Icarus

A satellite orbit drift in binary near-Earth asteroids (66391) 1999 KW4 and (88710) 2001 SL9 - Indication of the BYORP effect
--Manuscript Draft--

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Abstract:

We obtained thorough photometric observations of two binary near-Earth asteroids (66391) Moshup = 1999 KW4 and (88710) 2001 SL9 taken from 2000 to 2019.

We modeled the data and derived physical and dynamical properties of the binary systems. For (66391) 1999 KW4, we derived its mutual orbit's pole, semimajor axis

and eccentricity that are in agreement with radar-derived values (Ostro et al. [2006]. Science, 314, 1276–1280). However, we found that the data are inconsistent with a

constant orbital period and we obtained unique solution with a quadratic drift of the mean anomaly of the satellite of -0.65 ± 0.16 deg/yr ^{2} (all quoted uncertainties

correspond to 3σ). This means that the semimajor axis of the mutual orbit of the components of this binary system, determined a = 2.548 ± 0.015 km by Ostro et al.

(2006), increases in time with a mean rate of 1.2 ± 0.3 cm/yr.
For (88710) 2001 SL9, we determined that the mutual orbit has a pole within 10° of (L, B) = (302°, -73°) (ecliptic coordinates), and is close to circular (eccentricity

< 0.07). The data for this system are also inconsistent with a constant orbital period and we obtained two solutions for the quadratic drift of the mean anomaly: 2.8 ± 0:2

and 5.2 ± 0:2 deg/yr ^{2} , implying that the semimajor axis of the mutual orbit of the components (estimated a ~ 1.6 km) decreases in time with a mean rate of -2.8 ± 0.2

or -5.1 ± 0.2 cm/yr for the two solutions, respectively.
The expanding orbit of (66391) 1999 KW4 may be explained by mutual tides interplaying with binary YORP (BYORP) effect (McMahon, J., Scheeres, D. [2010].

Icarus 209, 494-509). However, a modeling of the BYORP drift using radar-derived shapes of the binary components predicted a much higher value of the orbital drift

than the observed one. It suggests that either the radar-derived shape model of the secondary is inadequate for computing the BYORP effect, or the present theory

of BYORP overestimates it. It is possible that the BYORP coefficient has instead an opposite sign than predicted; in that case, the system may be moving into an

equilibrium between the BYORP and the tides.
In the case of (88710) 2001 SL9, the BYORP effect is the only known physical mechanism that can cause the inward drift of its mutual orbit.
Together with the binary (175706) 1996 FG3 which has a mean anomaly drift consistent with zero, implying a stable equilibrium between the BYORP effect and

	mutual body tides (Scheirich et al. [2015]. Icarus 245, 56-63), we now have three distinct cases of well observed binary asteroid systems with their long-term dynamical models inferred. They indicate a presence of all the three states of the mutual orbit evolution – equilibrium, expanding and contracting – in the population of near-Earth binary asteroids.
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Response to Reviewers:	

Dear editor,

We are submitting the revision of the manuscript of paper A satellite orbit drift in binary near-Earth asteroids (66391) 1999 KW4 and (88710) 2001 SL9 — Indication of the BYORP effect for publication in your journal Icarus.

We apologise for it took so long, but we hope that the reviewers will find the changes acceptable and we are looking forward for your response.

Sincerely,

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We are grateful to the reviewers for their constructive and useful comments that led us to improve the paper in several points. We respond to specific comments raised by the reviewers in following.

Reviewer #1: This is an interesting article discussing detailed characterisation of two binary asteroid systems, (66391) 1999 KW4 and (88710) 2001 SL9, based on a long-term photometric campaign. The authors detect a drift in orbital elements of mutual orbits in both systems and explore possible explanations, including BYORP as possible mechanism affecting the mutual orbits. This is a well-rounded sudy with with sound methodology, and can be recommended for publication. I will focus on the observational aspect of the work, and I only have minor comments.

p. 8: I would like to know what step sizes were selected for the mean anomaly drift search.

A: The steps in ΔM_d were 0.005 deg/yr2 and 0.01 deg/yr2 for 1999 KW4 and 2001 SL9, respectively. We added this information to the paper.

p.9: The last couple sentences of the first paragraph are confusing. I assume that the range of investigated pericenter drifts reflect the values that would be possible assuming realistic parameters of the system, but the wording might need adjusted.

A: This assumption is correct; we modified the wording accordingly.

In the paragraph describing the RMS for the fit of SL9 models the solutions with higher RMS are rejected as they "do not appear real". Is this only because of the higher RMS? I would suggest making this clearer or including any potential additional reasons for the claim.

A: See our response to a similar comment by the second reviewer.

Figure 3: Is the period used to plot the dashed-line model optimised assuming zero mean anomaly drift, or is it the same period as for the best-fit solution with non-zero anomaly drift (i.e. period at the model epoch)?

A: The former is the case. The dashed-line shows the model with the mean anomaly drift fixed at 0, but all other parameters fitted, including the orbital period. We amended the caption of the figure to emphasize this.

Figures 4 and 8: I think those figures are slightly misleading. Which orbital period was used to plot the points? The orbital period at model epoch for the best-fit solutions which also include a non-zero mean anomaly drift, or the orbital period corresponding to the solution assuming zero mean anomaly drift in in figures 1 and 2? If the former applies, I think the captions to the figures and text on page 9 need adjusting to make it clearer.

A: We edited the text on page 9 and the figures captions to make it clearer.

p. 11: Reference to Warner et al. 2009 is included, but the bibliography data is missing in the References section.

A: We added the reference to the section.

p. 12 The radar results were used to derive the diameters ot the components, and the size ratio obtained for KW4 is compared with the results of the radar study (Ostro et al. 2006). Could the radar shape model of the primary along with the size-corrected radar model of secondary be also used to verify the mean anomaly drift?

A: A synthetic primary lightcurve computed from the radar shape model, assuming a uniform surface light scattering, does not fit the observed primary lightcurve well. (We note that we have found similar discrepancies between synthetic lightcurves computed from primary radar shape models and observed lightcurves for other binary NEAs as well. It appears that either the radar shape models are not precise enough, or the primary's surfaces don't have uniform light scattering.) So using the primary shape model would make the fit worse instead of verifying it. And the radar shape model of the secondary, besides its underestimated size, is even affected by much larger errors due to low SNR, as is noted before the end of the Section 3 of the paper.

p. 13 It is unclear what the "actual light scattering model" is.

A: We used a combination of Lommel-Seeliger and Lambert scattering, as stated in the beginning of the Section 2.2. We modified the text on p. 13 (now page 15) accordingly.

p. 14 I would suggest including the paremeters derived by Pravec et al. (2006) to illustrate the agreement with presented results.

A: We include the parameters from Pravec et al. (2006) to the text.

p. 17 Please clarify if "perturbing the vertices vertically" refers to perturbations along surface normals, radially, or along another direction.

A: The perturbations were radial, we edited the text to clarify that.

p. 19 Are the ellipsoid models developed for the two components insufficient for BYORP calculations? The opening of section 5.2 is confusing, as section 4 discusses possible near-spherical shape for the secondary.

A: The BYORP effect requires the secondary body to be of irregular shape (see Cuk and Burns, 2005), the ellipsoidal approximation is therefore insufficient in this case. We modified the opening of the section 5.2 to clarify that.

Appendix A: The NIR spectroscopy of KW4 is discussed here. However I feel some additional information is needed. What was the time span of spectral observations? Also, the authors obtain 37 spectra, yet only one is analysed, is this a sum of the 37? Figure 14 could benefit from including illustration of mean spectra of Q (and maybe O) type to support the discussion.

A: We added the time span (5:30-7:55 UTC) to the text and clarify that the analysed spectrum is an average of all obtained spectra. We also added mean Q and O spectra

2

to Fig. 14.

Reviewer #2: I recommend that this paper be revised substantially. This submission claims to have detected the quadratic drift of the mean anomaly of a binary asteroid mutual orbit in time for two systems. This is a significant achievement, however the evidence as presented is problematic. In particular, the submission does not adequately demonstrate with a statistical test that the claimed best fit solutions are significant despite the claim of significance on page 9. For Moshup 1991 KW4, the best fit solution as shown in Figure 3 is visually convincing particularly compared to the non-drifting mean anomaly case. However, for 2001 SL9, the data as shown in Figure 7 is far from convincing and, visually, all three shown cases look like they fit the data equally well. In order to be convinced, the authors need to not just calculate the value of a goodness-of-fit measure but describe the uncertainty of such a measure. Currently, the authors use the RMS magnitude residuals as a goodness-of-fit measure, but they do not report the statistics of this measure, so it is unclear as to whether a 0.0015 mag difference is significant; just comparing that number to the uncertainties of a given measurement or average of measurements would be something. A better solution would be to conduct either a Pearson chi-squared test or a G-test between the observations and the model so that the likelihood of the difference between two models being due to chance could be directly evaluated and significance assessed. The values and uncertainties of each measurement would be used to determine the goodness-of-fit for each choice of model orbit parameters and then the chi-squared or G-test metric would follow a chi square distribution and a p-value could be assessed, which will inform if the difference is statistically likely.

