

University of  
Zurich<sup>UZH</sup>

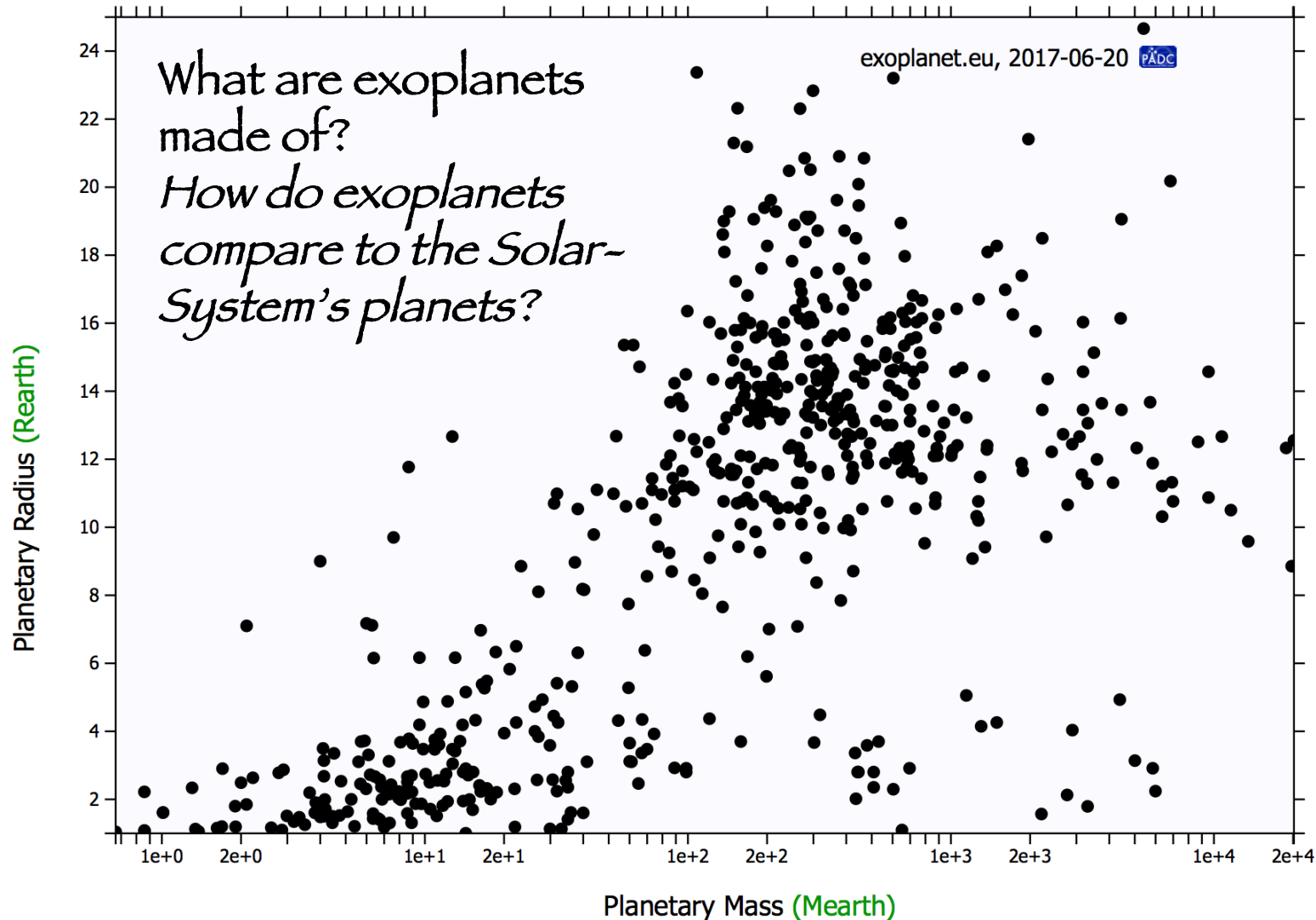
# Challenges in Exoplanet Characterization

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Institute for Computational Science  
Center for Theoretical Astrophysics & Cosmology,  
University of Zurich

# Exoplanets Discovery → Exoplanets Characterization

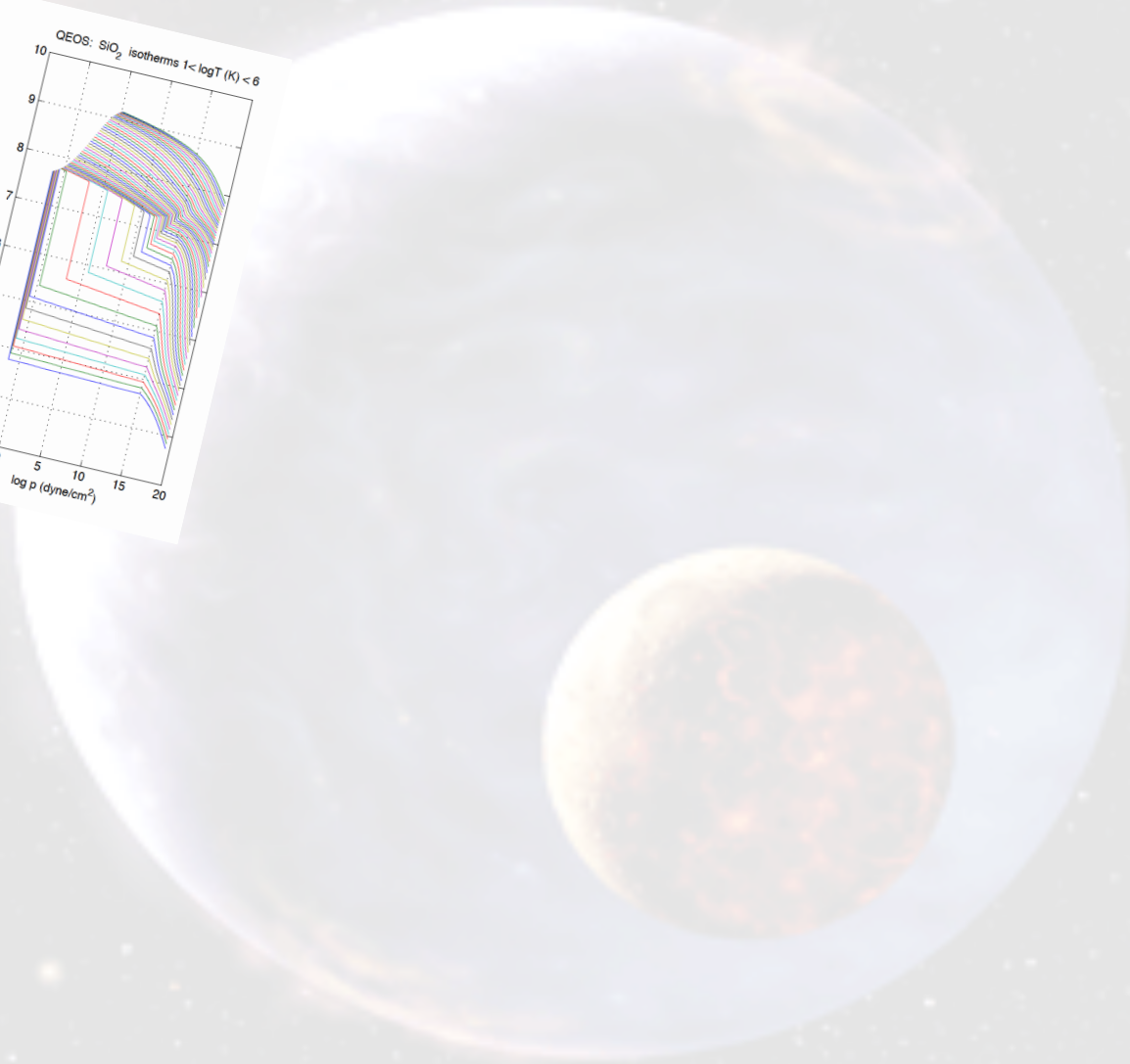
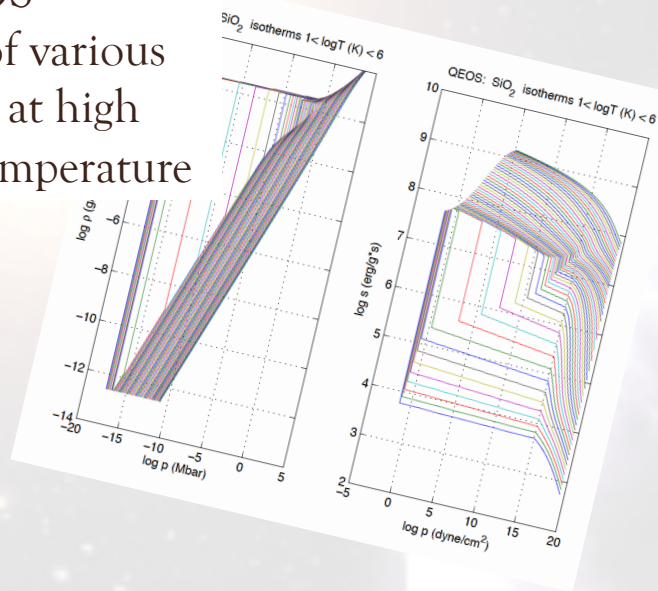
Planets are diverse: a large variety of masses and radii



# Main sources of uncertainty/open issues

## EOS

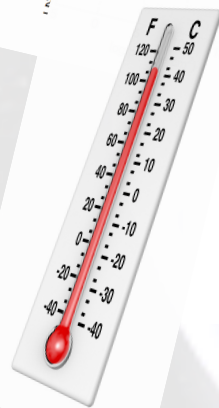
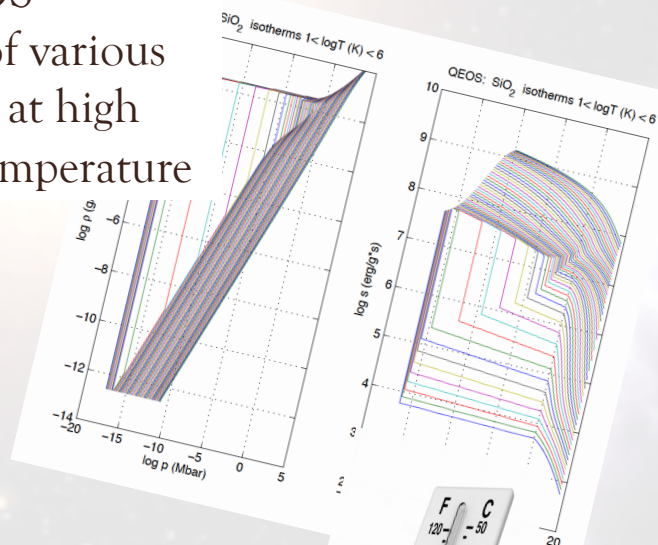
Behavior of various materials at high pressure/temperature



# Main sources of uncertainty/open issues

## EOS

Behavior of various materials at high pressure/temperature

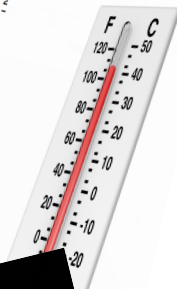
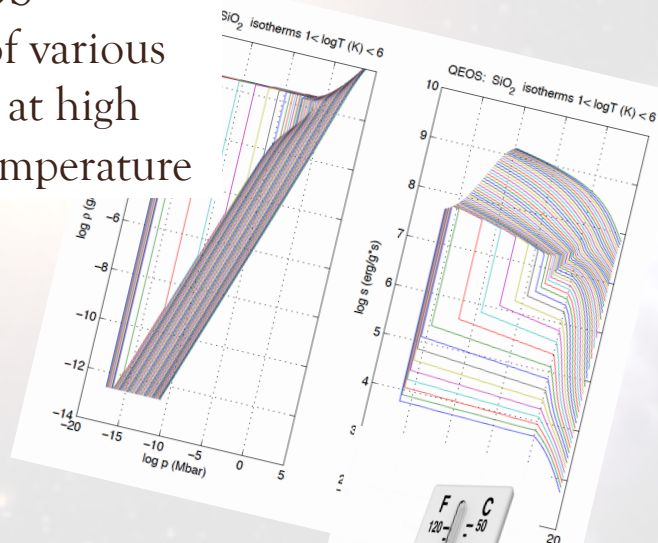


Temperature  
(radial distance)  
Different planetary  
type?

# Main sources of uncertainty/open issues

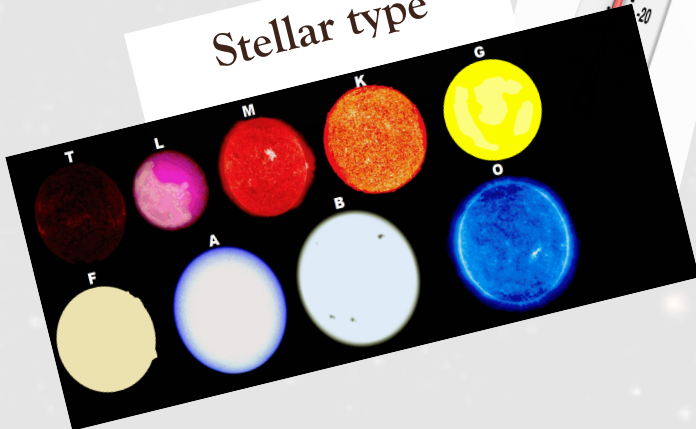
## EOS

Behavior of various materials at high pressure/temperature



Temperature  
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Different planetary  
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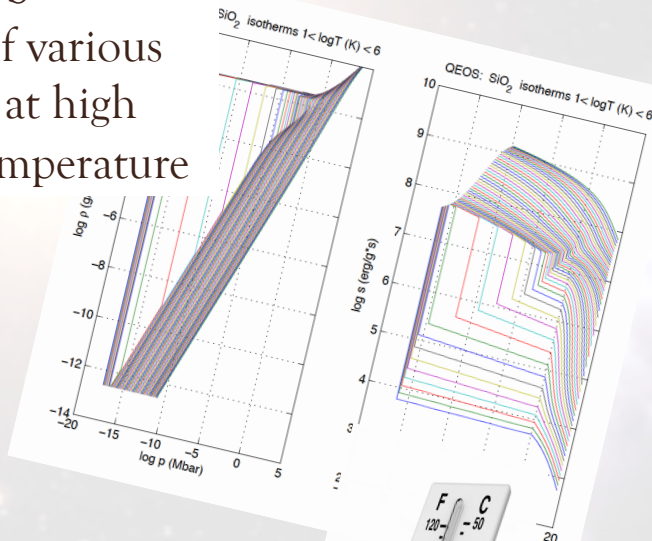
Stellar type



# Main sources of uncertainty/open issues

## EOS

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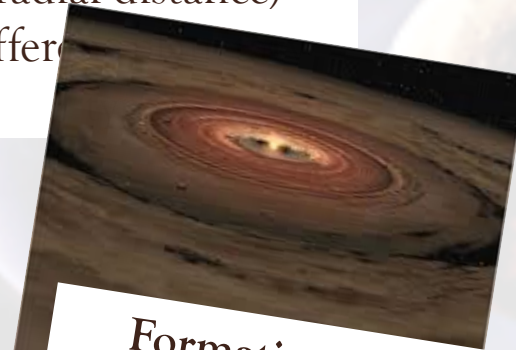


Stellar type



Temperature  
(radial distance)  
Differ

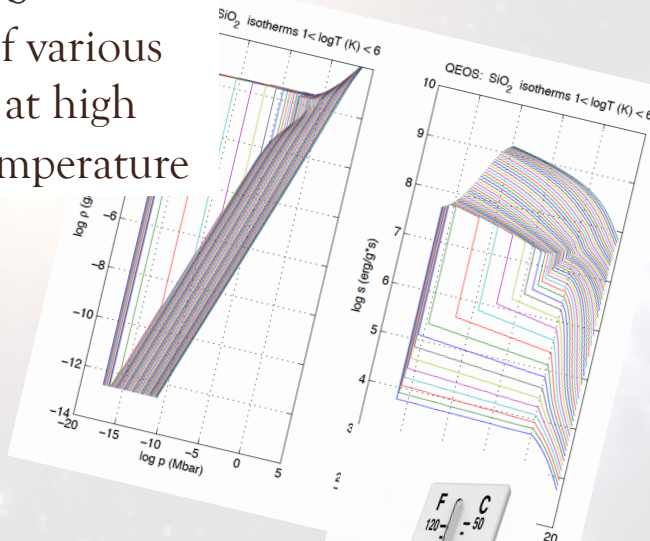
Formation history  
How? Where? When?



# Main sources of uncertainty/open issues

## EOS

Behavior of various materials at high pressure/temperature



Time/Age  
Evolution, time  
dependence

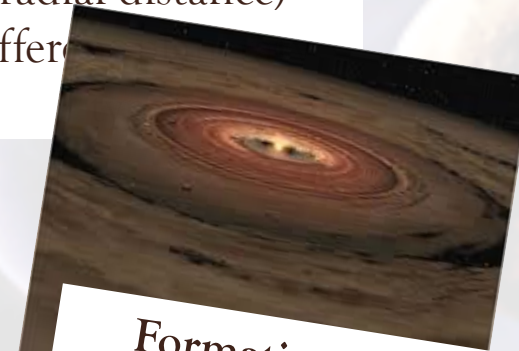


Temperature  
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Stellar type



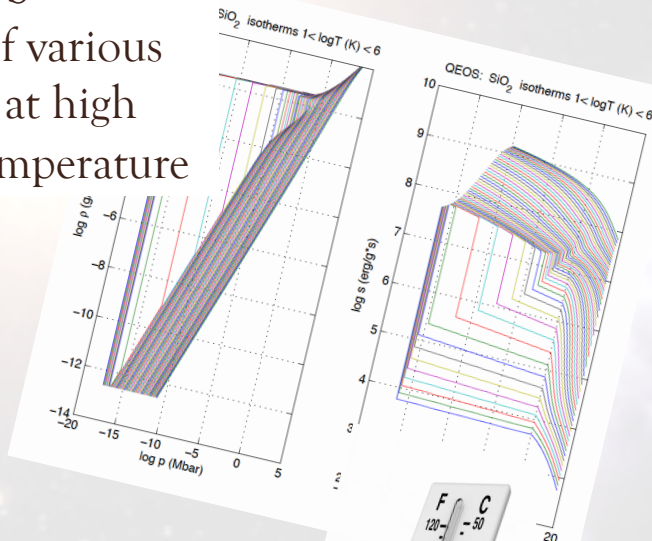
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Stellar type



Formation hist  
How? Where? W.

