ erg}$



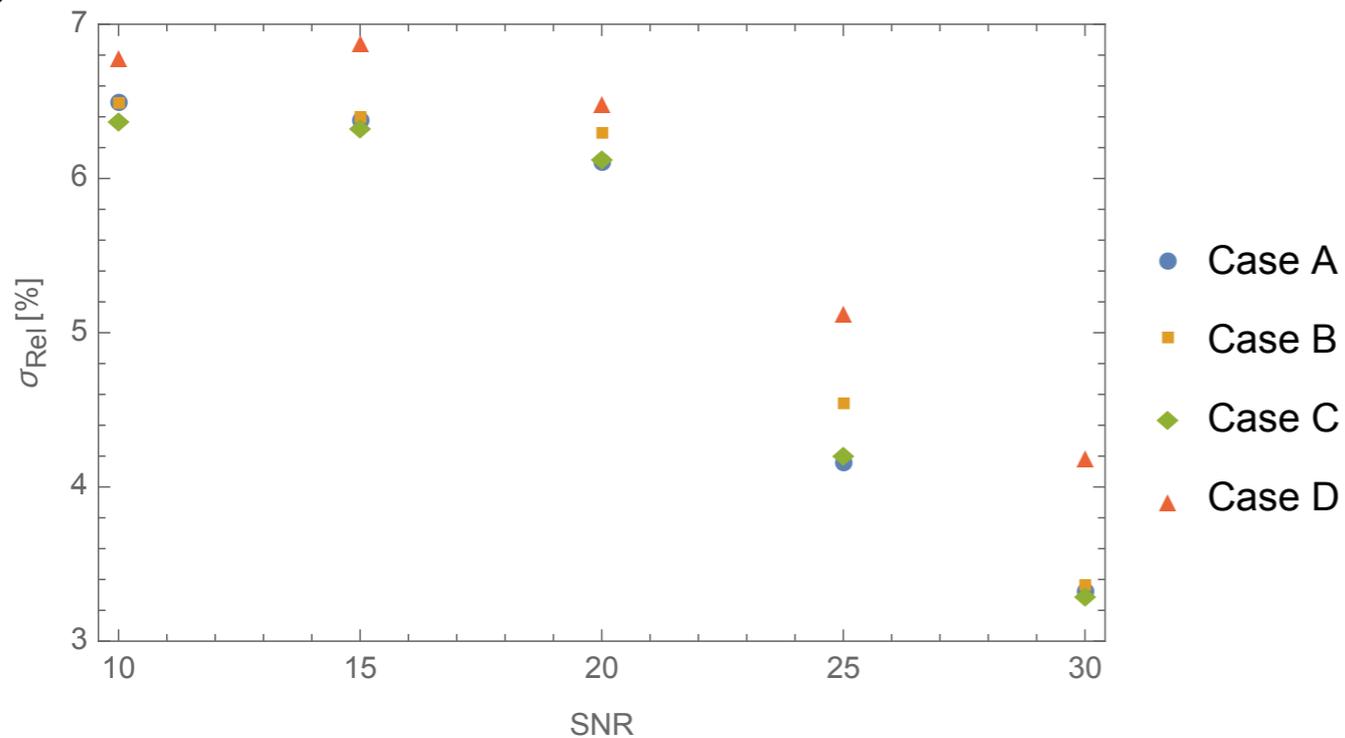
Predictivity Test: We are able to reconstruct an injected NS

Injected EOS = APR4



Comparison between our results (those in previous slides) and results from observation of two qLMXBs

# More Results...



## Accuracy as a function of SNR for different choice of parameters

- Cases A and B have  $E_{\gamma,ISO} = 10^{50} \text{ erg}$
- Cases C and D have  $E_{\gamma,ISO} = 5 \times 10^{51} \text{ erg}$
- Cases A and C have a flat prior in the beaming angle in the range  $[1^\circ, 20^\circ]$
- Cases B and D have a flat prior in the cos of beaming angle in the range  $[\cos(30^\circ), \cos(1^\circ)]$