A: The differences between the observed and simulated data in the binary asteroid photometry are dominated by systematic effects – mainly due to the model simplifications. It results in that the fit residuals of nearby points are correlated. The statistical tests assume that the residuals are random and normally distributed, which is not justified here. To overcome the problem, so that we can use the chi-square test, we adopted a strategy described in new section 2.3.

We also enlarged the number of presented lightcurve sessions (Figs. 9 and 10 in the revised version) in order to emphasize the differences between the synthetic curve of the model with ΔM_d fixed at 0 and the observed data. We also point out that the differences are systematic in the sense that the synthetic curve for $\Delta M_d = 0$ is shifted in time with respect to the observed data and that this shift is different for each observed apparition. Moreover, these shifts evolve in time so that they are consistent with the quadratic drift of the mean anomaly, as shown in Fig. 11.

In the abstract, it may be helpful to provide the semi-major axis in km to give context to the mean rate of change of the semi-major axis or to calculate the semi-major axis doubling/halving timescale. Instead of using "internal" consider using "mutual" to describe the dynamics of the binary components about their shared center of mass as opposed to their joint motion around the Sun.

A: We added the semi-major axes in km to the abstract.

We modified the wording to "mutual two-body dynamics" in the Introduction.

The values used in the calculations in Section 5.1 appear to be different than the values in Table 4. Why is this? Wouldn't it be best to introduce a single set of nominal parameters and use those parameters for all calculations except for when one is explicitly varying them?

A: We updated the semimajor axis to agree with the value in Table 4 and explained in the footnote 3, why R_{mean} doesn't agree with $D_{2,V}$ from Table 4.

Given the claimed best fit semi-major axis drift and estimates of all the other binary asteroid parameters for 1991 KW4, it seems appropriate for the paper to provide an estimate of the BYORP coefficient if tides were insignificant, if Q/k is consistent with the Taylor & Margot (2010), and if Q/k is consistent with the Schierich et al. (2015) estimate.

A: We added these estimates to the end of Section 5.1.

It's important to note that the Taylor & Margot (2010) estimate of Q/k is of a lower bound because they assume a maximum tidal evolution timescale – this should be made clear in the text. It's also important to note that the Q/k estimate from Schierich et al. (2015) is good for the 1996 FG3 system but theory suggests that it should scale with size. Goldreich and Sari (2009) hypothesize that k goes as R for rubble piles, Jacobson & Scheeres (2011) fit binary systems to find that Q/k goes as 1/R and hypothesized that k went as 1/R, but, lastly, Nimmo and Matsuyama (2019) explain why Q should go as R^2 so that when k goes as R as Goldreich & Sari (2009) surmised, Q/k goes as 1/R as Jacobson & Scheeres (2011) discovered. Thus, it's important to scale the Q/k value regarding 1996 FG3 in Schierich et al. (2015) to the binaries at hand.

A: We noted that Q/k from Taylor & Margot (2010) is a lower bound in the text and replaced equalities with inequalities on corresponding derived values.

The works cited indicate that Q/k goes as R, not as 1/R. We assume that that was a typo in reviewer's comments. We therefore scaled the Q/k estimate from Scheirich et al. to KW4 and SL9 accordingly and updated the text and values.

Highlights

- Orbital vectors of two binary near-Earth asteroid were determined.

- An orbit of the satellite of (66391) Moshup is expanding in time.

- An orbit of the satellite of (88710) 2001 SL9 is shrinking in time.

- The evolution of the orbits due to emission of thermal radiation (BYORP effect).

A satellite orbit drift in binary near-Earth asteroids (66391) 1999 KW4 and (88710) 2001 SL9 — Indication of the BYORP effect

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Abstract

We obtained thorough photometric observations of two binary near-Earth aster-oids (66391) Moshup = 1999 KW4 and (88710) 2001 SL9 taken from 2000 to 2019. We modeled the data and derived physical and dynamical properties of the binary systems. For (66391) 1999 KW4, we derived its mutual orbit's pole, semimajor axis and eccentricity that are in agreement with radar-derived values (Ostro et al. [2006]. Science, 314, 1276–1280). However, we found that the data are inconsistent with a constant orbital period and we obtained unique solution with a quadratic drift of the mean anomaly of the satellite of -0.65 ± 0.16 deg/yr^2 (all quoted uncertainties correspond to 3σ). This means that the semimajor axis of the mutual orbit of the components of this binary system, determined $a = 2.548 \pm 0.015$ km by Ostro et al. (2006), increases in time with a mean rate of 1.2 ± 0.3 cm/yr.

For (88710) 2001 SL9, we determined that the mutual orbit has a pole within $10°$ of $(L, B) = (302°, -73°)$ (ecliptic coordinates), and is close to circular (eccentricity < 0.07). The data for this system are also inconsistent with a constant orbital period and we obtained two solutions for the quadratic drift of the mean anomaly: 2.8 ± 0.2 and 5.2 ± 0.2 deg/yr^2, implying that the semimajor axis of the mutual orbit of the components (estimated $a \sim 1.6$ km) decreases in time with a mean rate of -2.8 ± 0.2 or -5.1 ± 0.2 cm/yr for the two solutions, respectively.

The expanding orbit of (66391) 1999 KW4 may be explained by mutual tides interplaying with binary YORP (BYORP) effect (McMahon, J., Scheeres, D. [2010]. Icarus 209, 494-509). However, a modeling of the BYORP drift using radar-derived shapes of the binary components predicted a much higher value of the orbital drift than the observed one. It suggests that either the radar-derived shape model of the secondary is inadequate for computing the BYORP effect, or the present theory of BYORP overestimates it. It is possible that the BYORP coefficient has instead an opposite sign than predicted; in that case, the system may be moving into an equilibrium between the BYORP and the tides.

In the case of (88710) 2001 SL9, the BYORP effect is the only known physical mechanism that can cause the inward drift of its mutual orbit.

Together with the binary (175706) 1996 FG3 which has a mean anomaly drift consistent with zero, implying a stable equilibrium between the BYORP effect and mutual body tides (Scheirich et al. [2015]. Icarus 245, 56-63), we now have three distinct cases of well observed binary asteroid systems with their long-term dynam-ical models inferred. They indicate a presence of all the three states of the mutual orbit evolution – equilibrium, expanding and contracting – in the population of near-Earth binary asteroids.

Key words: Asteroids, dynamics; Near-Earth objects; Photometry

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1 Introduction

Binary asteroids exhibit interesting mutual two-body dynamics driven by thermal emission from irregularly shaped components, but up to now there has appeared only one study constraining its limits based on direct measurements so far: Scheirich et al. (2015) found an upper limit on drift of the mutual orbit of the components of binary near-Earth asteroid (175706) 1996 FG3, that is consistent with the theory of Jacobson and Scheeres (2011) of that synchronous binary asteroids are in a state of stable equilibrium between binary YORP (BYORP) effect [1] and mutual body tides. In this paper, we present a comprehensive analysis of mutual orbit drifts in two well-observed binary near-Earth asteroids (NEAs).

The NEA (66391) Moshup = 1999 KW4 was discovered by Lincoln Near-Earth Asteroid Research in Socorro, New Mexico, on 1999 May 20. Its binary nature was revealed by Benner et al. (2001). We obtained thorough photometric observations for it in six apparitions from 2000 to 2019. Since the asteroid was named only recently and its original designation 1999 KW4 is well-known to the asteroid science community, we use it throughout this paper.

The NEA (88710) 2001 SL9 was discovered by Near-Earth Asteroid Tracking at Palomar on 2001 September 18. Its binary nature was revealed by Pravec et al. (2001). We obtained thorough photometric observations for it in five apparitions from 2001 to 2015.

Among binary NEAs observed so far, our photometric datasets for these three systems (together with 1996 FG3) are the longest coverages obtained, providing a unique opportunity to study evolution of the mutual orbits of components of small binary asteroids.

The structure of this paper is as follows. In Section ??, we present a model of the mutual orbit of the components of 1999 KW4 and 2001 SL9 constructed from our complete photometric datasets. Then in Sections ?? and ??, we summarize our results with already known parameters of the two binaries. In Section ??, we then discuss implications of the observed characteristics, especially on the BYORP theory, from the derived drifts of the mutual orbits.

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[1] The BYORP effect is a secular change of the mutual orbit of the components of a binary asteroid due to the emission of thermal radiation from asymmetric shapes of the components. It was first theoretically proposed by Ćuk and Burns (2005).