Evolution  
Atmosphere loss/secondary  
atmospheres, mixing,  
differentiation

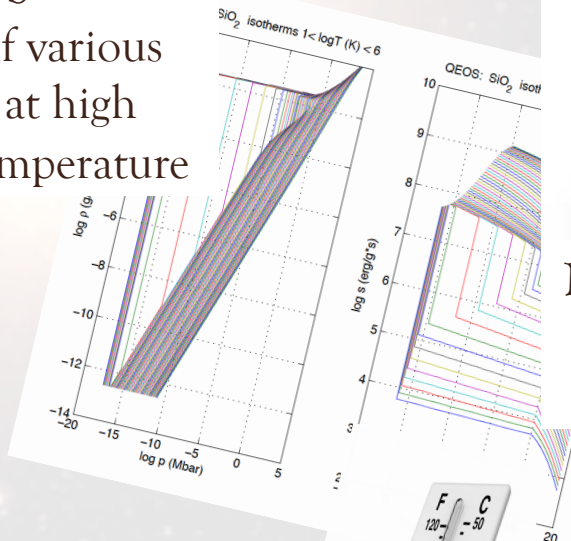




# Main sources of uncertainty/open issues

## EOS

Behavior of various materials at high pressure/temperature

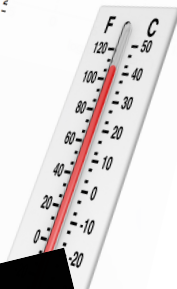


Model assumptions  
Composition,  
internal structure

Time/Age  
Evolution, time  
dependence



Temperature  
(radial distance)  
Differ



Stellar type



Formation hist  
How? Where? W.

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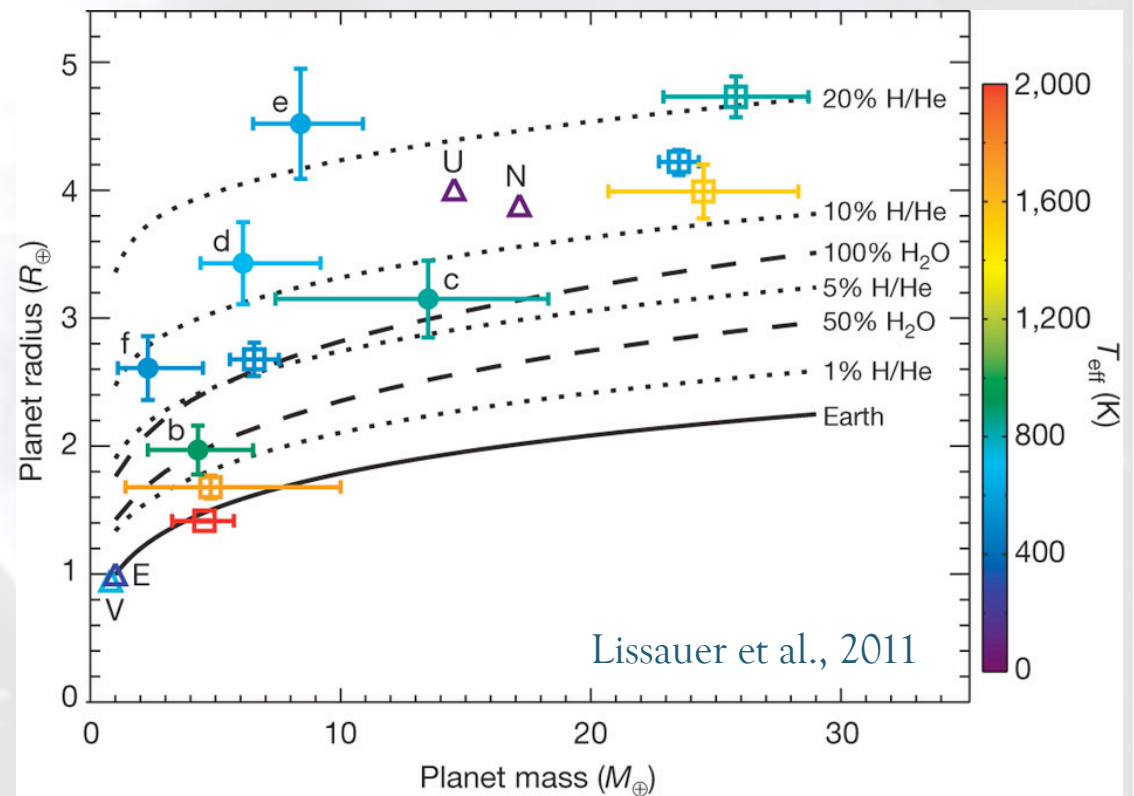


# How do we characterize exoplanets?

Measured mass & radius (M-R diagram)  $\rightarrow$  mean density  $\rightarrow$  composition.  
How can we use the M-R relation to derive composition & internal structure?

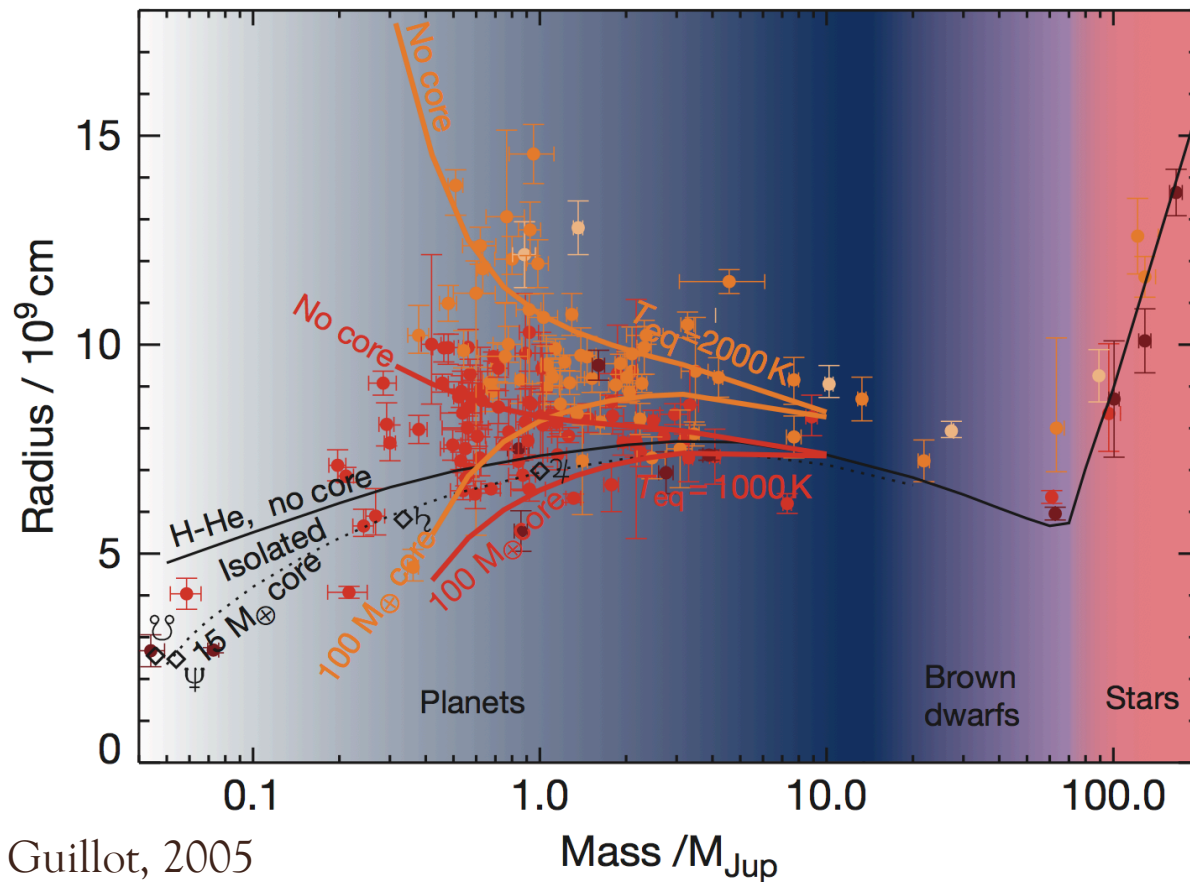
Mean density does **NOT**  
give us the distribution of  
the materials

A very large range of  
compositions will provide  
the *same* mean density



# How do we know that there are heavy elements in giant planets?

The mass-radius relation is a relationship between the radius,  $R$ , of an astrophysical object and its mass,  $M$ .



For stars:  
 $R \propto M$

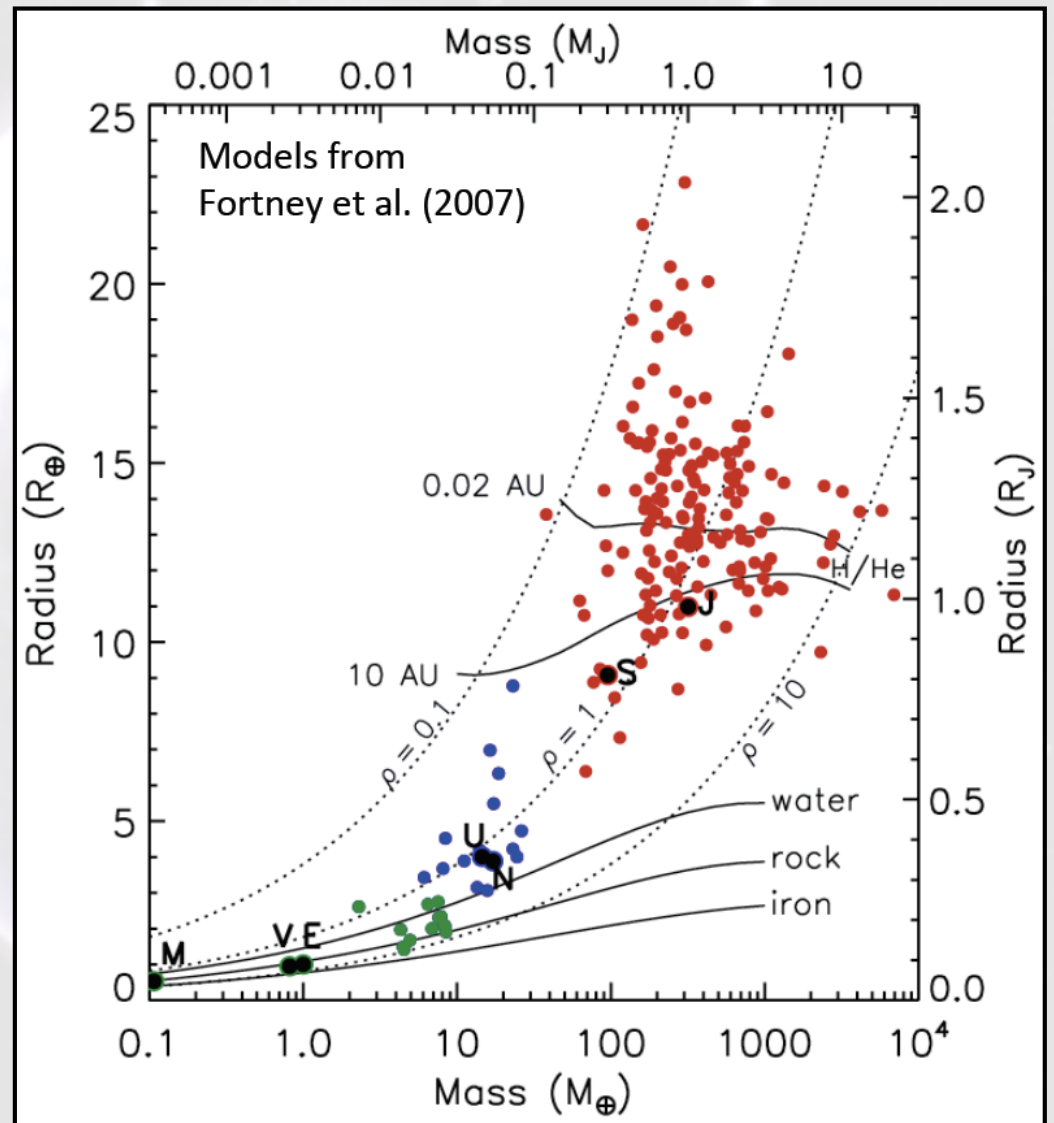
Degenerate pressure:  
 $R \propto M^{-1/3}$

Coulomb pressure  
(small objects):  
 $R \propto M^{1/3}$

# Masses and radii of exoplanets

**\*\*gas giants\*\***

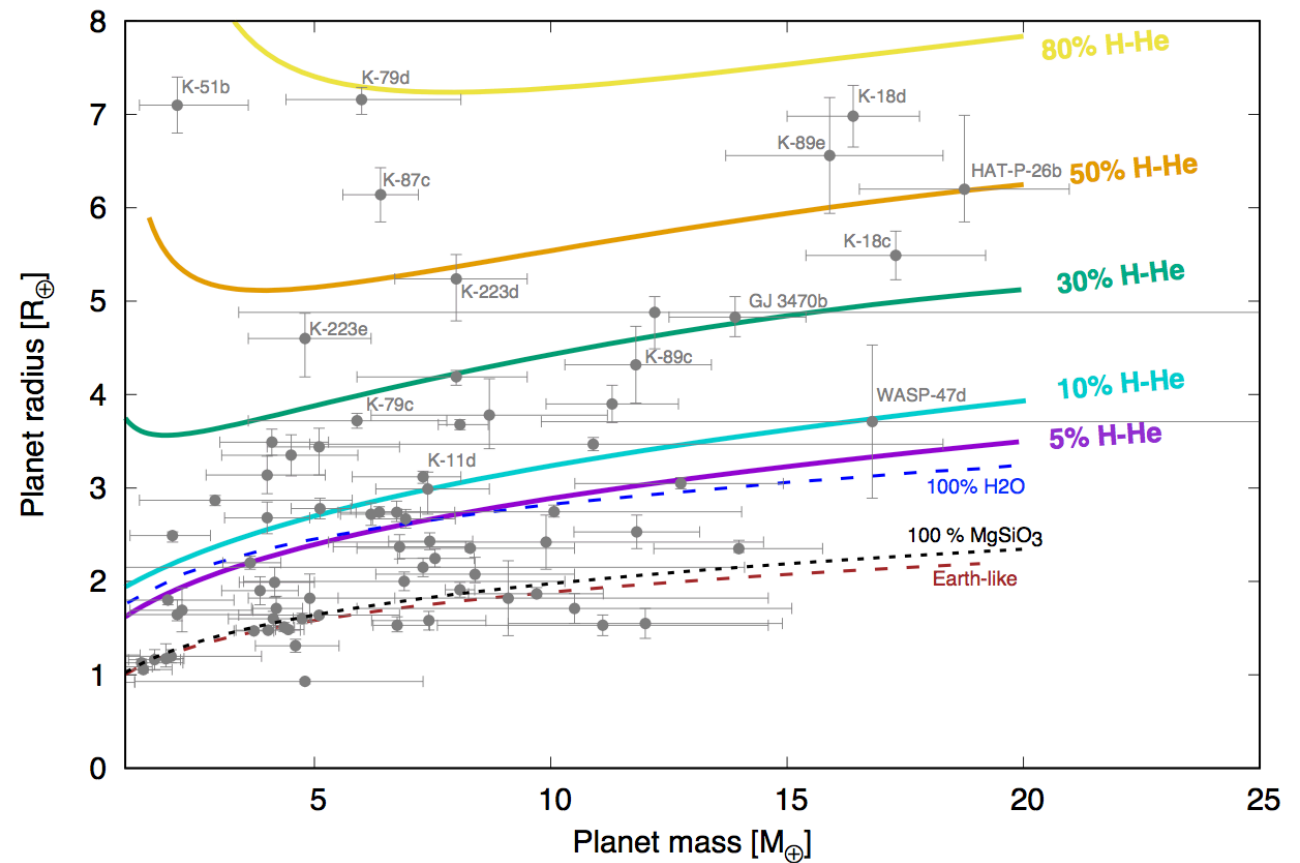
A simple M-R analysis suggests that something occurs in “hot Jupiters”



# Masses and radii of exoplanets

\*\*small/intermediate mass\*\*

For small planets we can try to identify the composition and the existence of an atmosphere



Venturini & Helled, 2017 (submitted)

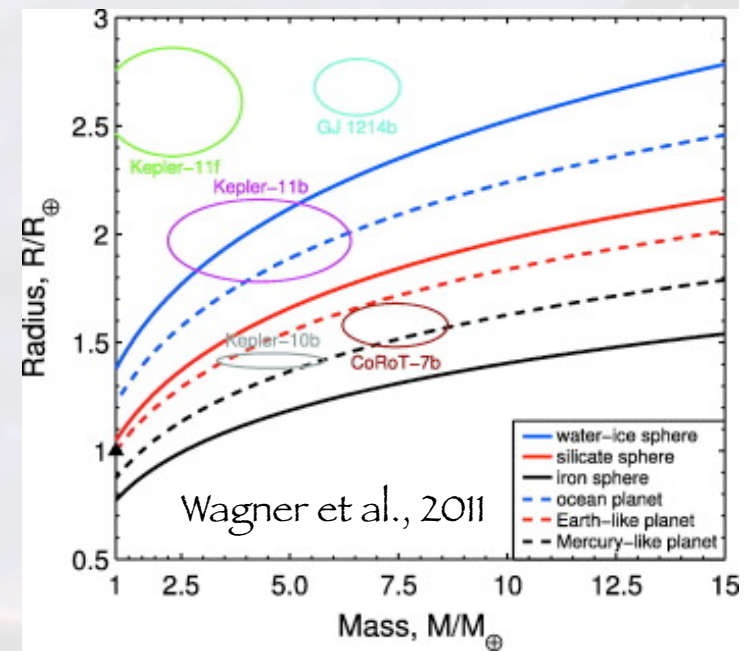
# Exoplanet characterization

## The challenges for theory:

- A degenerate problem: many unknowns and only a few constraints.
- Linking M-R relation and age of the system with planetary evolution.
- Model assumptions:
  - What materials to use?
  - How many layers to assume?
  - Are the materials well-mixed or differentiated?
  - Is the planet fully adiabatic?
  - How to include interior-atmosphere interactions?