Higher energy translates in higher degeneracy between parameters

# Rates

Epoch	Run Duration	BNS Range (Mpc)		Number of NSBH Detections	Number of GW-GRB Detections		
		LIGO	Virgo		All Sky	<i>Fermi</i> GBM	<i>Swift</i> BAT
2015	3 months	70–130	...	0.0001–1	$3 \times 10^{-4}$ –0.06	$2 \times 10^{-4}$ –0.03	$4 \times 10^{-5}$ –0.007
2016–17	6 months	130–200	30–100	0.002–10	0.005–0.5	0.003–0.3	$7 \times 10^{-4}$ –0.07
2017–18	9 months	200–280	100–140	0.01–40	0.03–2	0.02–1	0.004–0.3
2019+	(per year)	330	110–220	0.05–100	0.2–6	0.1–2	0.02–0.5
2022+	(per year)	330	220	0.1–200	0.4–10	0.2–3	0.03–0.7

$z_{max, NSBH} \simeq 4$  (ET design study <http://www.et-gw.eu/etdsdocument>)

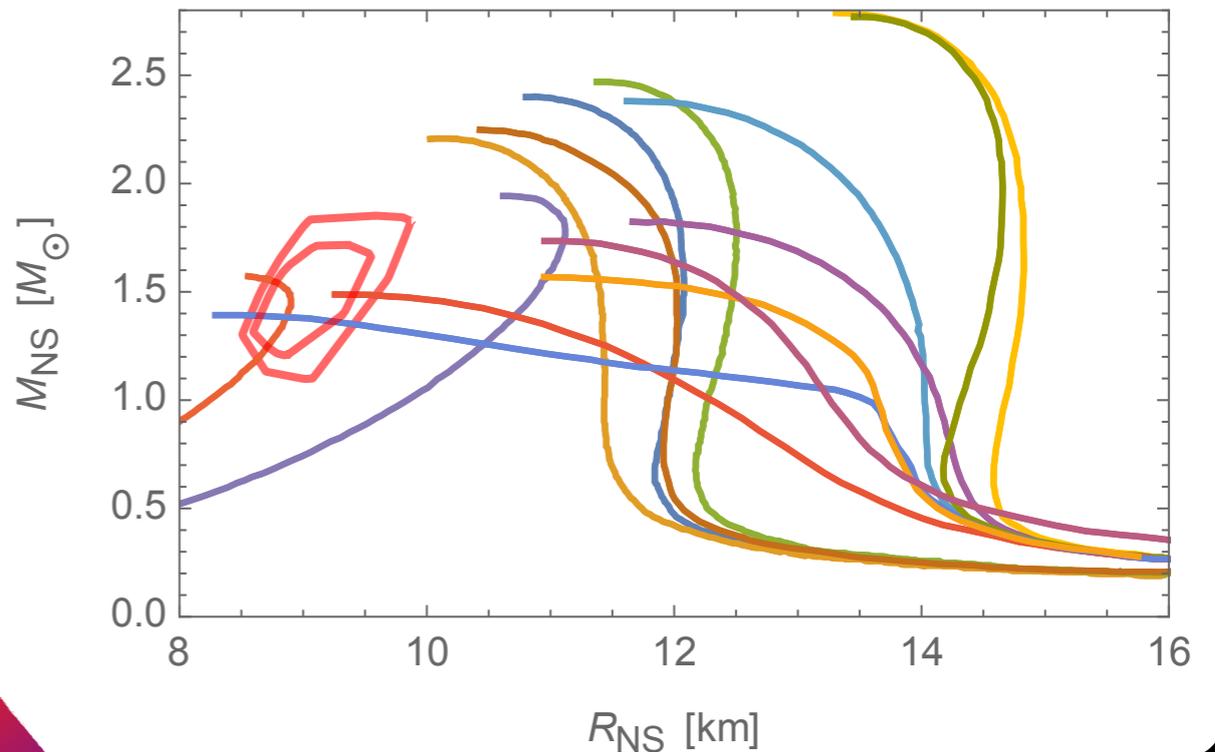
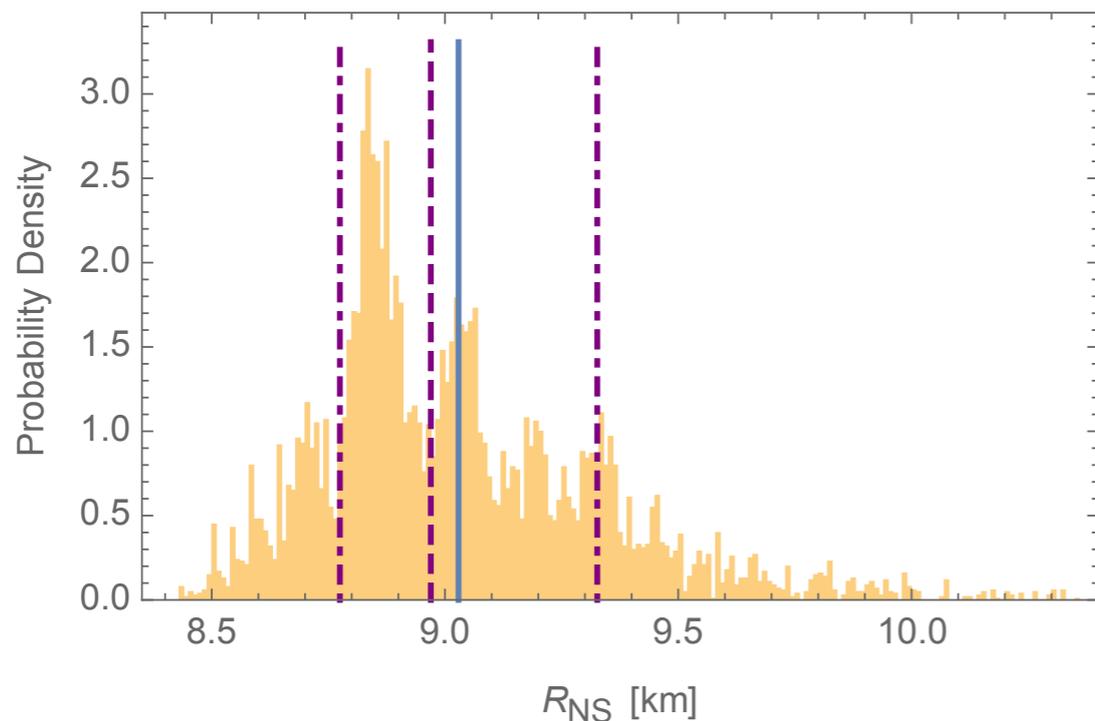
**ET**

Source	BNS	NS-BH	BBH
Rate ( $\text{Mpc}^{-1} \text{Myr}^{-1}$ )	0.1–6	0.01–0.3	$2 \times 10^{-3}$ –0.04
Event Rate ( $\text{yr}^{-1}$ ) in aLIGO	0.4–400	0.2–300	2–4000
Event Rate ( $\text{yr}^{-1}$ ) in ET	$\mathcal{O}(10^3\text{--}10^7)$	$\mathcal{O}(10^3\text{--}10^7)$	$\mathcal{O}(10^4\text{--}10^8)$

# More Results...

A case with higher  
BH spin...

$$\begin{aligned} m_1 &= 4.84 M_\odot & \chi_1 &= 0.80 \\ m_2 &= 1.35 M_\odot & z &= 0.03 \end{aligned}$$



Different GW parameters allows to  
probe different regions in the mass-  
radius plane !