2 Mutual orbit models of 1999 KW4 and 2001 SL9

2.1 Observational data

Table 1
Observations of (66391) 1999 KW4

Time span	No. of nights	Telescope	References
2000-06-19.0 to 2000-06-29.0	5	0.65-m Ondřejov	P06
2001-06-03.2 to 2001-06-20.9	7	0.41-m River Oaks	P06
	4	0.65-m Ondřejov	P06
2016-06-07.9 to 2016-06-22.3	6	0.65-m Ondřejov	This work
	6	0.5-m Sugarloaf Mountain	This work
2017-06-01.8 to 2017-06-27.0	8	0.65-m Ondřejov	This work
	6	0.5-m Sugarloaf Mountain	This work
2018-06-05.9 to 2018-06-18.9	9	0.65-m Ondřejov	This work
2019-05-31.1 to 2019-06-09.2	6	1.8-m Spacewatch II	This work
	6	0.65-m Ondřejov	This work
	5	0.5-m Sonoita	This work
	3	0.5-m Sugarloaf Mountain	This work
	3	0.5-m Shed of Science South	This work

Reference: P06 (Pravec et al., 2006)

Table 2
Observations of (88710) 2001 SL9

Time span	No. of nights	Telescope	References
2001-10-10.9 to 2001-10-21.3	7	0.65-m Ondřejov	P06
	2	0.5-m Palmer Divide	P06
2012-09-11.9 to 2012-11-15.4	4	1.54-m La Silla	This work
	4	1.5-m Maidanak	This work
2013-10-12.0 to 2013-12-05.1	7	1.54-m La Silla	This work
	2	0.7-m Abastumani	This work
	1	1.0-m Simeiz	This work
2014-10-18.0 to 2014-10-26.1	4	1.54-m La Silla	This work
2015-07-09.2 to 2015-08-17.3	6	1.8-m Lowell	This work
	3	2.2-m U. Hawaii	This work

Reference: P06 (Pravec et al., 2006)

The data used in our analysis, obtained during six and five apparitions for 1999 KW4 and 2001 SL9, respectively, are summarized in Tables **??** and **??**. The references and descriptions of observational procedures of the individual observatories are summarized in Table **??**.

The data were reduced using the standard technique described in Pravec et al.

Table 3
Observational stations

Telescope	Observatory	References for observational and reduction procedures
2.2-m U. Hawaii	Mauna Kea, Hawaii	1
1.8-m Lowell	Lowell Observatory, Arizona	2
1.8-m Spacewatch II	Spacewatch, Arizona	M07, L20
1.54-m La Silla	La Silla, European Southern Observatory, Chile	P14
1.5-m Maidanak	Maidanak Astronomical Observatory, Uzbekistan	P19
1.0-m Simeiz	Simeiz, Crimea	3
0.7-m Abastumani	Abastumani, Georgia	K16, P19
0.65-m Ondřejov	Ondřejov, Czech Republic	P06
0.5-m Sugarloaf Mountain	Sugarloaf Mountain Observatory, Massachusetts	V17
0.5-m Sonoita	Sonoita Research Observatory, Arizona	C15
0.5-m Palmer Divide	Palmer Divide Observatory, Colorado	P06
0.5-m Shed of Science South	Shed of Science South Observatory, Texas	4
0.41-m River Oaks	River Oaks Observatory, Texas	P06

References: 1: The observations were made in the Cousins R filter. Standard procedure of image reduction included dark removal and flatfield correction. 2: The observations were reduced using the same procedure as the observations from the 1.54-m La Silla, see Pravec et al. (2014) for details. 3: The observations were carried with a 1-m Ritchey-Chrétien telescope at Simeiz Department of the Crimean Astrophysical Observatory using camera FLI PL09000. The observations were made in the Johnson-Cousins photometric system. Standard procedure of image reduction included dark removal and flatfield correction. The aperture photometry was done with the AstPhot package described in Mottola et al. (1995). The differential lightcurves were calculated with respect to an ensemble of comparison stars by the method described in Erikson et al. (2000) and Krugly (2004). 4: The Shed of Science South utilizes a 0.5m Corrected Dall Kirkham telescope operating at a focal ratio of f4.5 and a pixel scale of 1.24 arc seconds per pixel using an SBIG ST10XME. Flat, dark, and bias images were applied using MaximDL and photometry was done using MPO Canopus. All images were unfiltered. C15 (Cooney et al., 2015), K16 (Krugly et al., 2016), L20 (Larsen, J. A., et al. 2020. In preparation.), M07 (McMillan et al., 2007), P06 (Pravec et al., 2006), P14 (Pravec et al., 2014), P19 (Pravec et al., 2019), V17 (Vokrouhlický et al., 2017).

(2006). By fitting a two-period Fourier series to data points outside mutual (occultation or eclipse) events, the rotational lightcurves of the primary (short-period) and the secondary (long-period), which are additive in linear flux units, were separated. The long-period component containing the mutual events and the secondary rotation lightcurve is then used for subsequent numerical modeling.

We constructed models of the two binary asteroids using the technique of Scheirich and Pravec (2009) that was further developed in Scheirich et al. (2015). In following, we outline the basic points of the method, but we refer the reader to the 2009 and 2015 papers for details of the technique.

The shapes of the binary asteroid components were represented with ellipsoids, orbiting each other on a Keplerian orbit with apsidal precession and allowing for a quadratic drift in mean anomaly. The primary was modeled as an oblate spheroid, with its spin axis assumed to be normal to the mutual orbital plane of the components (i.e., assuming zero inclination of the mutual orbit). The shape of the secondary was modeled as a prolate spheroid in synchronous rotation, with its long axis aligned with the centers of the two bodies (i.e., assuming zero libration). The shapes were approximated with 1016 and 252 triangular facets for the primary and the secondary, respectively. The components were assumed to have the same albedo. The brightness of the system as seen by the observer was computed as a sum of contributions from all visible facets using a ray-tracing code that checks which facets are occulted by or are in shadow from the other body. A combination of Lommel-Seeliger and Lambert scattering laws was used (see, e.g., Kaasalainen et al., 2002).

The quadratic drift in mean anomaly, ΔM_d, was fitted as an independent parameter. It is the coefficient in the second term of the expansion of the time-variable mean anomaly:

$$M(t) = M(t_0) + n(t - t_0) + \Delta M_d(t - t_0)^2, \tag{1}$$

where

$$\Delta M_d = \frac{1}{2}\dot{n}, \tag{2}$$

where n is the mean motion, t is the time, and t_0 is the epoch. ΔM_d was stepped from -15 to $+15$ deg/yr^2 in the case of 1999 KW4 and from -9 to $+39$ deg/yr^2 in the case of 2001 SL9 and all other parameters were fitted at each step.[2] The steps in ΔM_d were 0.005 deg/yr^2 and 0.01 deg/yr^2 in the case of 1999 KW4 and 2001 SL9, respectively.

To reduce the complexity of the model, we estimated upper limits on the eccentricity of the mutual orbits by fitting the data from the best covered apparitions: the 2001 apparition for 1999 KW4 and the 2013 apparition for 2001 SL9. The model includes a precession of the line of apsides. The pericenter drift rate depends on the

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[2] ΔM_d of 2001 SL9 was sampled on the larger interval because in our initial modeling runs, there appeared possible solutions at high positive ΔM_d values. Therefore, we expanded the interval in order to examine them; there turned out to be no significant solution at high ΔM_d finally.

mutual orbital period, the mutual semimajor axis and on the polar flattening of the primary (see Murray and Dermott, 1999, Eq. (6.249)). While we know the first two parameters quite well, the polar flattenings are poorly constrained from the data (see Tables **??** and **??**). We therefore fit the drift rate as an independent parameter. Its initial values were stepped in a range from 0 to 25°/day. This range reflects the uncertainties of the three parameters determining the drift rate.

Since we found that the upper limits on eccentricity were low, in further modeling of the data from all apparitions together, we set the eccentricity equal to zero for simplicity and efficiency. This assumption had a negligible effect on the accuracy of other derived parameters of the models.

Across all observations, we found a unique solution for the system parameters except for an ambiguity in the quadratic drift in mean anomaly and the orbital period of 2001 SL9, see Tables **??** and **??**. We describe and discuss these parameters in Sections **??** and **??**. Plots of the RMS residuals (root mean square of observed magnitudes minus the values calculated from the model) vs ΔM_d are shown in Figs. **??** and **??**. In order to save computing time, the plots were constructed using spherical shapes of both components. However, neighborhoods of local minima were then revisited using ellipsoidal shapes in order to improve the fit.

For 1999 KW4, the RMS residuals of the two best local minima obtained using the spherical shapes (with ΔM_d of -0.65 and -1.3 deg/yr^2) were 0.0307 and 0.0320 mag, respectively. The fits improved to 0.0251 and 0.0266 mag using the elipsoidal shapes. The fit is significanly poorer for the latter solution. The former solution provides a satisfactory fit to the data and it is accepted as real solution for the binary asteroid parameters.

For 2001 SL9, the RMS residuals of the five best local minima obtained using the spherical shapes (with ΔM_d of 2.8, 5.2, 7.6, 4.0 and 0.5 deg/yr^2) were 0.0238. 0.0238, 0.0245, 0.0246 and 0.0248 mag, respectively. The fits improved to 0.0236, 0.0236, 0.0243, 0.0245 and 0.0245 mag using the elipsoidal shapes; the marginal improvement is due to that the secondary of 2001 SL9 is not prominently elongated. The first two solutions provide satisfactory fit to the data; one of them is a real solution for the binary asteroid parameters, but we cannot resolve this ambiguity with the available data. The other three solutions with the higher RMS residuals provide significantly poorer fits to the data and they do not appear real.