Model assumptions  
Composition,  
internal structure



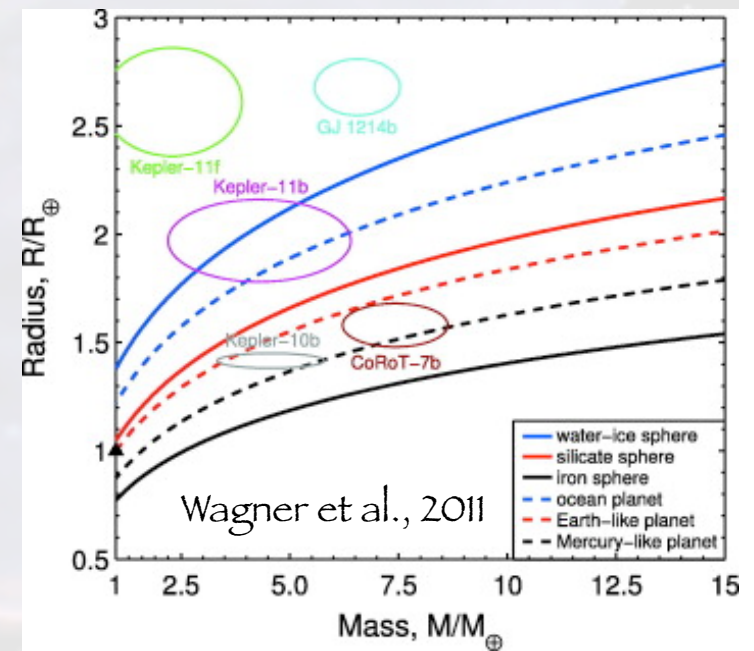
# Exoplanet characterization

## The challenges for theory:

- A degenerate problem: many unknowns
- Linking system with planetary evolution.

Are there compositions which are impossible? more likely?

- Model assumptions:
  - What materials to use?
  - How many layers to assume?
  - Are the materials well-mixed or differentiated?
  - Is the planet fully adiabatic?
  - How to include interior-atmosphere interactions?



# The Mass-Radius (M-R) relation

## Gaseous planets:

- Hydrogen and helium, heavy elements
- Inflated hot-Jupiters (e.g., Guillot et al., 1996; Burrows et al., 2007)
- Cold Jupiters (e.g., Miller & Fortney, 2011)

*Sensitive to temperature, internal structure, heavy element mass, EOS, age*

## Terrestrial planets:

- Super-Earths; mini-Neptunes (e.g., Valencia et al., 2007; Seager et al., 2007)
- Earth-like composition, M-R relation of pure refractory materials

*Sensitive to composition, EOS*

## What about a mixture?

- Exoplanets are diverse – many intermediate mass with volatiles.
- The challenge: temperature, age, and internal structure (Baraffe et al., 2008; Vazan et al., 2013).

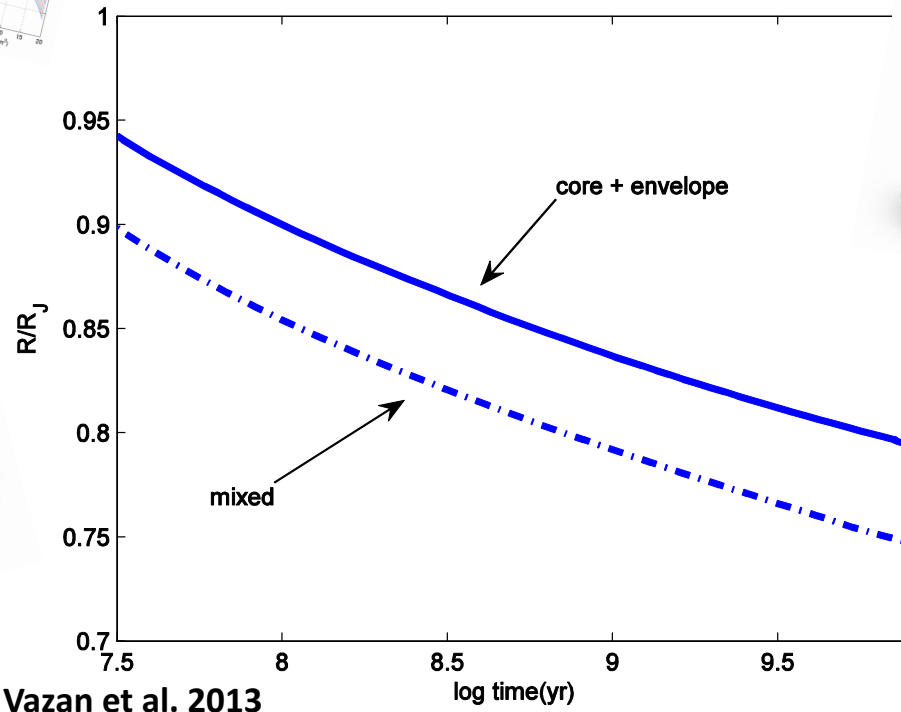
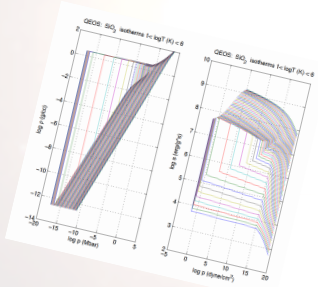


A few examples...



# The importance of the distribution of heavy elements (and EOS)

## Gaseous (massive) planets:



**1  $M_J$  planet**  
 $Z=0.5$

Distribution

$\Delta$  structure  $\sim 7\%$

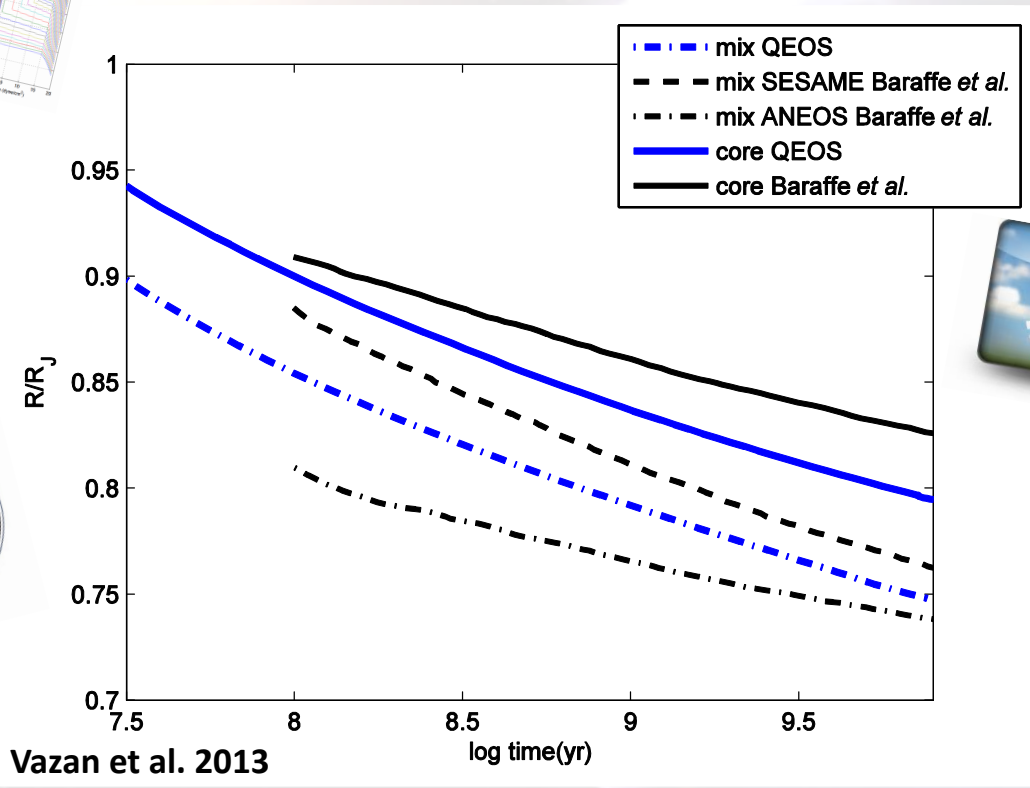
EOS

$\Delta$ EOS = 10%  
(Baraffe et al. 2008)

$M$ - $R(t)$  is affected by the heavy-element distribution in metal-rich giant planets.

# The importance of the distribution of heavy elements (and EOS)

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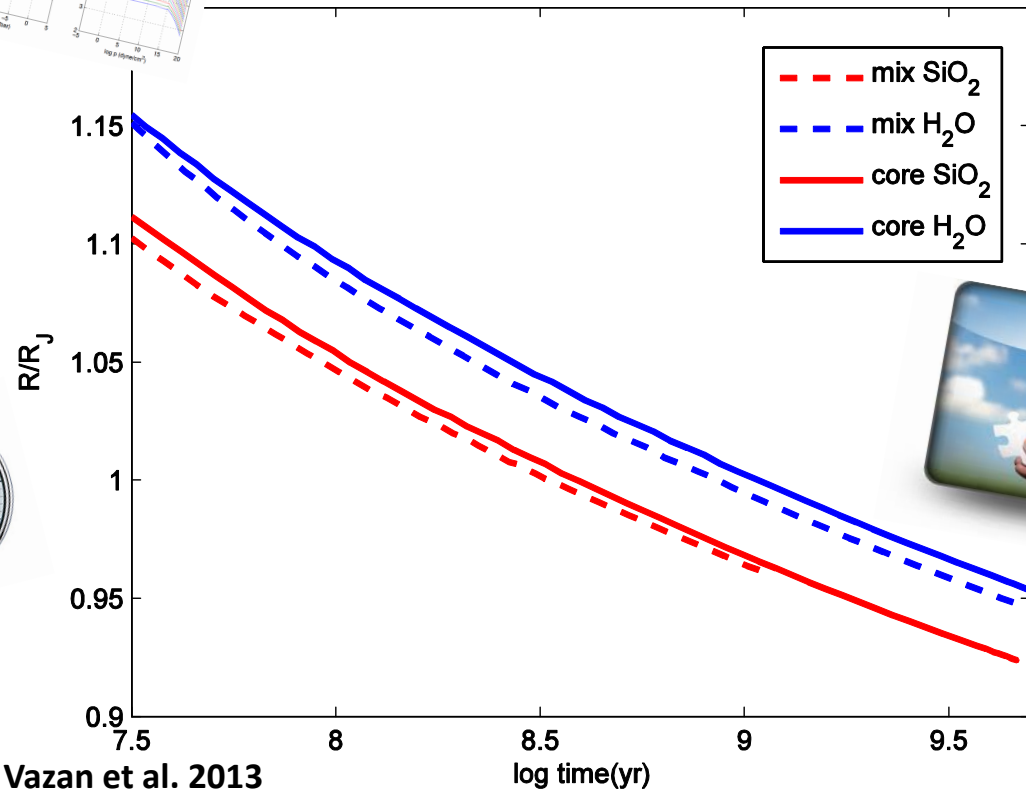
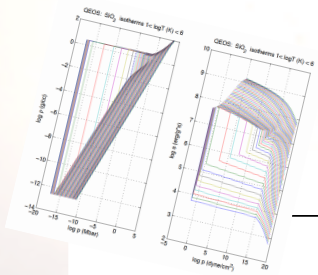
EOS

$\Delta$ EOS = 10%

M-R(t) is affected by the heavy-element distribution in metal-rich giant planets.

# The importance of the distribution of heavy elements (and EOS)

## Gaseous (massive) planets:



**1  $M_J$  planet**  
 $Z=0.2$

Composition  
 $\Delta \text{rock-ice} \sim 5\text{-}15\%$



Vazan et al. 2013

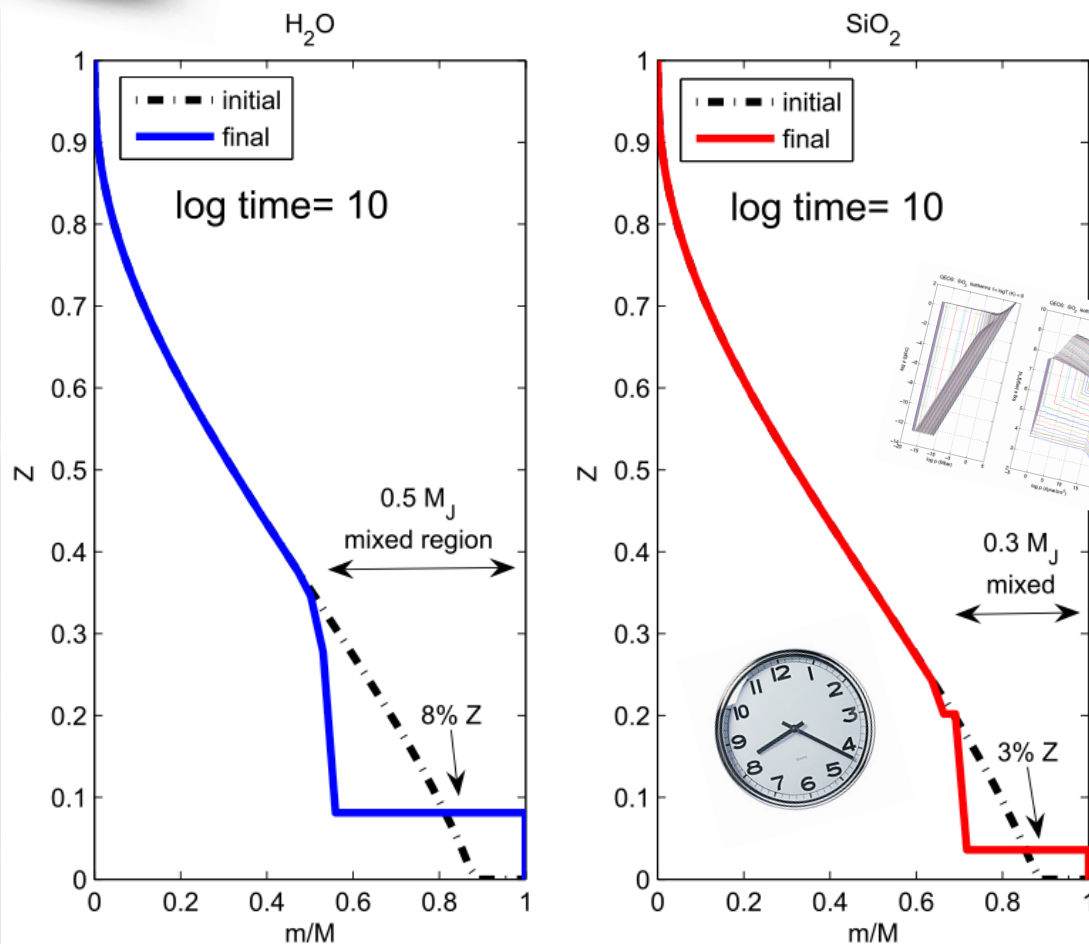
For  $Z \leq 0.2$  the M-R relation is less sensitive to the assumed distribution.

# The importance of composition gradients

## Effect of composition



Gaseous (massive) planets:



1 M<sub>J</sub> with Z=0.35

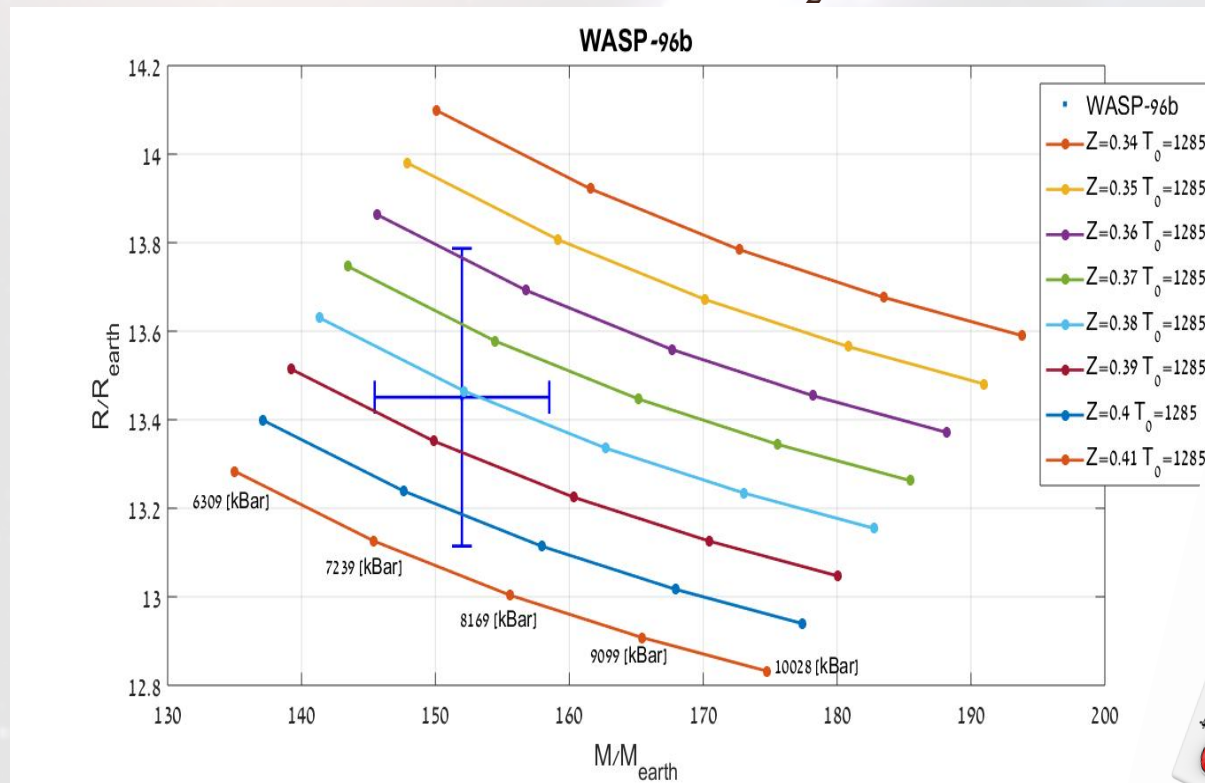
Efficiency of mixing depends on the primordial internal structure and on the assumed composition

# Adiabatic models

## The example of WASP-96b

1 bar temperature: of 1285 K  
Heavy elements - H<sub>2</sub>O

$$M_p = 0.48 \pm 0.03 M_J$$
$$R_p = 1.2 \pm 0.06 R_J$$
$$a = 0.0453 \pm 0.00128 \text{ AU}$$
$$M_{\star} = 1.06 \pm 0.09 M_{\odot}$$



Best fit  
composition:  
 $Z=0.38$   
A highly  
enriched giant  
planet!



# Adiabatic models

## The example of WASP-96b

$$M_p = 0.48 \pm 0.03 M_J$$

$$R_p = 1.2 \pm 0.06 R_J$$

$$a = 0.045 \pm 0.001 \text{ AU}$$

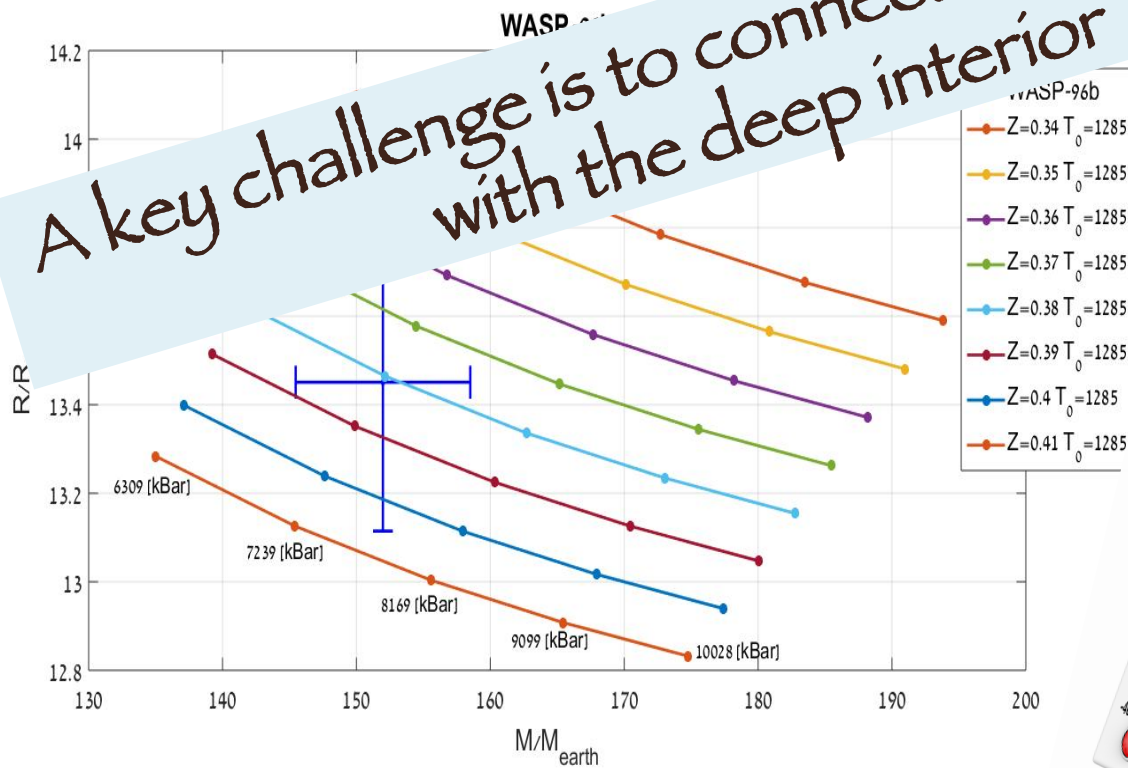
$$M_* = 0.8128 M_\odot$$

$$M_p = 0.48 M_\oplus$$

1 bar temperature: of 1285 K

Heavy elements -  $H_2O$

A key challenge is to connect the atmosphere with the deep interior



Best fit composition:  
 $Z=0.38$   
A highly enriched giant planet!

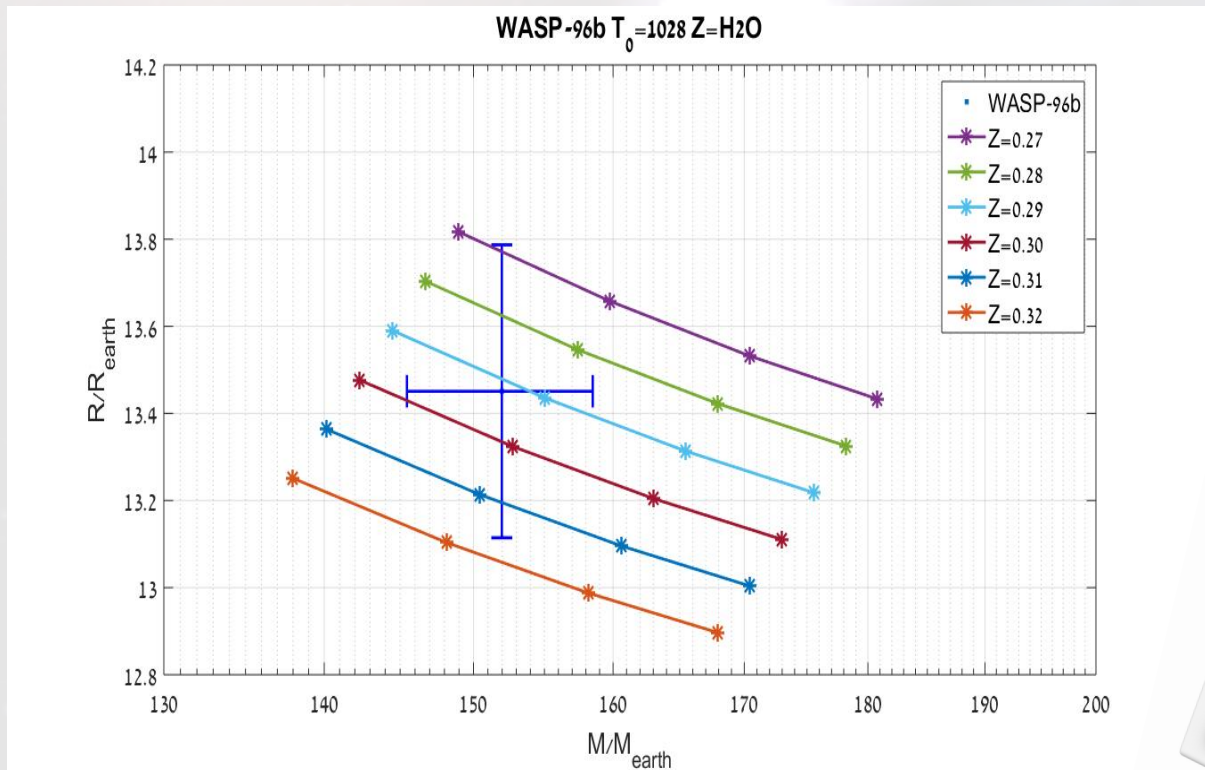


# Adiabatic models

## The example of WASP-96b

1 bar temperature is lowered by 20%  
Heavy elements - H<sub>2</sub>O

$$\begin{aligned}M_p &= 0.48 \pm 0.03 M_J \\ R_p &= 1.2 \pm 0.06 R_J \\ a &= 0.0453 \pm 0.00128 \text{ AU} \\ M_\star &= 1.06 \pm 0.09 M_\odot\end{aligned}$$



Best fit  
composition:  
**Z=0.29**  
Z decreases by  
~ 35%!



Lahav et al., in prep.

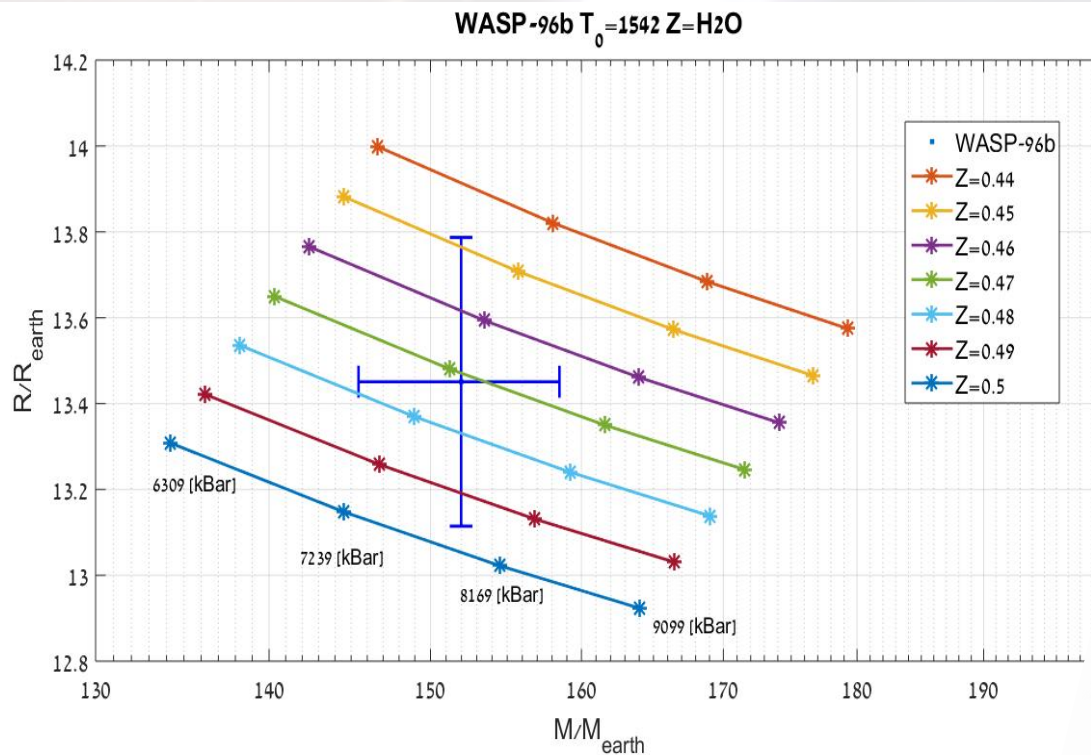


# Adiabatic models

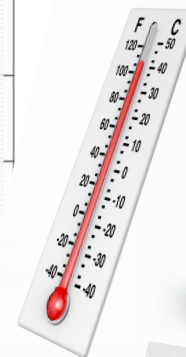
## The example of WASP-96b

1 bar temperature is increased by 20%  
Heavy elements - H<sub>2</sub>O

$$M_p = 0.48 \pm 0.03 M_J$$
$$R_p = 1.2 \pm 0.06 R_J$$
$$a = 0.0453 \pm 0.00128 \text{ AU}$$
$$M_\star = 1.06 \pm 0.09 M_\odot$$



Best fit  
composition:  
**Z=0.47**  
Z increases by  
~ 20%!



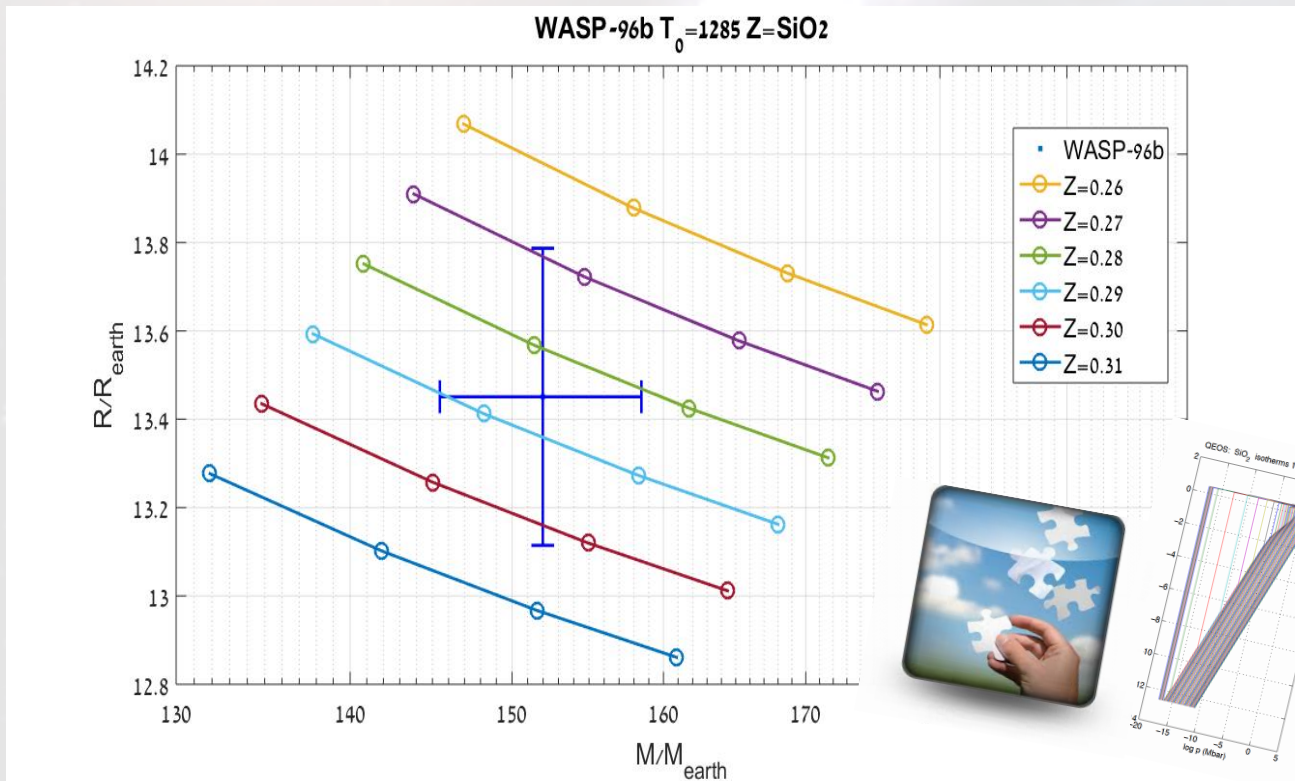
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# Adiabatic models

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$$\begin{aligned}M_p &= 0.48 \pm 0.03 M_J \\ R_p &= 1.2 \pm 0.06 R_J \\ a &= 0.0453 \pm 0.00128 \text{ AU} \\ M_\star &= 1.06 \pm 0.09 M_\odot\end{aligned}$$

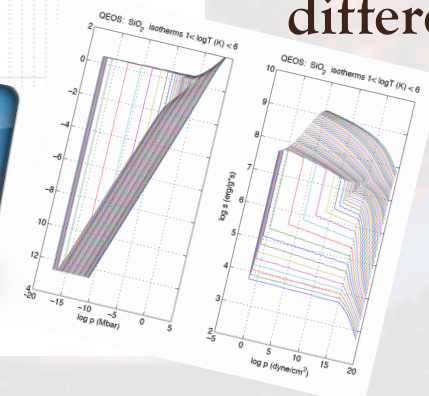
1 bar temperature: of 1285 K  
Heavy elements -  $\text{SiO}_2$



Best fit  
composition:

$$Z=0.295$$

More than 20%  
difference due to  
different EOS.