Figures **??** and **??** show the quadratic drift in the mean anomaly, ΔM, which was computed as follows. We generated a synthetic lightcurve using model with parameters from the best-fit solution except ΔM_d, which was fixed at zero. Then, for each apparition separately, we fitted the mean anomaly of the model in order to obtain the best match between its synthetic lightcurve and the observed data. ΔM is a difference between the mean anomaly of the original model and the fitted one.

Examples of the long-period component data together with the synthetic lightcurves of the best-fit solutions are presented in Figs. **??**, **??** and **??**. Uncertainty areas of the orbital poles are shown in Figs. **??** and **??**.

We estimated realistic uncertainties of the fitted parameters using the procedure described in Scheirich and Pravec (2009). For each parameter, we obtained its admissible range that corresponds to a 3-σ uncertainty.

Fig. 1. The RMS residuals vs. ΔM_d for solutions of the model of (66391) 1999 KW4 presented in Section **??**. Each dot represents the best-fit result with ΔM_d fixed and other parameters varied. The plots were constructed using spherical shapes of both components; see text for details.

Fig. 2. The normalized χ^2 vs. ΔM_d for solutions of the model of (66391) 1999 KW4 presented in Section **??**. The three horizontal lines gives the p-values – the probabilities that the χ^2 exceeds a particular value only by chance, corresponding to 1-, 2- and 3σ interval of the χ^2 distribution with 236 degrees of freedom. See text for details.

Fig. 3. The RMS residuals vs. ΔM_d for solutions of the model of (88710) 2001 SL9 presented in Section **??**. Each dot represents the best-fit result with ΔM_d fixed and other parameters varied. The plots were constructed using spherical shapes of both components; see text for details.

Fig. 4. The normalized χ^2 vs. ΔM_d for solutions of the model of (88710) 2001 SL9 presented in Section **??**. The three horizontal lines gives the p-values – the probabilities that the χ^2 exceeds a particular value only by chance, corresponding to 1-, 2- and 3σ interval of the χ^2 distribution with 359 degrees of freedom. See text for details.

2.3   Statistical significance of the solutions for ΔM_d

The residuals of the model fitted to the observational data do not obey the Gaussian statistics because of systematic errors resulting from model simplifications. In particular, the residuals of nearby measurements appear correlated.

To eliminate the effect we adopted following strategy for evaluating the statistical significance, based on the χ^2 test, of the solutions for ΔM_d.

We choose a correlation time d and for each data point (i) we calculated how many other data points, K_i, are within $\pm d/2$ from the given point. We then applied a weight of $1/K_i$ to the data point in the χ^2 sum. We also calculated an effective number of data points as $N_{\text{eff}} = \sum_{i=1}^{N} 1/K_i$, where N is the total number of data points. For normalized χ^2 we than have $\chi^2 = 1/(N_{\text{eff}} - M) \sum_{i=1}^{N} (O - C)_i^2/(\sigma_i^2 K_i)$, where M is the number of fitted parameters of the model and σ_i is a standard deviation of the ith point. As the residuals are predominated by model rather than observational uncertainties, we assign each data points the same standard deviation $\sigma_i = \sigma$, where σ is the RMS residual of the best fit solution.

The procedure described above is equivalent to reducing the number of data points to one in each time interval with the length d (i.e., to reducing the total number of point to N_{eff}) and assigning $(O - C)^2$ of this point to be a mean of $(O_i - C_i)^2$ of all the points within the interval. However, our approach has the advantage that it does not depend on a particular realisation of dividing the observing time span into intervals of length d.

We choose the correlation time d to be equal to $1/2$ of the mean duration of a descending/ascending branch of the secondary mutual event, i.e., the mean time between the first and the second or between the third and the fourth contact. For 1999 KW4 and 2001 SL9, they are $d = 0.30\,\text{h}$ and $0.15\,\text{h}$, respectively. We also tested them with d twice as long, i.e., equal to the full mean duration of the secondary event branch, but we found it to be inadequate as the longer correlation time resulted in a substantial loss of information by a too big reduction of the data points.

We note that the mutual orbit model fit is sensitive only to data points in mutual events and their closest neighborhood. Therefore we limited the above analysis only to such data points; points further outside events were not used as they contain information on secondary's rotation, but they do not effectively contribute to determination of the mutual orbit.

Plots of the normalized χ^2 vs ΔM_d for values of ΔM_d close to the best-fit solutions are shown in Figs. **??** and **??** for 1999 KW4 and 2001 SL9, respectively. The plots

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were constructed using elipsoidal shapes of the components. p-values of the χ^2 test (see, e.g., Feigelson and Babu 2012), corresponding to 1, 2 and 3σ interval of the χ^2 distribution with $(N_{\mathrm{eff}} - M)$ degrees of freedom, are also shown.

3 Parameters of (66391) 1999 KW4

In this section, we summarize the best-fit model parameters of the binary system (66391) 1999 KW4 and overview previous publications. The parameters are listed in Table **??**.

In the first part of the table, we present data derived from optical and spectroscopic observations of the system. H_V and G are the mean absolute magnitude and the phase parameter of the H–G phase relation (Bowell et al., 1989). Using H_V and effective diameter of the whole system $(D_{\mathrm{eff}} \equiv (D_{1,\mathrm{C}}^2 + D_{2,\mathrm{C}}^2)^{1/2})$ at the mean observed aspect of 27° (see below), we derived the visual geometric albedo p_V. We note that our value is in agreement with $p_V = 0.19 \pm 0.05$ derived by Devogèle et al. (2019) from their polarimetric observations. We also observed 1999 KW4 in near-infrared spectral range and classified it as a Q type asteroid (see Appendix A.).

In the next two parts of Table **??**, we give parameters for the components of the binary. The indices 1 and 2 refer to the primary and the secondary, respectively.

$D_{i,\mathrm{C}}$ is the cross-section equivalent diameter, i.e., the diameter of a sphere with the same cross section, of the i-th component at the observed aspect. Since the aspect changed with time, the given value is an average over all lightcurve sessions. To quantify the mean aspect we used an asterocentric latitude of the Phase Angle Bisector (PAB), which is the mean direction between the heliocentric and geocentric directions to the asteroid. As discussed in Harris et al. (1984), this is an approximation for the effective viewing direction of an asteroid observed at non-zero solar phase. The average absolute value of the asterocentric latitude of the PAB (computed using the nominal pole of the mutual orbit; we assume that the spin poles of both components are the same as the orbit pole) was 27°.

$D_{i,\mathrm{V}}$ is the volume equivalent diameter, i.e., the diameter of a sphere with the same volume, of the i-th component. $D_{2,\mathrm{C}}/D_{1,\mathrm{C}}$ is the ratio between the cross-section equivalent diameters of the components. P_i is the rotational period of the i-th component.

An analysis of the best subset of data for the secondary rotation taken from 2018-06-07.9 to -11.0 gave a formal best-fit estimate for the secondary rotation period of 17.53 ± 0.12 h (3σ; this includes also a synodic-sidereal difference uncertainty). This agrees with the mutual orbit period, within the error bar. Considering that all the observed secondary lightcurve minima coincide with or lie close to the mutual events —small differences may be due to a phase effect or secondary libration—, it is very likely that the secondary is in synchronous rotation. We therefore assume that P_2 is equal to the orbital period (see Table **??**).

Table 4
Properties of binary asteroid (66391) 1999 KW4.

Parameter	Value	Unc.	Reference
Whole system:			
H_V	16.74 ± 0.22	1σ	This work
G	$(0.24 \pm 0.11)^a$	1σ	This work
p_V	0.162 ± 0.034	1σ	This work
Taxon. class	Q		This work
Primary:			
$D_{1,C}$ (km)	1.367 ± 0.041^b	1σ	From O06
$D_{1,V}$ (km)	1.317 ± 0.040	1σ	O06
P_1 (h)	2.7645 ± 0.0003	1σ	O06
$(A_1 B_1)^{1/2}/C_1$	$\leq 1.6^c$ / 1.17 ± 0.15	3σ	This work / O06
A_1/B_1	1.04 ± 0.04	1σ	O06
ρ_1 (g cm^{-3})	$1.3^{+0.7}_{-0.4}$ / 1.97 ± 0.72	3σ	This work / O06
Secondary:			
$D_{2,C}/D_{1,C}$	0.42 ± 0.03^d	3σ	This work
$D_{2,C}$ (km)	0.574 ± 0.066	3σ	This work
$D_{2,V}$ (km)	$(0.59 \pm 0.04)^e$	1σ	This work
P_2 (h)	$(17.46)^f$		This work
A_2/B_2	$1.3^{+0.3}_{-0.1}$	3σ	This work
Mutual orbit:			
$a/(A_1 B_1)^{1/2}$	1.7 ± 0.2	3σ	This work
a (km)	2.548 ± 0.015	1σ	O06
(L_P, B_P) (deg.)	$(329.6, -62.3) \pm (12 \times 4)^g$	3σ	This work
P_{orb} (h)	17.45763 ± 0.00004^h	3σ	This work
L_0 (deg.)	40 ± 5^h	3σ	This work
e	≤ 0.006	3σ	O06
ΔM_d (deg/yr^2)	-0.65 ± 0.16	3σ	This work
$\dot{P}_{\mathrm{orb}}$ (h/yr)	0.00013 ± 0.00003	3σ	This work
$\dot{a}$ (cm/yr)	1.2 ± 0.3	3σ	This work

References: O06 (Ostro et al., 2006)

[a] The range of high solar phase angles covered by the observations did not allow to determine the G parameter. We assumed the mean G value for S-complex asteroids (Warner et al., 2009).