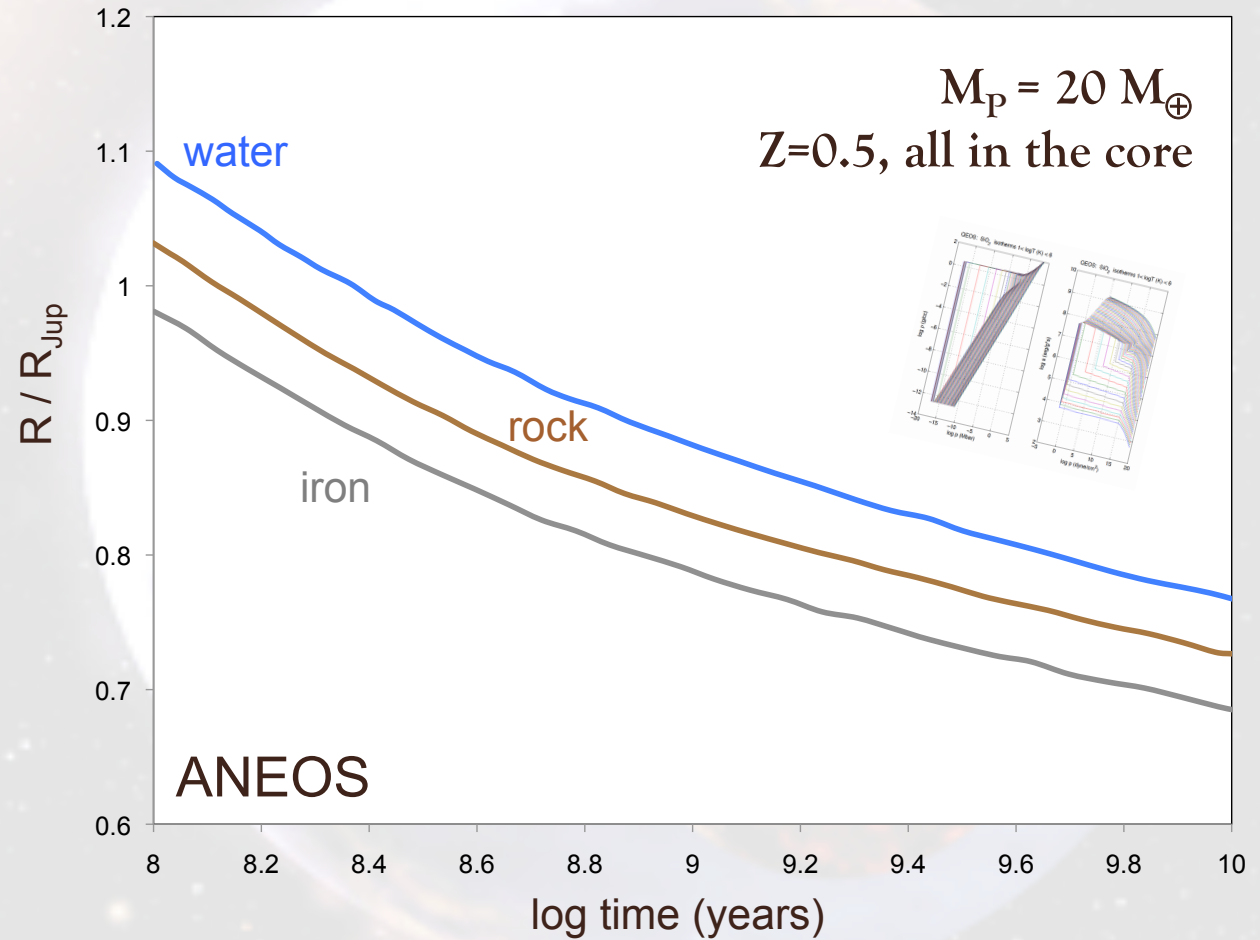
# The importance of the assumed composition (high-Z)



$$M_p = 20 M_{\oplus}$$
$$M_z = 10 M_{\oplus}$$

$\Delta \sim 10\%$   
uncertainty in R  
at a given age

## Intermediate-mass planets:



see Baraffe et al., 2008 for details

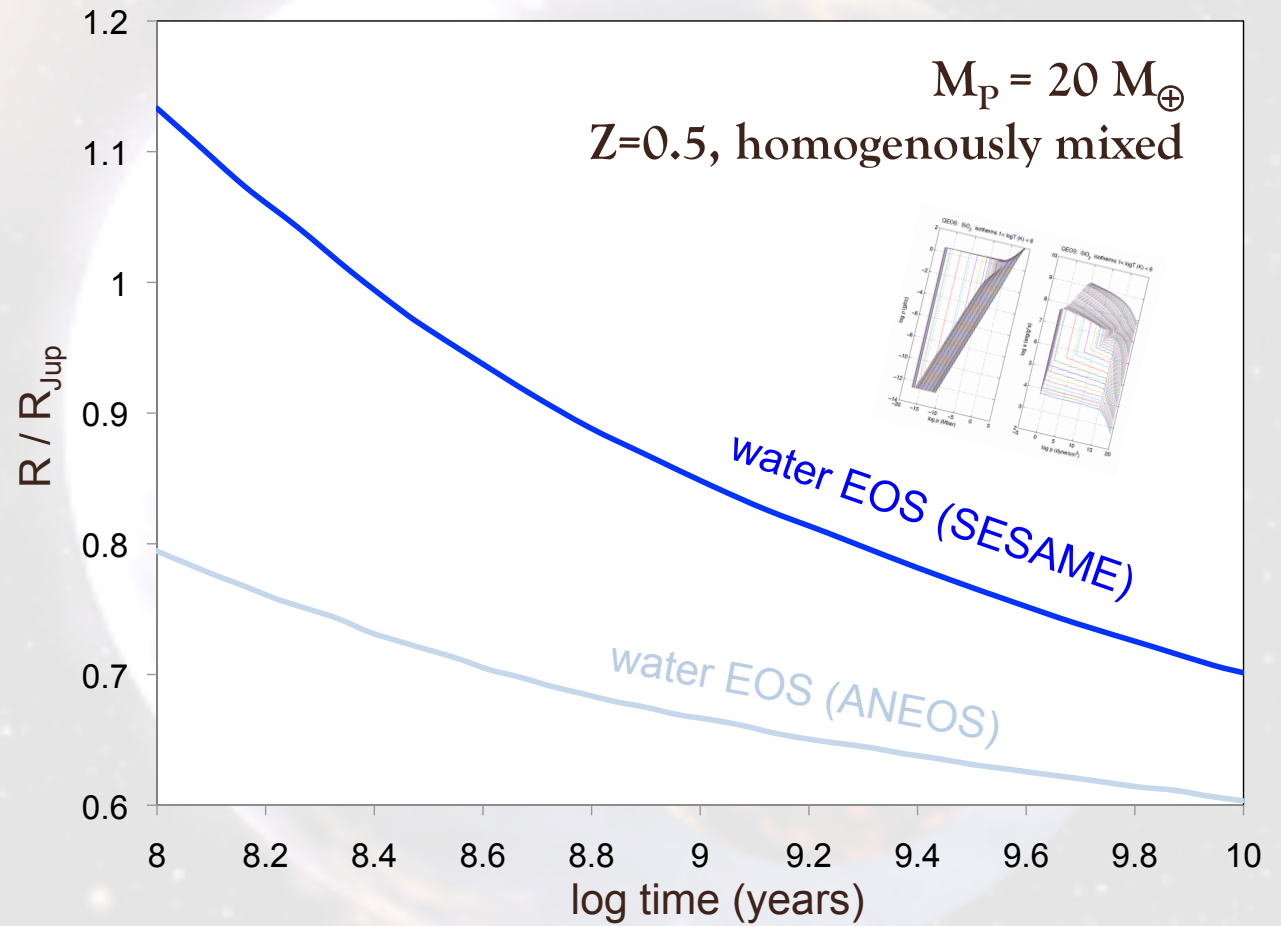
# The importance of the EOS (mixed model)



$$M_P = 20 M_{\oplus}$$
$$M_Z = 10 M_{\oplus}$$

$\Delta \sim 10\text{-}20\%$   
uncertainty in  $R$   
at a given age  
homogenous  
interior

## Intermediate-mass planets:



see Baraffe et al., 2008 for details

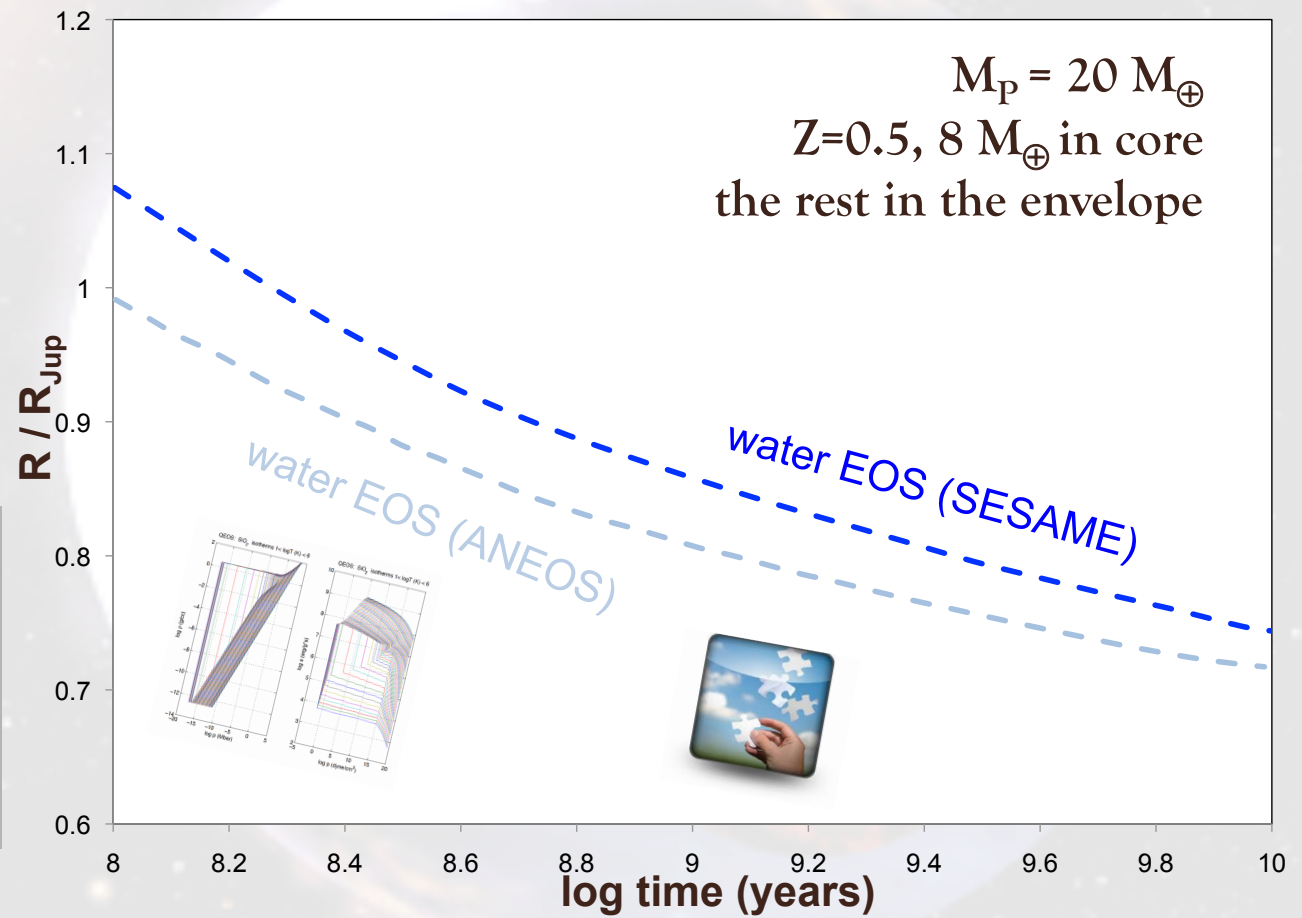
# The importance of the EOS (core+envelope)



## Intermediate-mass planets:

$$M_P = 20 M_{\oplus}$$
$$M_Z = 10 M_{\oplus}$$

$\Delta < \sim 10\%$   
uncertainty in  $R$  at  
a given age  
core + envelope



see Baraffe et al., 2008 for details

# The importance of the EOS (core+envelope)



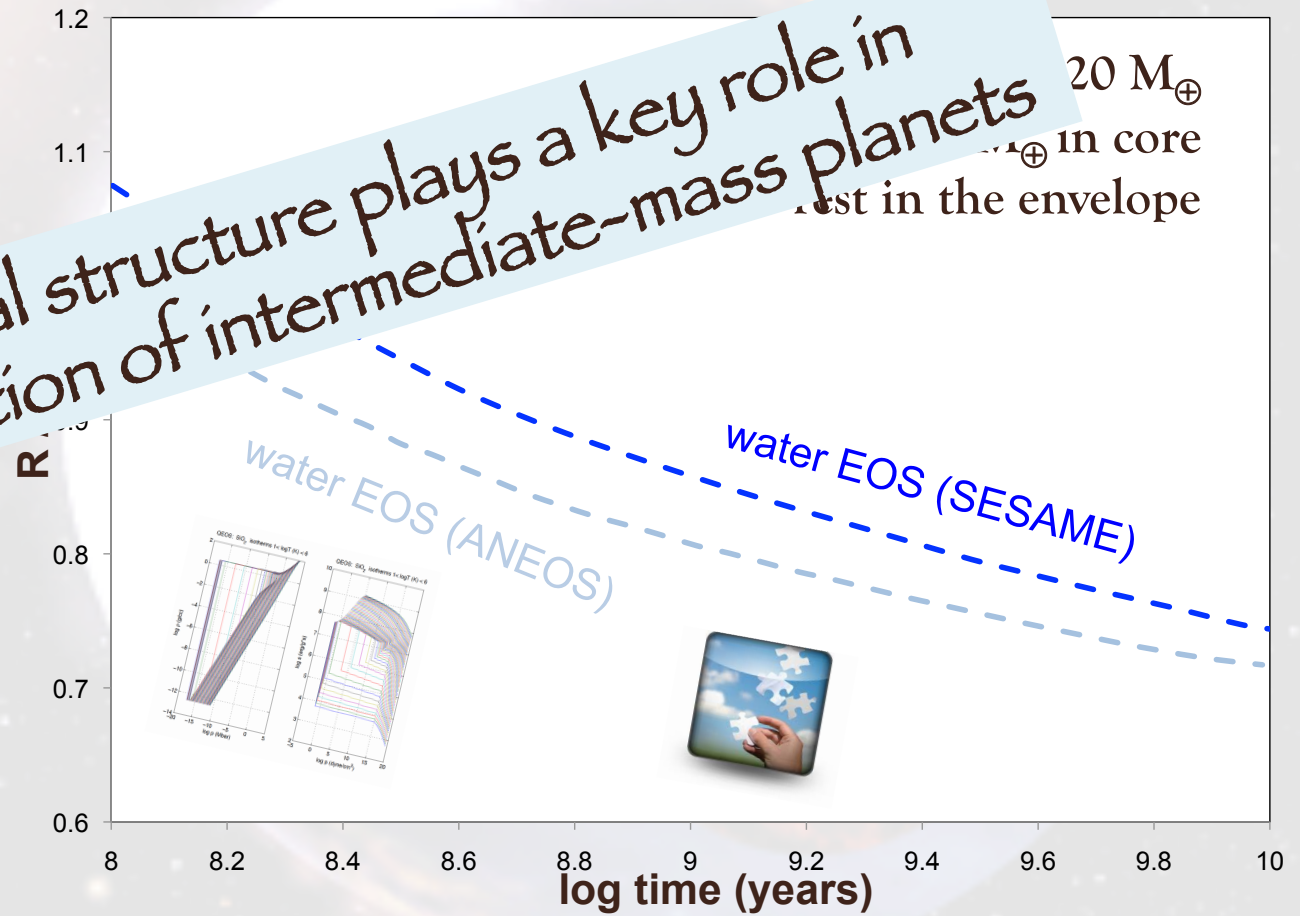
## Intermediate-mass planets:

$$M_P = 20 M_{\oplus}$$

$$M_Z = 10 M_{\oplus}$$

The internal structure plays a key role in the characterization of intermediate-mass planets

$\Delta R \sim 10\%$   
uncertainty in  $R$  at  
a given age  
core + envelope



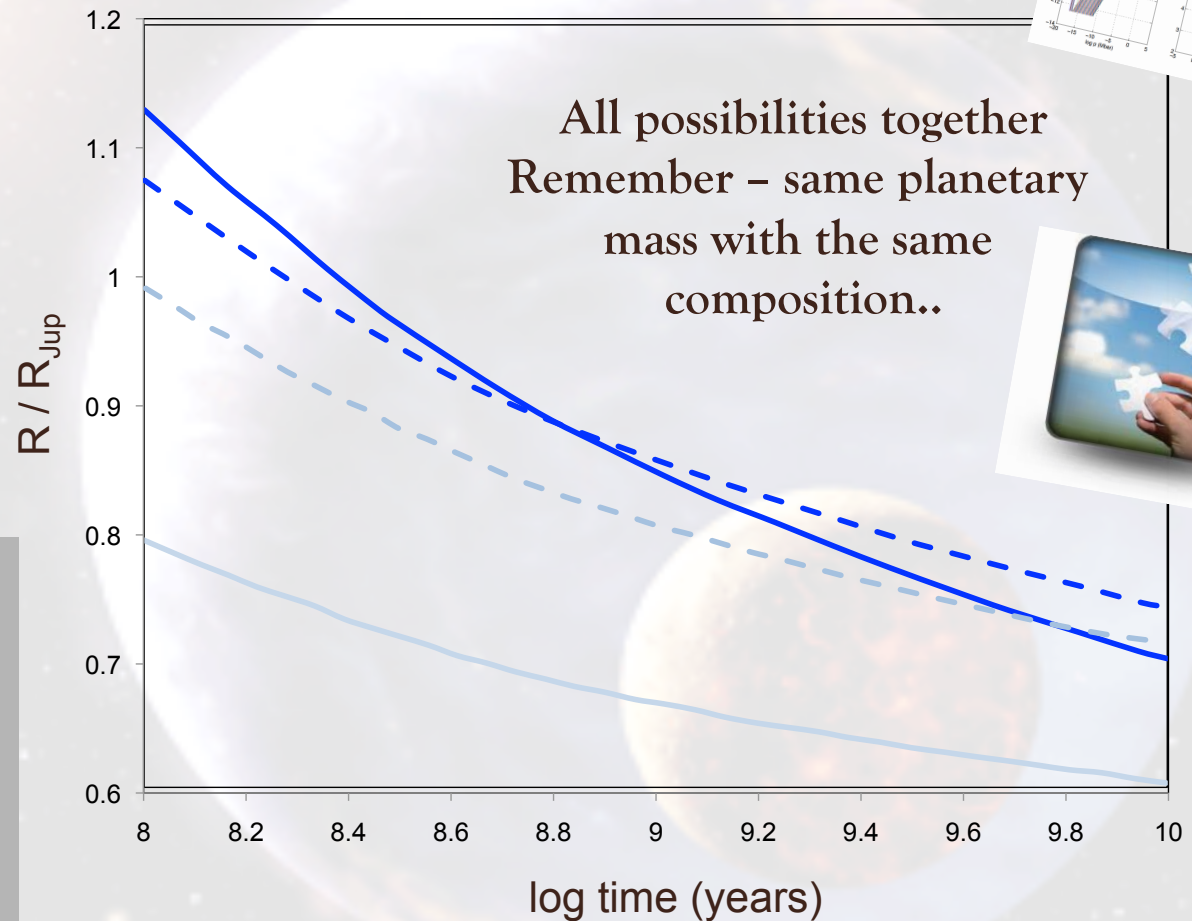
see Baraffe et al., 2008 for details

# The importance of assumed composition, distribution, EOS



$$M_p = 20 M_{\oplus}$$
$$M_z = 10 M_{\oplus}$$

## Intermediate-mass planets:



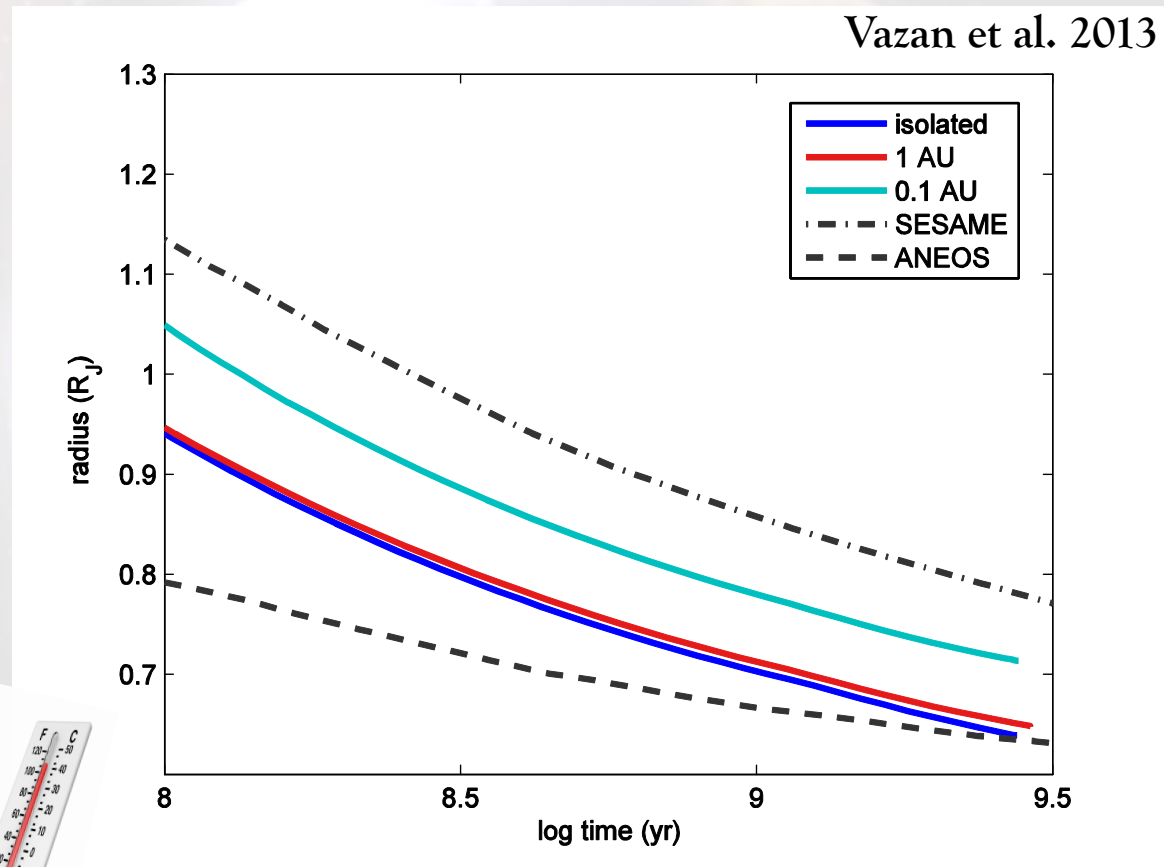
$\Delta > \sim 20\%$   
uncertainty in  
radius at a given  
age  
\*this is large\*

# The importance of radial distance

## Intermediate-mass planets:

$$M_p = 20 M_{\oplus}$$
$$Z=0.5 \text{ (mixed)}$$

EOS is very important for Neptune-mass ( $Z > 0.2$ ), especially for homogenous interiors

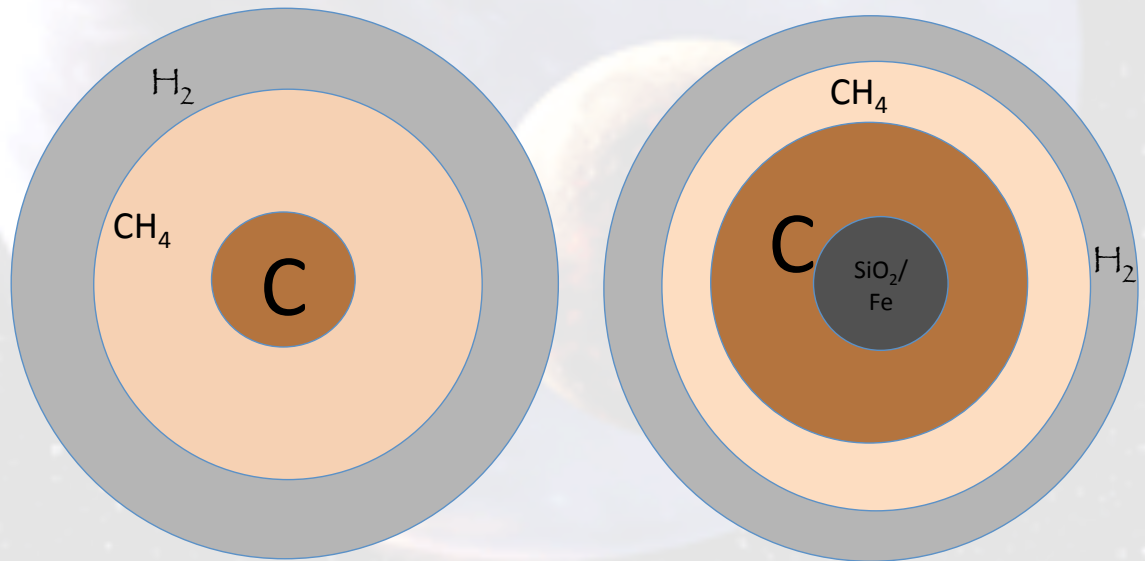




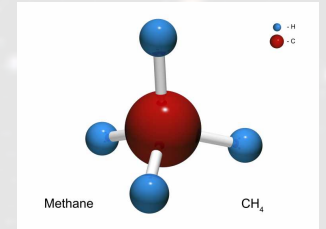
# A non-monotonic behavior of M-R due to dissociation (the example of CH<sub>4</sub> planets)

- Pure CH<sub>4</sub> planets:  
If  $P_c > P_{\text{diss}}$  carbon EOS (core). Dissociation of CH<sub>4</sub> produces  $1/3M_C$  of H which is assumed to form H<sub>2</sub>-atmosphere. The remaining mass is in a CH<sub>4</sub> shell.
- CH<sub>4</sub> planets + SiO<sub>2</sub>/Fe core:  
Innermost region is SiO<sub>2</sub>/Fe above the core, if  $P > P_{\text{diss}}$  carbon EOS, otherwise CH<sub>4</sub>. Mass of H-atmosphere is 1/3 the mass of the carbon shell.

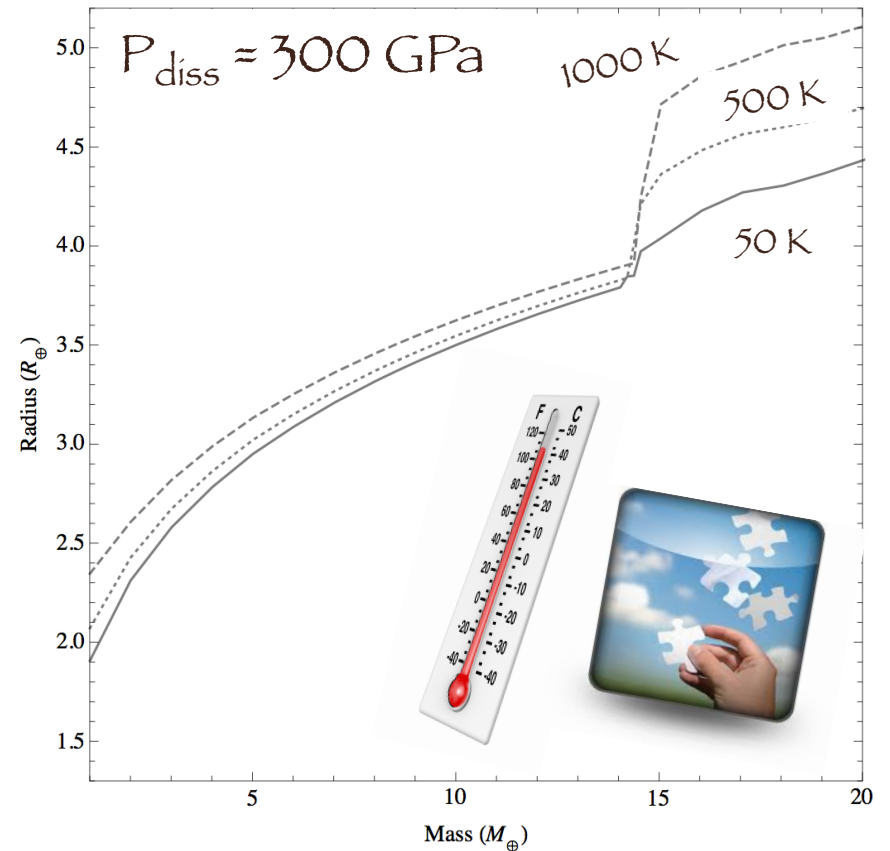
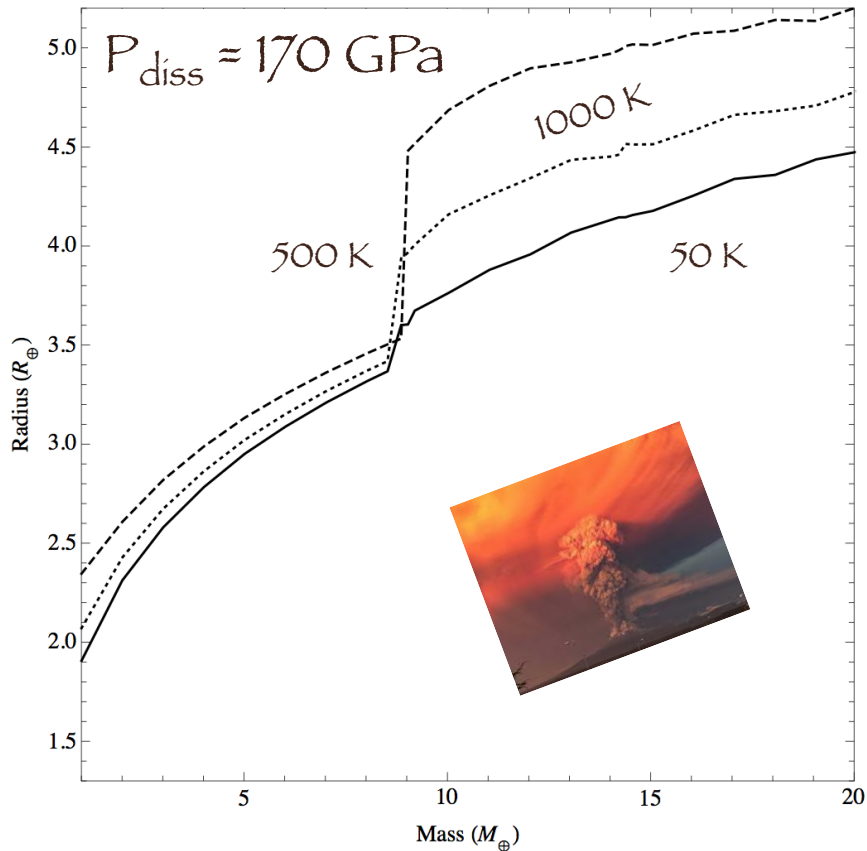
To be explored in detail:  
other materials;  
temperature profiles; photo-  
evaporation; differentiation,  
chemical interactions



# M-R relation: CH<sub>4</sub> planets

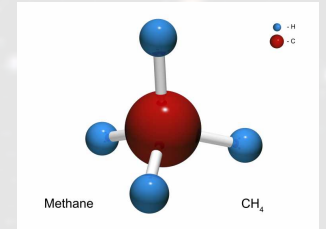


Helled et al., 2015

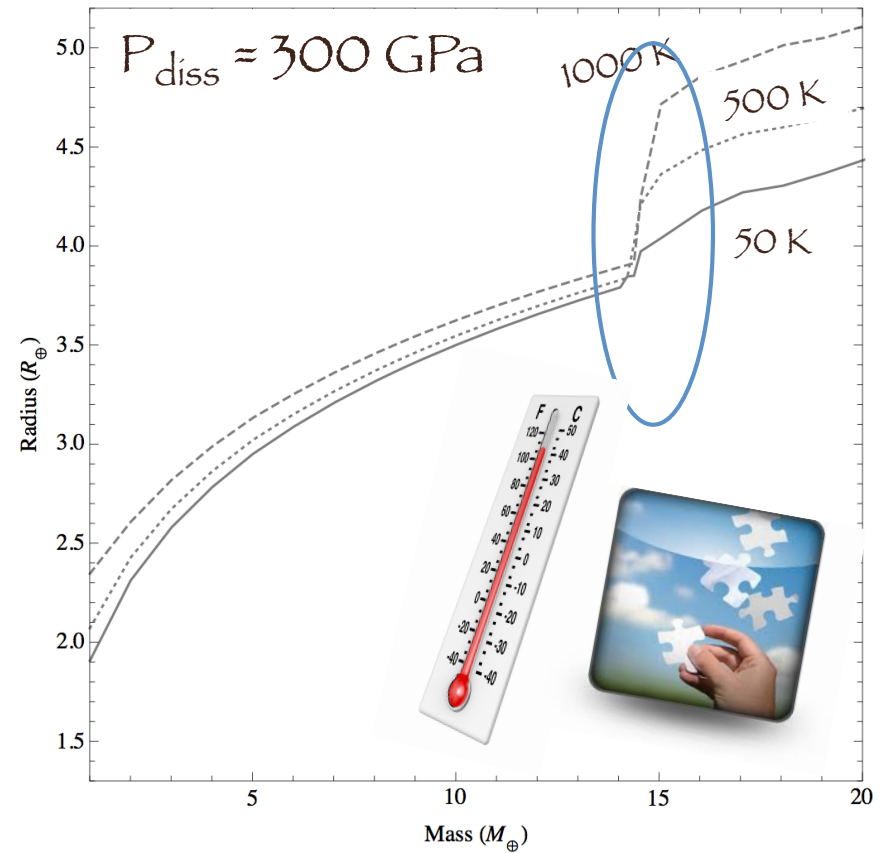
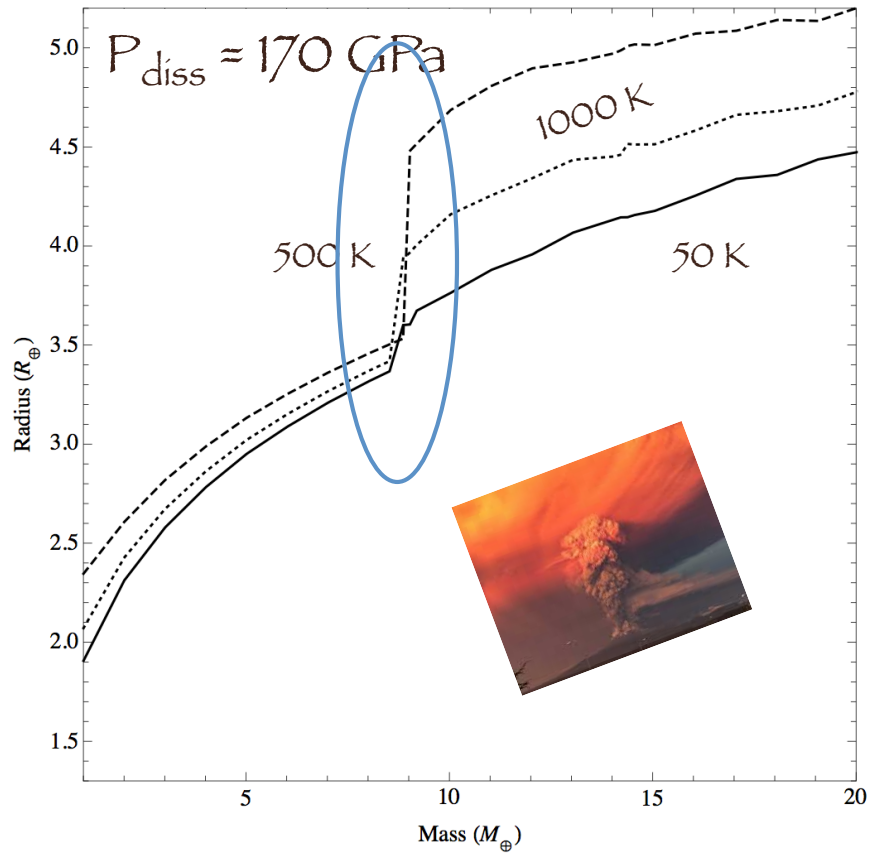