[b] Derived from the primary shape model by O06 and for the average observed aspect. See text for details.

[c] The formal best-fit value is 1.1.

[d] This is a ratio of the cross-section equivalent diameters for the average observed aspect of 27°. See text for details.

[e] Derived using the shape model of the secondary from O06 rescaled by 130%. See text for details.

[f] The secondary appears to be in synchronous rotation. See text for details.

[g] These are the semiaxes of the uncertainty area; see its actual shape in Fig. **??**.

[h] The P_{orb} and L_0 values are for epoch JD 2455305.0 (asterocentric time, i.e., light-time corrected), for which P_{orb} and ΔM_d do not correlate.

$(A_1 B_1)^{1/2}/C_1$ is a ratio between the mean equatorial and the polar axes of the primary. A_i/B_i is a ratio between the equatorial axes of the i-th component (equatorial elongation). $\rho_1 = \rho_2$ are the bulk densities of the two components, which we assumed to be the same in our modeling.

Most of the reported quantities have been derived as the parameters of our model described in Section **??** fitted to our observational data. Some values were taken or derived using data from other sources as we describe in following.

The cross-section and volume equivalent diameters of the primary were derived using the shape model of the primary from Ostro et al. (2006). Assuming its spin pole is the same as the mutual orbit pole (see below), we computed its rotationally averaged cross-section for each lightcurve session and present the mean value over all sessions. Its 1σ uncertainty was computed using the uncertainties of the dimensions of the primary from Ostro et al. (2006).

$D_{1,\mathrm{V}}$ was taken from Table 2 of Ostro et al. (2006).

$D_{2,\mathrm{V}}$ was derived using the shape model of the secondary by Ostro et al. (2006), rescaled to 130% of its original size to match mutual events' depths from our data (see below). Its 1σ uncertainty is a formal value taken from Table 2 of Ostro et al. (2006), but the real uncertainty may be higher because of uncertainties of the secondary radar shape model (Lance Benner, personal communication).

In the last part of Table **??**, we summarize the parameters of the mutual orbit of the binary components. a is the semimajor axis, $L_\mathrm{P}, B_\mathrm{P}$ are the ecliptic coordinates of the orbital pole in the equinox J2000, L_0 is the length of the secondary (i.e., the sum of angular distance from the ascending node and the length of the ascending node) for epoch JD 2455305.0, e is the orbit eccentricity (only its upper limit was determined), and ΔM_d is the quadratic drift in mean anomaly. Since the orbital period P_orb changes in time, the value presented in Table **??** is valid for epoch JD 2455305.0. For this epoch, which is approximately the mean time of all observed events, a correlation between P_orb and ΔM_d is zero. We also give the time derivatives of the orbital period and the semimajor axis, derived from ΔM_d.

Although the orbit of 1999 KW4 crosses those of Earth, Venus and Mercury, according to JPL HORIZONS system the asteroid experienced only four close approaches to Earth between 2000 and 2019. The approaches took place in May 2001, May 2002, May 2018 and May 2019 at distances of 0.032, 0.089, 0.078 and 0.035 AU, respectively. Since the observed mutual orbit period increase is based on the observations at six effective epochs (apparitions), we can rule out planetary-tug effects as a potential cause for the increase.

The uncertainty area of the orbit pole is shown in Fig. **??**. The size of the area shrinks with increasing the flattening of the primary $(A_1 B_1)^{1/2}/C_1$. To demonstrate the effect, we constrained the orbit pole uncertainties using three fixed values of the flattening (1.0, 1.2 and 1.4) and plotted the respective areas in the figure.

The uncertainties of the mutual semimajor axis and flattening of the primary are

the main sources of the uncertainty of the bulk density of the system. In addition to that, the uncertainties of the two parameters are not independent. We therefore stepped a and $(A_1B_1)^{1/2}/C_1$ on a grid (while all other parameters were fitted at each step) to obtain an uncertainty area of both parameters together. The area is shown in Fig. **??** with values of the bulk density for each combination of the parameters indicated.

The mutual orbit and shapes of the binary asteroid components of 1999 KW4 were modeled by Ostro et al. (2006) with radar observations taken in 2001. They report the size of the primary to be close to a tri-axial ellipsoid with axes $1417 \times 1361 \times 1183$ m (1σ uncertainties of $\pm 3\%$), and the secondary to be a tri-axial ellipsoid with axes $595 \times 450 \times 343$ m (1σ uncertainties of $\pm 5\%$). The dimensions given are extents of dynamically equivalent equal-volume ellipsoid (DEEVE; a homogeneous ellipsoid having the same moments of inertia and volume as the shape model).

They also found the parameters of the mutual orbit to be as follows: orbital period $P_{\mathrm{orb}} = 17.422 \pm 0.036$ h, semimajor axis $a = 2548 \pm 15$ m, eccentricity $e = 0.0004 \pm 0.0019$, pole direction in ecliptic coordinates: $L_{\mathrm{P}} = 325.8 \pm 3.5$ deg, $B_{\mathrm{P}} = -61.8 \pm 1.2$ deg (uncertainties correspond to 1σ).

To compare our results with the values from Ostro et al. (2006), we computed $(A_1B_1)^{1/2}/C_1$ and $a/(A_1B_1)^{1/2}$ using their DEEVE for the primary and their semimajor axis of the mutual orbit. The result is plotted as a solid point in Fig. **??** with 1σ error bars.

There is one significant discrepancy between our results and those by Ostro et al. (2006): We obtained a significantly larger secondary-to-primary size ratio. To compare their result with ours, we computed a mean (rotationally averaged) cross-section ratio from the component shapes by Ostro et al. (2006): $(D_{2,\mathrm{C}}/D_{1,\mathrm{C}})_{\mathrm{radar}} = 0.34 \pm 0.02$ (1σ) at the same mean aspect as our observations (asterocentric latitude of the Phase Angle Bisector, $B_{\mathrm{PAB}} = 27°$). The value is significantly lower than our $D_{2,\mathrm{C}}/D_{1,\mathrm{C}} = 0.42 \pm 0.03$ (3σ).

To look more into the discrepancy between the secondary-to-primary size ratios by Ostro et al. (2006) and by us, we performed following test. Using the shape models of both components from Ostro et al. and the orbital parameters from Table **??**, we generated a synthetic long-period component of the lightcurve. We then increased the size of the secondary until the depths of the secondary events (occultations and eclipses of the secondary) matched the observed event depths. We obtained a match when we increased the secondary axes by Ostro et al. (2006) to 130% of their original values. This is even slightly greater than $0.42/0.34 \doteq 124\%$ because in this test a more realistic scattering model (a combination of Lommel-Seeliger and Lambert scattering) was used for calculating the synthetic lightcurve, which models the scattering from non-spherical component shapes at the high solar phases and it is more precise than simply comparing the estimated mean cross-sections above. We note that replacing the parameters of the mutual orbit with those derived by Ostro et al. did not change the result.

We discussed this issue with Lance Benner and we received following information:

"The dimensions of the secondary might be underestimated by Ostro et al. (2006) because the radar images were obtained at relatively coarse range and Doppler resolutions and at modest signal-to-noise ratios. Consequently, it is plausible that the trailing edge of the secondary in the radar images were less than would be detected if the SNRs were substantially higher." (Lance Benner, personal communication.)

Fig. 5. Selected data of the long-period lightcurve component of (66391) 1999 KW4. The observed data are marked as points. The solid curve represents the synthetic lightcurve for the best-fit solution with $\Delta M_d = -0.65$ deg/yr^2. For comparison, the dashed curve is the model with ΔM_d fixed at 0.0 deg/yr^2 and all other parameters varied to obtain the best fit.

Fig. 6. A time evolution of the mean anomaly difference ΔM for (66391) 1999 KW4. See text for details. Each point corresponds to the middle of one of the six apparitions from 2000 to 2019. Vertical error bars represent estimated 3σ uncertainties of the event times, expressed in mean anomaly. The solid curve is a quadratic fit to the data points.

Fig. 7. Area of admissible poles for the mutual orbit of (66391) 1999 KW4 in ecliptic coordinates (grey area) for $(A_1 B_1)^{1/2}/C_1 = 1$. The dot is the nominal solution given in Table **??**. This area corresponds to 3σ confidence level. To demonstrate the effect of a flattening of the primary on the estimated pole, the areas confined by solid lines shows the admissible poles constrained using $(A_1 B_1)^{1/2}/C_1 = 1.2$ (middle area) and 1.4 (the smallest area). The open circle with error bars represents a solution for the orbital pole from Ostro et al. (2006) with 1σ uncertainties. The south pole of the current asteroid's heliocentric orbit is marked with the cross.