At high enough mass (depending on  $P_{\text{diss}}$ ) CH<sub>4</sub> dissociates → a jump in M-R relation

# M-R relation: CH<sub>4</sub> planets



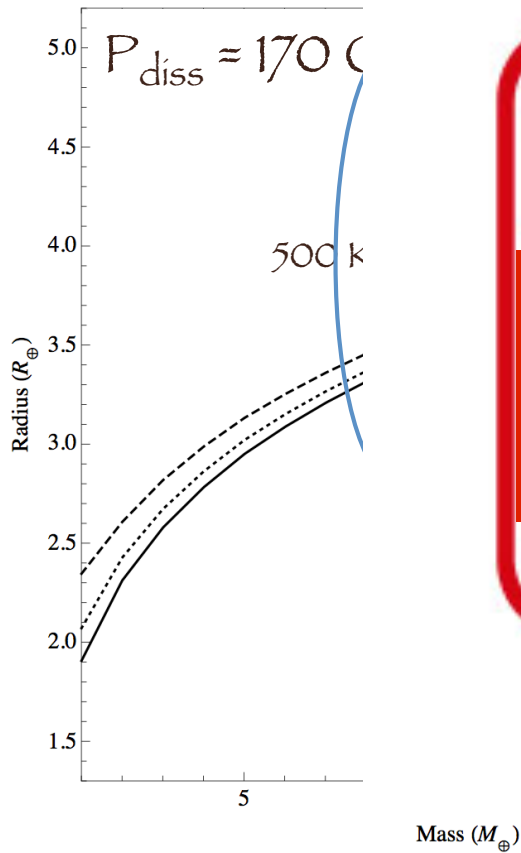
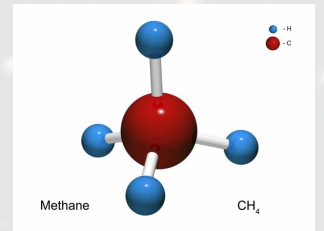
Helled et al., 2015



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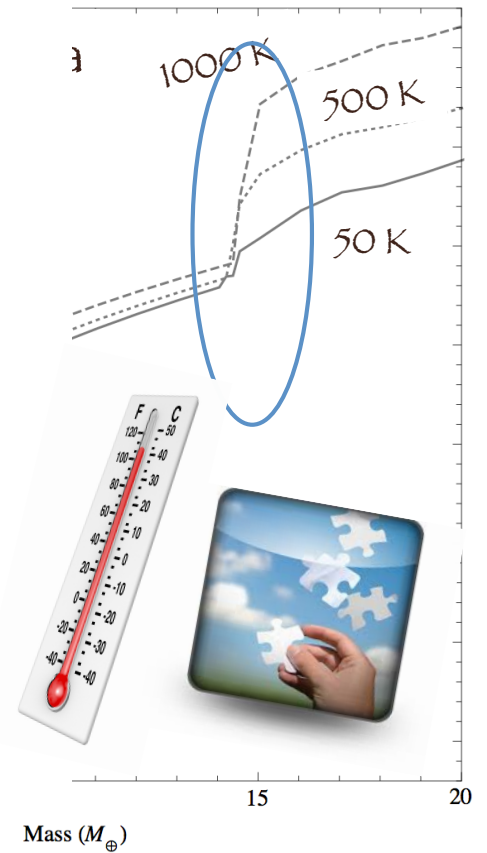
M.D. 1.1

Helled et al., 2011



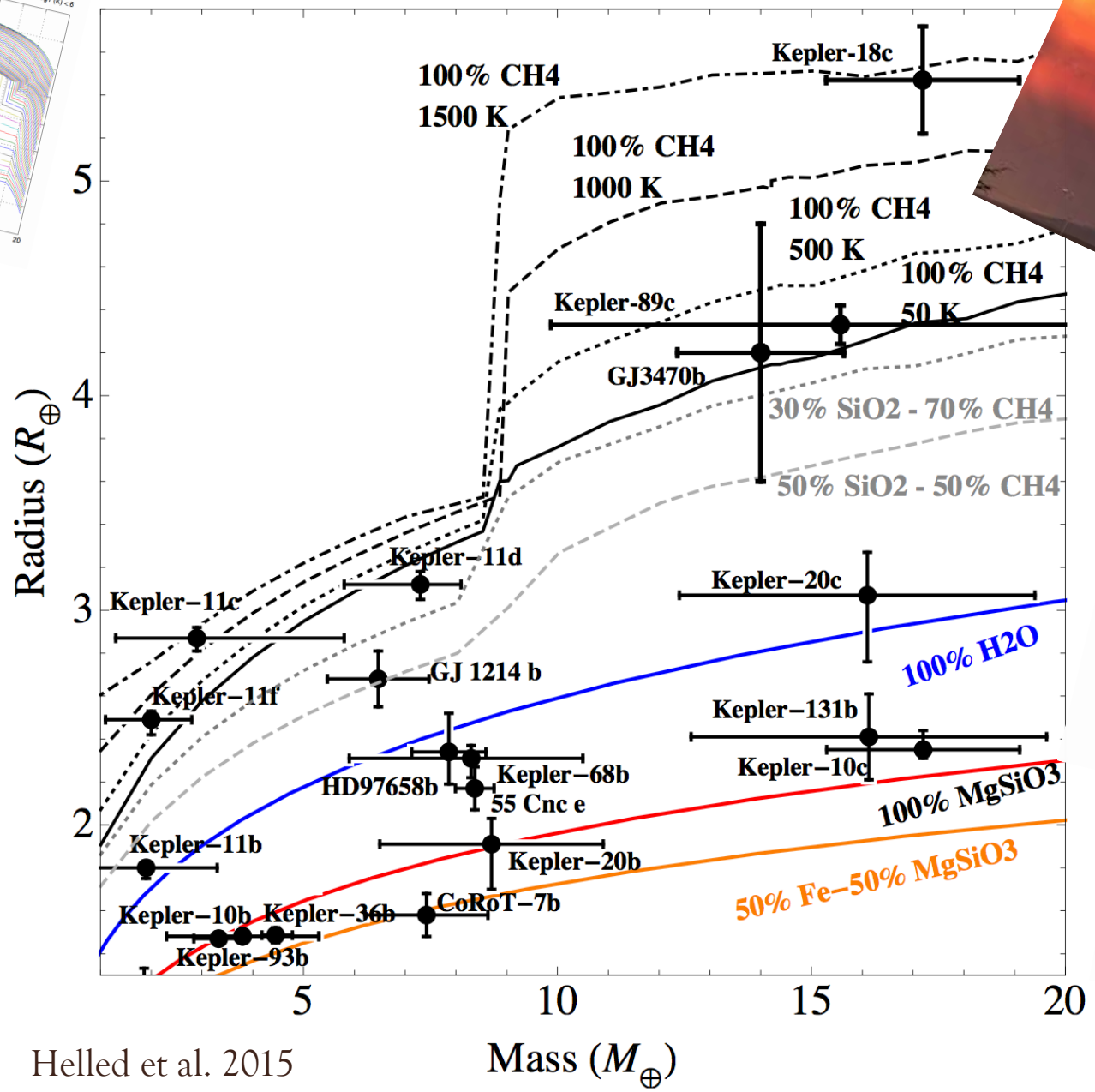
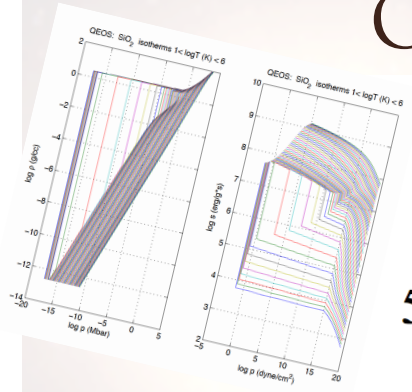
**ATTENTION**

As long as the planet is undifferentiated R is insensitive to temperature. When the planet is massive enough to produce H<sub>2</sub> atmosphere, R increases and the temperature becomes crucial.

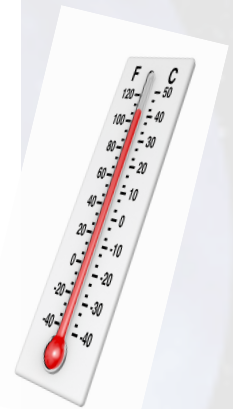


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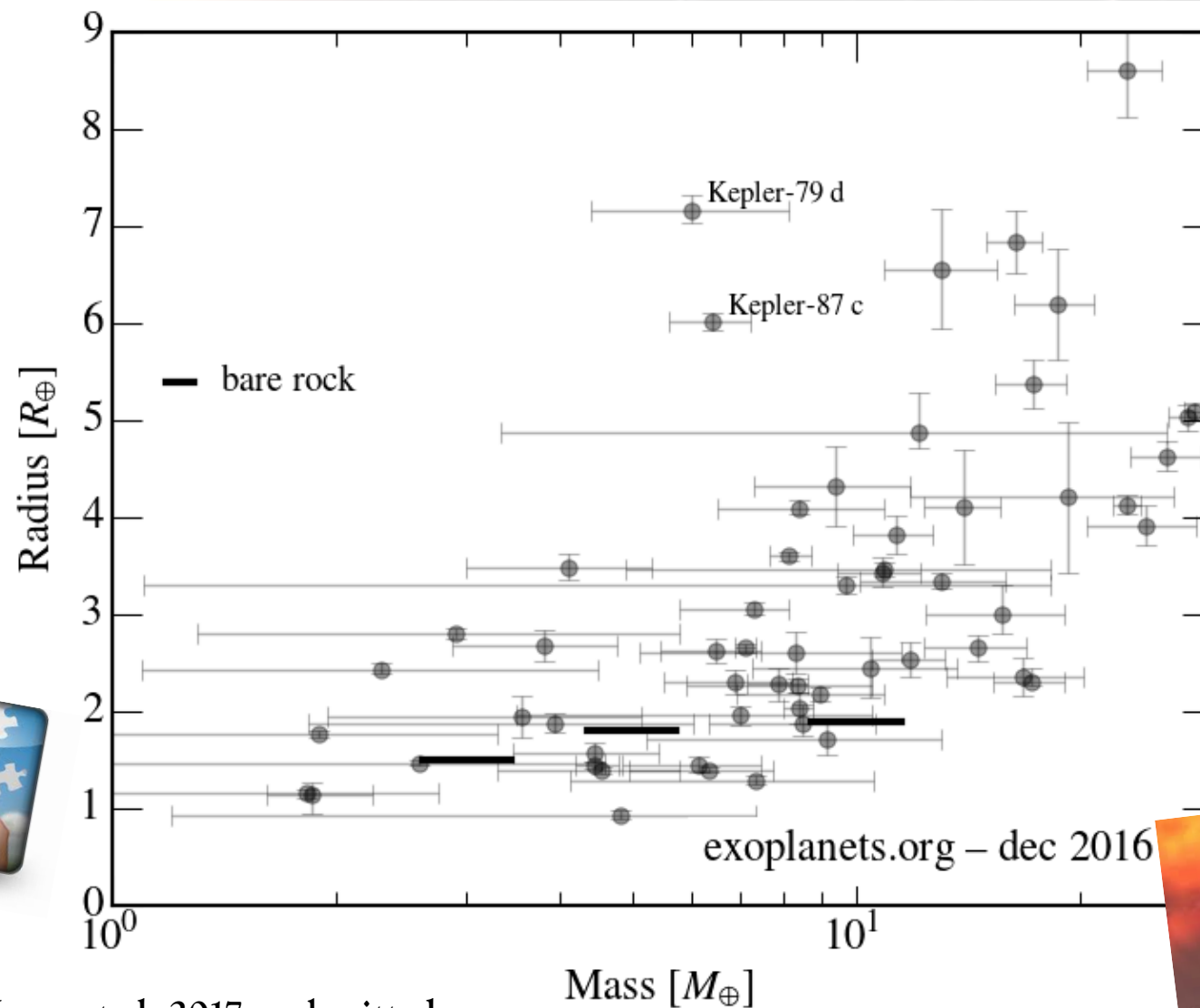
# CH<sub>4</sub> planets & detected exoplanets



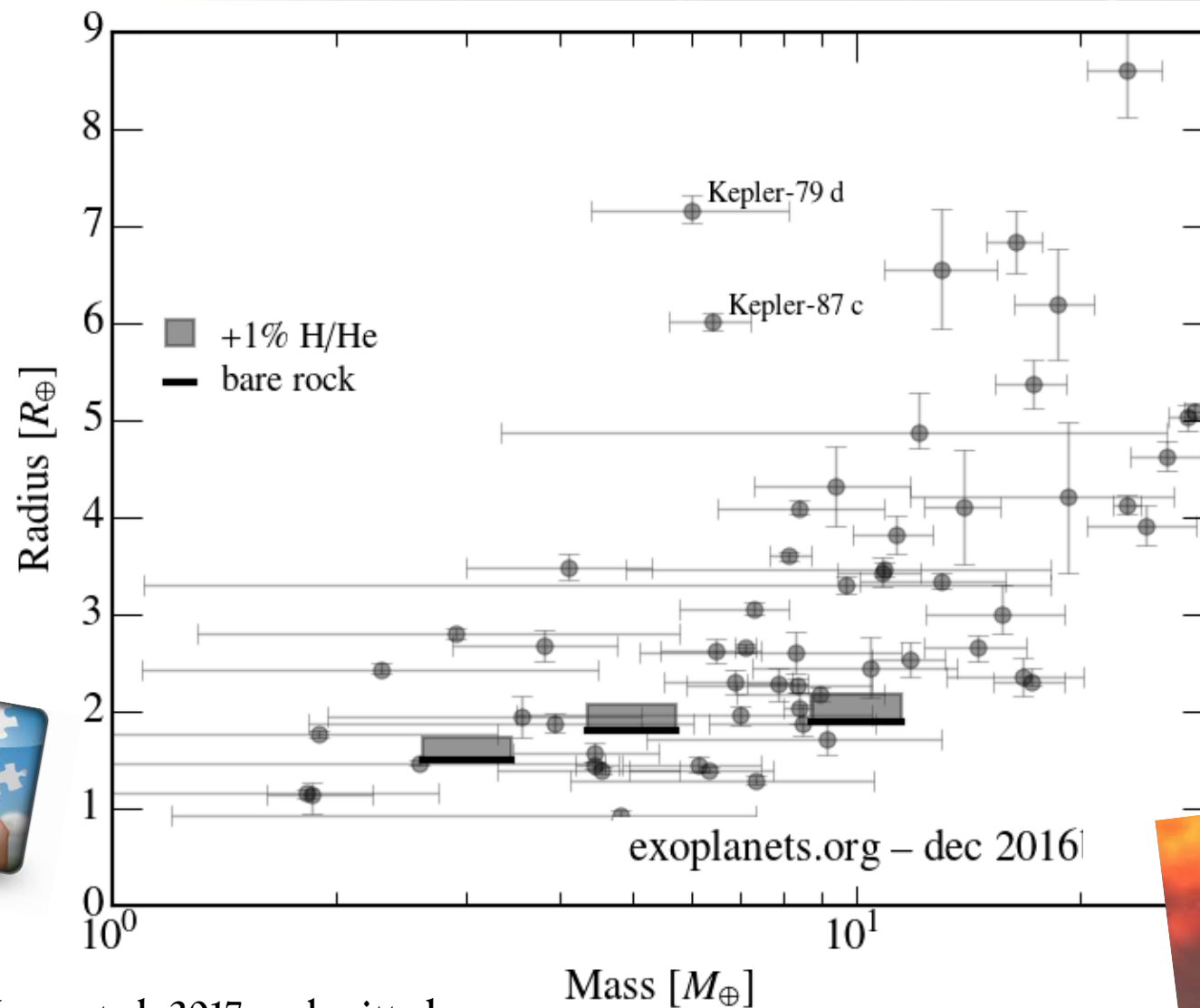
Helled et al. 2015



# The importance of thermal effects & existence of an atmosphere on the M-R relation



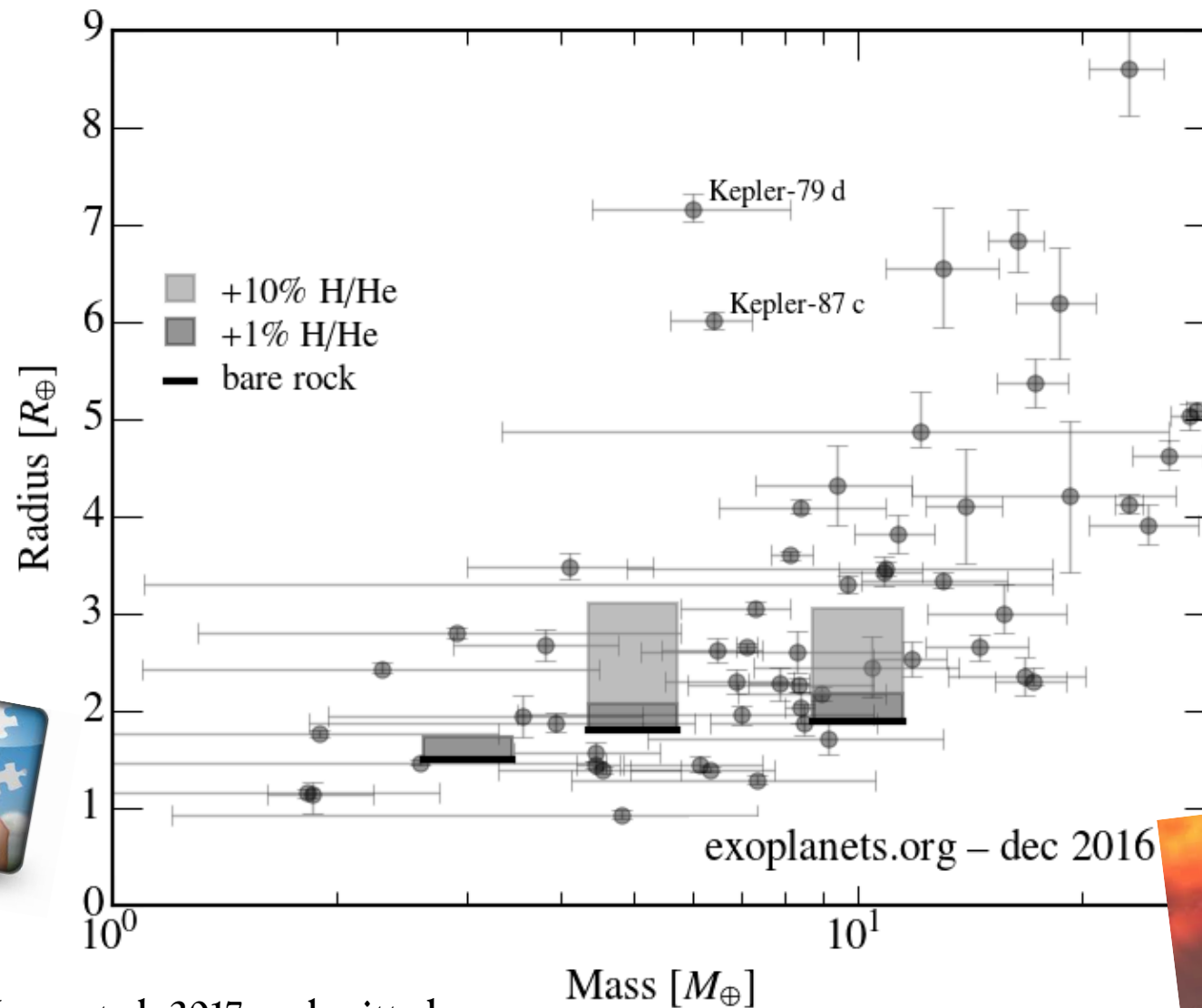
# The importance of thermal effects & existence of an atmosphere on the M-R relation