Fig. 8. Area of admissible combinations of the ratio between the mean equatorial and the polar axes of the primary $((A_1 B_1)^{1/2}/C_1)$ and the semimajor axis of the mutual orbit a of (66391) 1999 KW4. This area corresponds to 3σ confidence level. Values of the bulk density of the system (ρ) in g cm^{-3} are indicated. The dot with the error bars is the result from Ostro et al. (2006) and its 1σ uncertainties (see text for details).

4 Parameters of (88710) 2001 SL9

In this section, we summarize the best-fit model parameters of the binary system (88710) 2001 SL9 and overview previous publications. The parameters are listed in Table **??**.

The notation of the values in the table and their uncertainties are the same as in Table **??** (see Section **??**).

The average absolute value of the asterocentric latitude of the PAB (computed using the nominal pole of the mutual orbit, assumed to be the rotation pole of both components) was 11°; we observed the asteroid close to equator-on.

Three works were published reporting spectroscopic observations of 2001 SL9 in the visual and near-infrared spectral range: Lazzarin et al. (2004, 2005) and Pajuelo et al. (2018). Based on moderate slope and broad 1μm and 2μm absorbtion bands, Lazzarin et al. (2004) and (2005) classified 2001 SL9 as an Sr and Q type, respectively. Pajuelo et al. found that the taxonomic types that fit their NIR spectrum are Sr, S and Sq, with Sr being the best fit.

From the measured H_V and assuming the mean albedo $p_V = 0.20 \pm 0.05$ for S-complex asteroids (Pravec et al., 2012), we estimated the effective diameter of the system D_{eff} at the observed (near equator-on) aspect.

A rotational state of the secondary is particularly important for the interpretations we present in Section **??**. However, as the amplitude of the secondary rotation lightcurve is very low, we could not derive its rotation period from the available data. It appears that the secondary is nearly spheroidal with low equatorial elongation.

Pravec et al. (2016) showed that asynchronous secondaries are absent among observed binary systems with close orbits ($a/D_1 \lesssim 2.2$, $P_{\mathrm{orb}} \lesssim 20$ h). They also pointed out that asynchronous secondaries are typically observed on eccentric orbits. Based on that, the parameters of the mutual orbit of 2001 SL9 (a close orbit with low or zero eccentricity) and the fact that the secondary spin relaxation is typically faster than the orbit circularization (Goldreich and Sari, 2009), we assume that the secondary of 2001 SL9 is in synchronous rotation, i.e., its rotation period is the same as the orbit period.

Earlier work where some of the binary asteroid parameters were derived is Pravec et al. (2006). Their values ($P_1 = 2.4004 \pm 0.0002$ h, $P_{\mathrm{orb}} = 16.40 \pm 0.02$ h, $D_{2,\mathrm{C}}/D_{1,\mathrm{C}} = 0.28 \pm 0.02$, $D_{1,\mathrm{C}} = 0.8$ km uncertain to a factor of two) are generally in agreement

Table 5
Properties of binary asteroid (88710) 2001 SL9.

Parameter		Value	Unc.	Reference
Whole system:				
H_V		17.98 ± 0.02	1σ	This work
G		0.34 ± 0.03	1σ	This work
$V - R$		0.457 ± 0.010	1σ	This work
D_{eff} (km)		0.75 ± 0.10^a	1σ	This work
Taxon. class		Sr, Q		P18, L05
Primary:				
$D_{1,\mathrm{C}}$ (km)		0.73 ± 0.32	3σ	This work
$D_{1,\mathrm{V}}$ (km)		0.77 ± 0.34	3σ	This work
P_1 (h)		2.4004 ± 0.0002	1σ	P06
$(A_1 B_1)^{1/2}/C_1$		$\leq 2.2^b$	3σ	This work
A_1/B_1		1.07 ± 0.01	1σ	PH07
$\rho_1 = \rho_2$ (g cm^{-3})		$1.8^{+2.5}_{-0.5}$	3σ	This work
Secondary:				
$D_{2,\mathrm{C}}/D_{1,\mathrm{C}}$		0.24 ± 0.02	3σ	This work
$D_{2,\mathrm{C}}$ (km)		0.18 ± 0.08	3σ	This work
$D_{2,\mathrm{V}}$ (km)		$(0.18 \pm 0.08)^c$	3σ	This work
P_2 (h)		$(16.40)^d$		
A_2/B_2		≤ 1.2	3σ	This work
Mutual orbit:	Solution			
$a/(A_1 B_1)^{1/2}$		1.75 ± 0.3	3σ	This work
$(L_{\mathrm{P}}, B_{\mathrm{P}})$ (deg.)		$(302, -73) \pm (10 \times 4)^e$	3σ	This work
P_{orb} (h)	1.	16.4022 ± 0.0002^f	3σ	This work
	2.	16.4027 ± 0.0002^f		
L_0 (deg.)	1.	51 ± 5^f	3σ	This work
	2.	56 ± 5^f		
e		≤ 0.07	3σ	This work
ΔM_d (deg/yr^2)	1.	2.8 ± 0.2	3σ	This work
	2.	5.2 ± 0.2		
$\dot{P}_{\mathrm{orb}}$ (h/yr)	1.	-0.00048 ± 0.00003	3σ	This work
	2.	-0.00089 ± 0.00004		
$\dot{a}$ (cm/yr)	1.	-2.8 ± 0.2	3σ	This work
	2.	-5.1 ± 0.2		

References: L05 (Lazzarin et al., 2005), P18 (Pajuelo et al., 2018), P06 (Pravec et al., 2006), PH07 (Pravec and Harris, 2007).

[a] From the derived H_V and assumed $p_V = 0.20 \pm 0.05$ that is the mean albedo for S-complex asteroids (Pravec et al., 2012).

[b] The formal best-fit value is 1.7.

[c] Assuming a spherical shape of the secondary.

[d] The secondary is assumed to in synchronous rotation. See text for details.

[e] These are the semiaxes of the uncertainty area; see its actual shape in Fig. **??**.

[f] These are the periods and L_0 for epoch JD 2456182.39026 (asterocentric time, i.e.,

with our current best estimated parameters, but they did not perform a modeling in order to get parameters of the mutual orbit.

(88710) 2001 SL9 appears to be a typical near-Earth binary asteroid according to its basic parameters. Its bulk density of ~ 1.8 g cm^{-3} is in good agreement with its rocky taxonomical class. The normalized total angular momentum content of 2001 SL9 is $\alpha_L = 1.1 \pm 0.2$ (1-σ uncertainty), i.e., in the range 0.9–1.3 for small near-Earth and main belt asteroid binaries and exactly as expected for the proposed formation of small binary asteroids by fission of critically spinning rubble-pile progenitors (Pravec and Harris, 2007).

According to JPL HORIZONS system, the closest Earth, Venus and Mars approaches of 2001 SL9 from 2001 to 2015 were 0.22, 0.13 and 0.36 AU, respectively. We can therefore rule out planetary-tug effects as a potential cause for the observed mutual orbital period decrease.

Fig. 9. Selected data of the long-period lightcurve component of 2001 SL9. The observed data are marked as points. The solid and dashed curves represent the synthetic lightcurves of the two best-fit solutions with $\Delta M_d = 2.8$ and 5.2 deg/yr^2, respectively. For comparison, the dotted curve is for the best-fit model with ΔM_d fixed at 0.0 deg/yr^2.

Fig. 10. Same as Fig. **??**, but for data from later dates.

Fig. 11. Time evolutions of the mean anomaly difference ΔM for (88710) 2001 SL9. See text for details. Each point corresponds to the middle of one of the five apparitions from 2001 to 2015. The open and solid circles stand for the two solutions with $\Delta M_d = 2.8$ and $5.2 \, \mathrm{deg/yr^2}$, respectively. The sizes of the symbols in vertical direction represent estimated 3σ uncertainties in the timing of events ($\pm 5°$ in mean anomaly). The curves are quadratic fits to the data points.

Fig. 12. Area of admissible poles for the mutual orbit of (88710) 2001 SL9 in ecliptic coordinates (grey area). The dot is the nominal solution given in Table **??**. This area corresponds to 3σ confidence level. The south pole of the current asteroid's heliocentric orbit is marked with the cross.

Fig. 13. Area of admissible combinations of the ratio between the mean equatorial and the polar axes of the primary $((A_1 B_1)^{1/2}/C_1)$ and the semimajor axis of the mutual orbit a of (88710) 2001 SL9. This area corresponds to 3σ confidence level. Values of the bulk density of the system (ρ) in g cm^{-3} are indicated.