Vazan et al. 2017 - submitted



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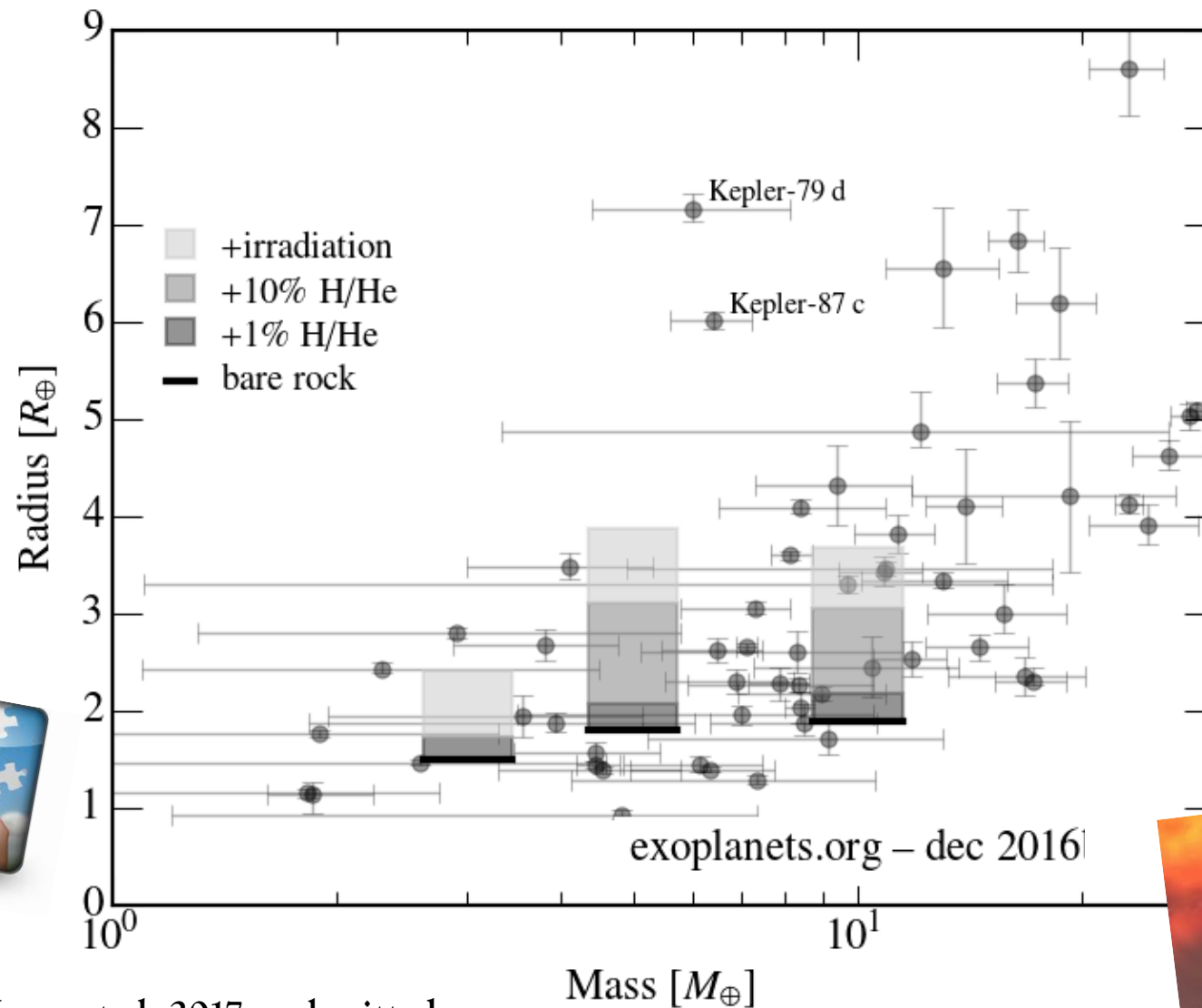


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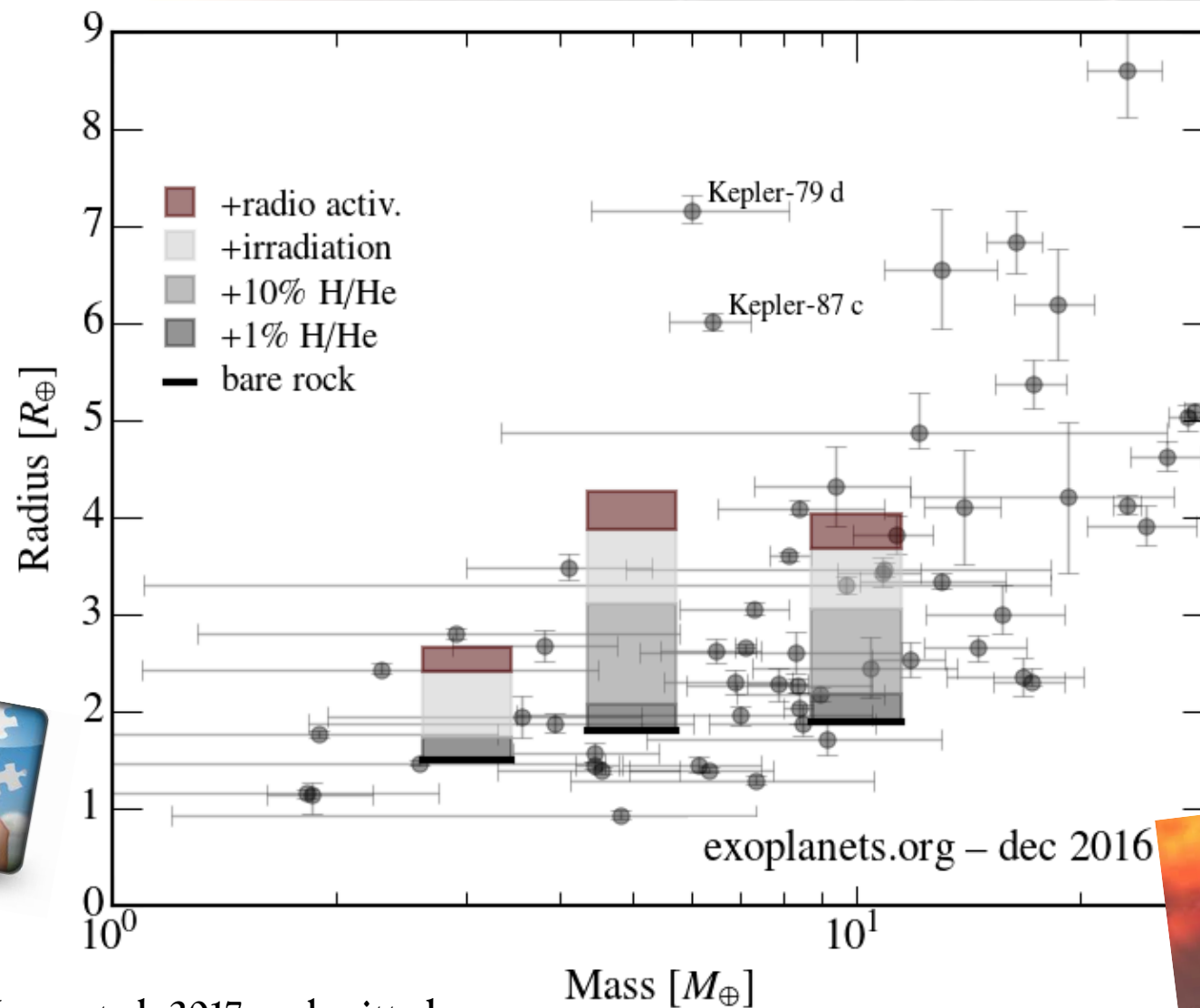
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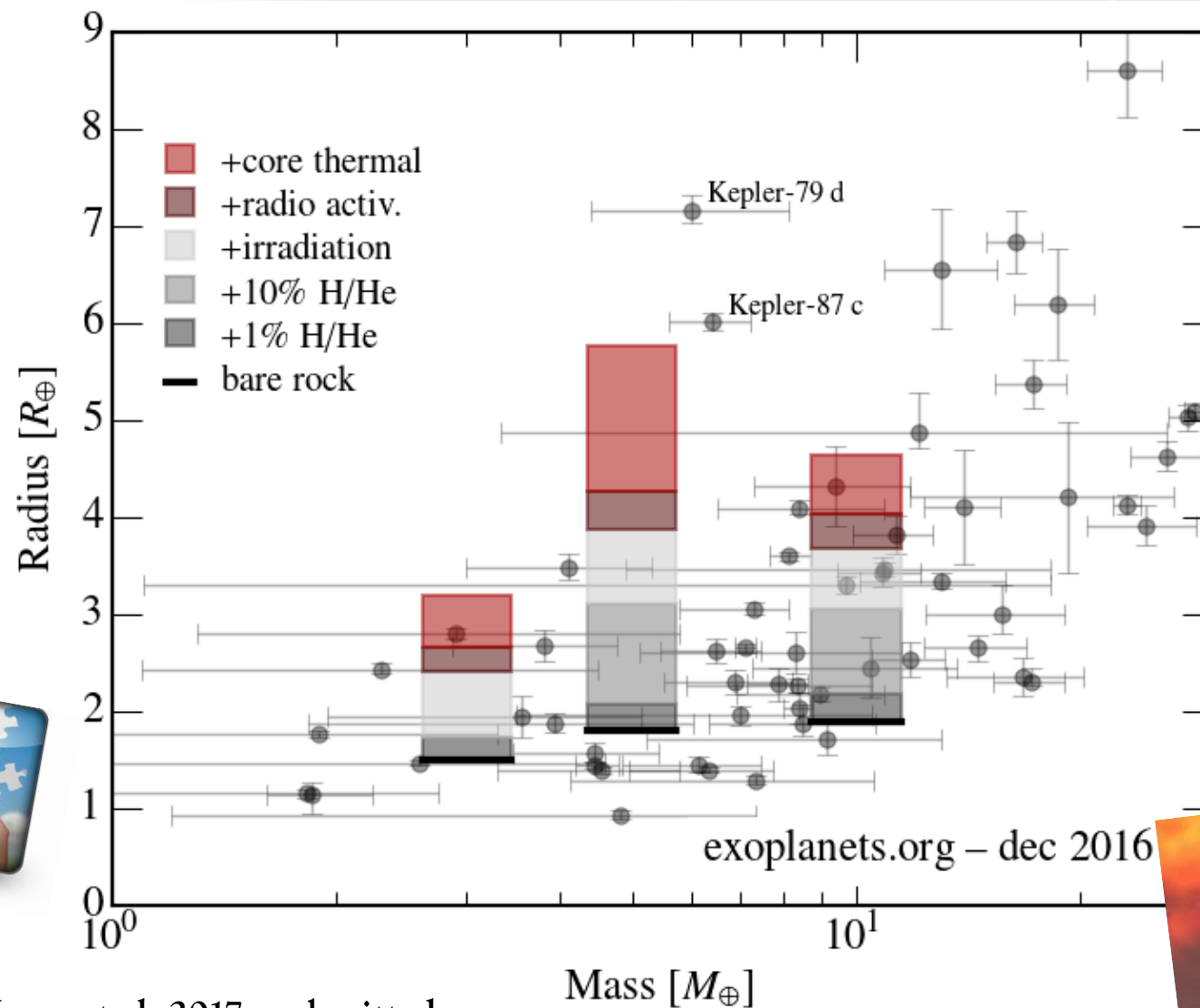
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# Conclusions & future work

- The M-R relation depends on assumed composition, EOS & distribution of heavy elements, age, temperature, opacity, irradiation.
- Intermediate-mass planets (with volatiles) are more sensitive to the EOS and the materials' distribution.
- The M-R relation can be complex including a non-monotonic behavior. Geophysical processes: mixing, outgassing, atmospheric loss, etc.

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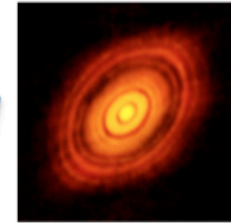
## Future work:

- Identify theoretical uncertainty on M-R relation → a crucial piece for data interpretation (TESS, CHEOPS, PLATO 2.0).
- Connect atmospheric measurements with deep interior.

# Thank you



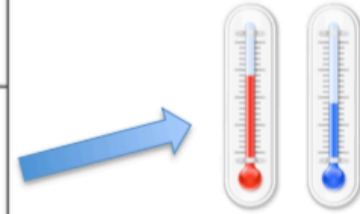
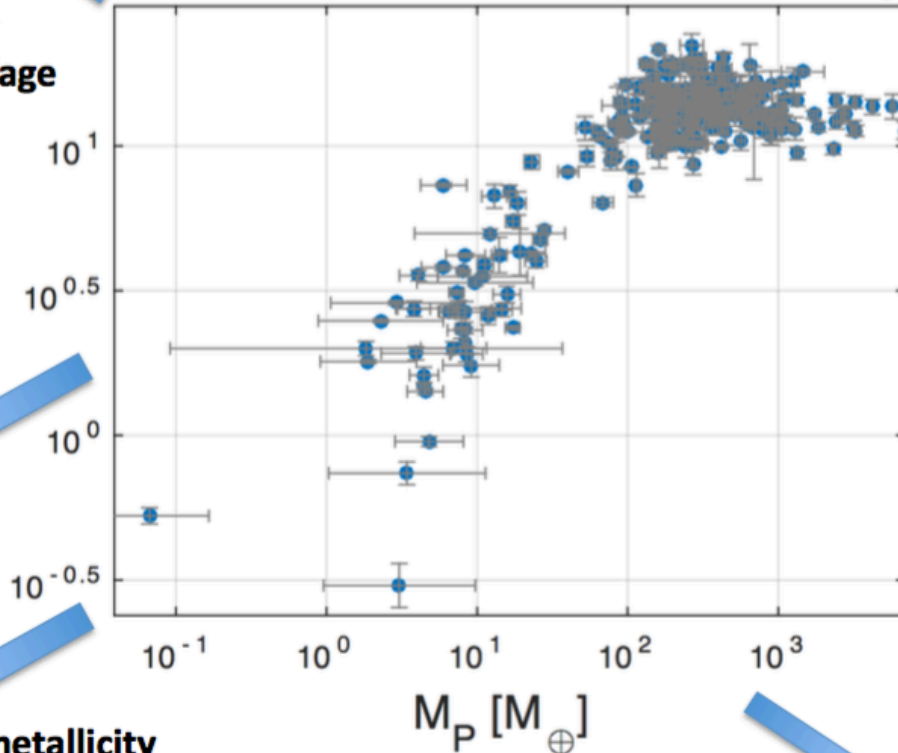
Time/age



Disk properties and formation history

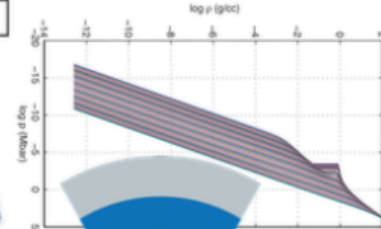
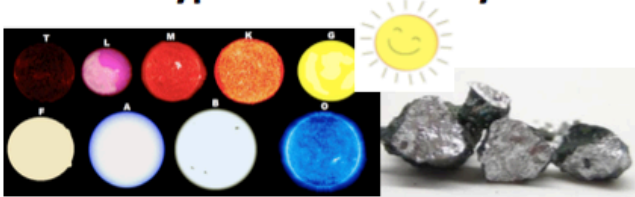
Other parameters?

$R_p [R_\oplus]$



Temperature and radial distance

Stellar type and metallicity



Equation of state (EOS) & assumed internal structure