5 Implications for the BYORP effect

5.1 (66391) 1999 KW4 BYORP Modeling

McMahon and Scheeres (2010b) computed a BYORP coefficient, B, for the secondary shape of 1999 KW4 based on the model published by Ostro et al. (2006). The nominal coefficient was found to be $B_{nom} = 2.082 \times 10^{-2}$, and based on the other parameters of the system this produced a semimajor axis drift rate of approximately 7 cm/yr, according to the relationship

$$\dot{a}_B = \frac{2P_\Phi}{a_h^2 \sqrt{1 - e_h^2}} \frac{a^{3/2} R_{mean}^2}{m_s \sqrt{\mu}} B, \tag{3}$$

where P_Φ is the solar radiation pressure constant, whose value is taken to be 10^{14} kg km/s^2; a_h is the heliocentric orbit semimajor axis of 0.642 AU, and $e_h = 0.688$ is the heliocentric orbit eccentricity. The other values – binary orbit semimajor axis, a, secondary mass, m_s, binary gravitational parameter, μ can be obtained from Table **??**. The secondary mean radius, R_{mean} was computed as average of vertices of the shape model of the secondary from Ostro et al., scaled up by 130%. The secondary mass can be expressed in terms of the estimated secondary volume, V_s and bulk density, ρ_s. The values are: $V_s = 0.105$ km^3, $\mu = 131.5$ m^3/s^2, $a = 2.548$ km, $R_{mean} = 283.7$ m. [3]

For ρ_s we used a value of 1.97 g/cm^3 – the density of the primary from Ostro et al., assuming that both components have the same density. The BYORP modeling with these newly estimated parameters gives $\dot{a} = 8.53$ cm/year, which is significantly larger than the observed value of 1.2 cm/year.

Given the previous discussion of the uncertainty in the secondary shape from Ostro et al. (2006), and the fact that we find an increase in size of approximately 30%, it is reasonable to assume that many details of the shape may not be accurately known. If the topography changes, the predicted BYORP coefficient will also change. To investigate this, we modeled the predicted BYORP effect for a suite of shapes similar to the KW4 secondary radar shape model from Ostro et al. (2006), to compute the likely range of values for the BYORP effect, using the computational model of McMahon and Scheeres (2010a), which incorporates self-shadowing and secondary intersections of re-radiated energy. The shapes were changed by perturbing the vertices radially [4] using the random Gaussian spheroid method (Muinonen 2010). The radial perturbations were set to approximate the size estimate accuracy given in Ostro et al. (2006) of 6% of the long axis, which comes out to 17.1 m for a 1σ radial dispersion. The correlation distances were set as 50 m (making small scale, "spiky" topography features), 150 m, and 300 m (smoother global variations in topography).

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[3] Note that the mean radius (R_{mean}) used to normalize the BYORP coefficient (B) is the mean of the vertex radii of the shape model. Upon scaling the KW4 secondary shape model up by 130% here, the mean radius to be used in Eq. (**??**) is 283.7 m.
[4] The vector from the origin to the vertex keeps its direction, but changes its magnitude.

The BYORP coefficients were computed for 90 such randomly perturbed shapes for each correlation distance.

The results of this process can be seen in Fig. **??**. As can be seen, these drift rates are all still higher than the measured value. The associated BYORP coefficients range from $B_{min} = 7.701 \times 10^{-3}$ to $B_{max} = 3.323 \times 10^{-2}$.

Fig. 14. Histogram of the resulting BYORP induced semimajor axis drift rates for the 270 perturbed secondary shape models of 1999 KW4.

One other parameter that is poorly constrained in Eq. **??** is the secondary density. In fact, while the previous computations assumed an equal density across both components, Ostro et al (2006) reported its large uncertainty. The effect of a variation in secondary density (with total system mass μ being held constant) can be seen in Fig. **??**. It can be seen here that in order for the secondary density alone to modify the semimajor axis drift rate to match the measured value – even with the minimum BYORP coefficient seen – the secondary density would have to be approximately 3.6 g/cm^3 – significantly higher than Ostro's estimate, and requiring a significantly more dense secondary than primary, but not impossible in terms of bulk density alone.

Fig. 15. Variation of $\dot{a}_B$ with secondary density, for the nominal and minimum BYORP coefficients.

The total semimajor axis drift rate for a binary asteroid is governed by the interplay between BYORP and tides, however tides are always expansive for 1999 KW4. The tide induced semimajor axis drift rates can be computed (Jacobson and Scheeres, 2011) as

$$\dot{a}_T = 3\frac{k_p}{Q}\left(\frac{\omega_d}{a_{rp}^{11/2}}\right)q\sqrt{1+q}, \tag{4}$$

where the surface disruption spin limit for a sphere is given by

$$\omega_d = (4\pi G\rho/3)^{1/2} \tag{5}$$

and q is the mass ratio, k_p is the tidal Love number of the primary, Q is the tidal dissipation number, and G is the gravitational constant, and $a_{rp} = a/(D_{1,V}/2)$ is the binary semimajor axis in units for primary radii. For the current estimate of 1999 KW4, $q = m_s/m_p = 0.090$, $\omega_d = 6.501 \times 10^{-4}$ rad/s, and the primary radius is taken to be $R_p = 0.6585$ km.

Q/k_p is a relatively unknown parameter for rubble pile asteroids, but two values have emerged from the literature: 2.15×10^7 (Taylor and Margot, 2011; recomputed from their value of μQ derived for 1999 KW4) and 2.40×10^5 (Scheirich et al. 2015; derived for 1996 FG3). Since the theory and observations suggest that Q/k scale with R_p (Nimmo and Matsuyama, 2019), we scaled the second value (from 1996 FG3) using diameter of 1999 KW4 to 1.87×10^5. We note that Taylor and

Margot (2011) assumed a maximum tidal evolution timescale and so their Q/k is a lower bound.

Using these two values as bounds, we find that the tide induced semimajor axis drift rate ranges from ≤ 0.0158 to 1.813 cm/yr.

The semimajor axis drift rate from BYORP is also lowered if the secondary is librating significantly, however the lightcurve observations show little evidence of this, implying that if there is any libration it is small and the degradation in the drift rate would be minimal. Thus, the overall BYORP coefficient may be significantly lower than predicted from our direct geometric theory or have an opposite sign, implying that the system may be moving into an equilibrium.

Given the observed semimajor axis drift rate (1.2 cm/year), we also estimate the BYORP coefficient for a case if the tides were insignificant and for the two values of Q/k_p mentioned above. To explain the observed drift rate due to the BYORP alone, the BYORP coefficient would need to be $B = 0.003$. Considering the tides as well, using $Q/k_p \geq 2.15 \times 10^7$ we obtain $B \geq 0.003$. Using $Q/k_p = 1.87 \times 10^5$ we obtain $B = -1.57 \times 10^{-3}$.

5.2 (88710) 2001 SL9 BYORP Modeling

Unlike with 1999 KW4, there is no detailed shape model available for the secondary of 2001 SL9 (except for an upper limit on its elongation, which is insufficient for BYORP calculation), so that no informed forward modeling for the BYORP coefficient can be carried out. Instead, we compute the value of the BYORP coefficient that would produce the measured semimajor axis drift rates.

Given that the secondary is assumed to be in synchronous rotation while the primary is spinning much faster than the orbit period, the tides work to expand the semimajor axis. Thus, inward BYORP must overcome tides to achieve the measured semimajor axis rates. Due to the uncertainty in the Q/k, we report four possible BYORP coefficients for 2001 SL9 in Table **??** – one for each combination of drift rate and tidal parameters. The first value of $Q/k = 1.1 \times 10^5$ was scaled from the value derived by Scheirich et al. (2015) for 1996 FG3, the second value of $Q/k \geq 2.5 \times 10^7$ was recomputed from μQ derived by Taylor and Margot (2011) for 2001 SL9.

Table 6
Computed BYORP coefficient, B, for SL9 based on measured semimajor axis drift rates and possible Q/k values.

	B	
	$Q/k = 1.1 \times 10^5$	$Q/k \geq 2.5 \times 10^7$
$\dot{a} = $ -2.8 cm/yr	-5.92×10^{-3}	$\leq -6.18 \times 10^{-3}$
$\dot{a} = $ -5.1 cm/yr	-1.10×10^{-2}	$\leq -1.12 \times 10^{-2}$

Note that for 2001 SL9, $q = 0.0128$, $\omega_d = 7.094 \times 10^{-4}$ rad/s, and given the primary radius of 0.385 km ($= D_{1,V}/2$), we get $a_{rp} = 4.177$. It is important to point out that BYORP is the only known physical mechanism that can cause an inward semimajor

axis drift rate, as measured here for 2001 SL9. The computed B coefficient magnitudes are in line with the modeled values for 1999 KW4, providing some confidence that the results are reasonable.

The results shown here, combined with the BYORP-tide equilibrium state detected for 1996 FG3[5] (Scheirich et al., 2015) does imply that BYORP effect seems to be real, but that we cannot adequately compute it as of yet. This inadequacy could either be from error in the shape models or a deficit in the theory.

5.3 Differential Yarkovsky force in binary asteroid system

Another effect affecting the magnitude of the mutual semimajor axis drift is the Yarkovsky force, which affects not only the motion of the center of mass of the whole binary system but also the relative motion of components. We computed the effect by a method described in Vokrouhlický et al. (2005). The shapes of the components were approximated by spheres represented by regular polyhedrons with 504 surface elements. The Yarkovsky accelerations $\mathbf{f_1}$ and $\mathbf{f_2}$ of both components were determined by numerical solution of the heat diffusion problem. The accelerations for the two components differ because of different sizes and spin rates. Moreover, they are affected by mutual shadowing of the components. Assuming zero eccentricity, the drift of the semimajor axis of the mutual orbit is $\dot{a} = 2/n \langle f_\tau \rangle$, where n represents the mean motion and $\langle f_\tau \rangle$ is a heliocentric-orbit averaged value of f_τ – a projection of the difference between the two Yarkovsky accelerations to the transversal direction of the relative motion $\mathbf{e_\tau}$,

$$f_\tau = \mathbf{e_\tau} \cdot (\mathbf{f_2} - \mathbf{f_1}). \tag{6}$$

Without the mutual shadowing of the components the value of $\langle f_\tau \rangle$ would be zero. Therefore, the resulting mutual semimajor axis drift depends also on the orientation of the heliocentric and mutual orbits.

The Yarkovsky acceleration is less sensitive to body's shape than to its thermophysical parameters. The results for the semimajor axis drift are shown in Fig. **??**. For the nominal solution of (66391) 1999 KW4 and the thermal inertia range 100–1000 $\mathrm{J\,m^{-2}\,s^{-1/2}\,K^{-1}}$ (Delbo et al., 2015), the semimajor axis drift is between -4 mm and -8 mm per year. With the pole of mutual orbit inside the admissible area (see Fig. **??**), the drift of mutual semimajor axis can differ by a factor of ~ 2 from the value for nominal solution.

In the case of (88710) 2001 SL9, the Yarkovsky force has only negligible effect on the mutual semimajor axis drift. For the nominal parameters the drift is ~ -1 mm/yr (see Fig. **??**). Depending on the orientation of the mutual orbit within its admissible area, the value can differ by a factor of ~ 2.

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[5] In Scheirich et al., 2015, we did not include the length of the secondary, L_0, in Table 3. We complete the information here: its value is 56 ± 6 deg for epoch JD 2450183.47442 (asterocentric time, i.e., light-time corrected).

Fig. 16. Semimajor axis drift of the mutual orbit due to differential Yarkovsky effect as a function of thermal inetria Γ. Solid curve corresponds to (66391) 1999 KW4 and the dashed one corresponds to (88710) 2001 SL9.

6   Conclusions

The near-Earth asteroids (66391) 1999 KW4 and (88710) 2001 SL9 are among the best characterized small binary asteroid systems. They are typical members of the population of near-Earth asteroid binaries for most of their parameters. With the data from our photometric observations taken during six apparitions over the time interval of 19 years and during five apparitions over almost 14 years for (66391) and (88710), respectively, we constrained the long-term evolution of their binary orbits.

For (66391), we found that the semimajor axis of its mutual orbit is expanding with a rate of 1.2 ± 0.3 cm/yr (3σ). The observed drift is on an order of the theoretical drift rate caused by mutual tides (≤ 0.0158 to 1.813 cm/yr). However the predicted drift caused by the BYORP effect (8.53 cm/yr) is much higher than the observed value. Thus, the BYORP coefficient may be significantly lower than predicted from

a direct geometric theory by McMahon and Scheeres (2010a) or have an opposite sign, implying that the system may be moving into an equilibrium.

For (88710), we found that the semimajor axis of its mutual orbit is shrinking with a rate of -2.8 ± 0.2 or -5.1 ± 0.2 cm/yr (3σ). The BYORP effect is the only known physical mechanism (except the differential Yarkovsky effect, which is much slower than the observed value) that can cause an inward drift. Since there is no shape model available for the secondary, no forward modeling for the BYORP coefficient is possible. Instead, the BYORP coefficient can be computed from the measured drift rates. The computed coefficient magnitudes are similar to the modeled values for (66391) 1999 KW4, providing some confidence that the results are reasonable.

Acknowledgements

Appendix A. Taxonomic classification of (66391) 1999 KW4

Near-infrared (NIR) spectra (0.7-2.5 μm) of (66391) 1999 KW4 were obtained in low-resolution prism mode on May 28, 2019 (5:30–7:55 UTC) with the SpeX instrument (Rayner et al., 2003) on NASA Infrared Telescope Facility (IRTF). The asteroid was 12.6 visual magnitude and was observed at a phase angle of 81°, and an airmass of $\sim$1.2-1.7. Weather conditions were stable during the observing run, with a seeing of 0.9" and a humidity of $\sim$25%. During the observations, the 0.8"-slit was oriented along the parallactic angle in order to minimize the effects of differential atmospheric refraction. To avoid saturation, the integration time was limited to 60 seconds. A G-type local extinction star was observed before and after the asteroid in order to correct the telluric bands. Solar analog SAO 120107 was also observed to correct for possible spectral slope variations. All spectra were reduced using the IDL-based software Spextool (Cushing et al., 2004). A detailed description of the steps involved in the data reduction process can be found in Sanchez et al. (2013).

The average NIR spectrum of (66391) 1999 KW4 is shown in Fig. **??**. The spectrum exhibits two very deep absorption bands at 0.94 and 1.94 μm, due to the presence of olivine and pyroxene. Using the online Bus-DeMeo taxonomy calculator

(http://smass.mit.edu/busdemeoclass.html) we found that (66391) is classified as either O- or Q-type in this taxonomic system (DeMeo et al., 2009). A visual inspection shows that the overall spectral characteristics of (66391) are more similar to a Q-type asteroid. However, we noticed that the absorption bands in the NIR spectrum of (66391) are much deeper than those of a typical Q-type. Band depths are measured from the continuum to the band centers and are given as percentage depths (Clark and Roush, 1984). For (66391), we found that the Band I depth is $34.4 \pm 0.2\%$, and the Band II depth is $15.9 \pm 0.2\%$, while the mean spectrum of a Q-type asteroid (DeMeo et al. 2009) has Band I and II depths of $23.8 \pm 0.1\%$, and $6.0 \pm 0.2\%$, respectively. This difference could be attributed to several factors, including mineral abundance, grain size, and the high phase angle at which (66391) was observed (e.g., Sanchez et al. 2012).

Fig. 17. NIR spectrum of (66391) 1999 KW4 and the mean spectrum of a Q-, and an O-type from DeMeo et al. (2009). All spectra are normalized to unity at 0.55 μm.

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This is pdfTeX, Version 3.14159265-2.6-1.40.21 (TeX Live 2020/W32TeX)
(preloaded format=pdflatex 2020.5.12)  2 DEC 2020 08:25
entering extended mode
 restricted \write18 enabled.
 %&-line parsing enabled.
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(./KW4-SL9_paper_rev_v4.tex
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ier/elsart.cls
Document Class: elsart 2007/08/16, 2.20: Elsevier
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Package: latexsym 1998/08/17 v2.2e Standard LaTeX package (lasy symbols)
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LaTeX Font Info:    Overwriting symbol font `lasy' in version `bold'
(Font)                 U/lasy/m/n --> U/lasy/b/n on input line 52.
)
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\c@alg=\count174
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(Font)              <12> on input line 1415.
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(Font)              <8> on input line 1415.
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(Font)              <6> on input line 1415.
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line 14
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File: ulasy.fd 1998/08/17 v2.2e LaTeX symbol font definitions
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\Slashbox=\box49
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Package: natbib 2010/09/13 8.31b (PWD, AO)
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LaTeX Info: Redefining \cite on input line 694.
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) (c:/TeXLive/2020/texmf-dist/tex/latex/graphics/graphicx.sty
Package: graphicx 2019/11/30 v1.2a Enhanced LaTeX Graphics (DPC,SPQR)
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Package graphics Info: Driver file: pdftex.def on input line 105.
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(Font)                  U/euf/m/n --> U/euf/b/n on input line 106.
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Package pdflscape Info: Auto-detected driver: pdftex on input line 81.
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File: l3backend-pdfmode.def 2020-05-05 L3 backend support: PDF mode
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\openout1 = `KW4-SL9_paper_rev_v4.aux'.

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! Package inputenc Error: Invalid UTF-8 byte "96.

See the inputenc package documentation for explanation.
Type  H <return>  for immediate help.
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l.174 ...., Scheeres, D. [2010]. Icarus 209, 494--
                                            509).
The document does not appear to be in UTF-8 encoding.
Try adding \UseRawInputEncoding as the first line of the file
or specify an encoding such as \usepackage [latin1]{inputenc}
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Alternatively, save the file in UTF-8 using your editor or another tool

\c@sv@footnote=\count269
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[4]
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\OT1/cmr/m/n/12 Palo-mar on 2001 Septem-ber 18. Its bi-nary na-ture was
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ed by Pravec et al. (2001).
 []

[5]
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Underfull \hbox (badness 10000) in paragraph at lines 260--262

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Overfull \hbox (83.73624pt too wide) in paragraph at lines 291--312
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LaTeX Warning: `h' float specifier changed to `ht'.

[6]
Underfull \vbox (badness 10000) has occurred while \output is active []

[7] [8]
Underfull \vbox (badness 5417) has occurred while \output is active []

[9] [10]

! LaTeX Error: File `66391_RMS_vs_DMd' not found.

See the LaTeX manual or LaTeX Companion for explanation.
Type H <return> for immediate help.
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l.437 ...phics[width=\textwidth]{66391_RMS_vs_DMd}

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If that doesn't work, type X <return> to quit.

[11]

! LaTeX Error: File `66391_Chi2Norm_vs_DMd' not found.

See the LaTeX manual or LaTeX Companion for explanation.
Type H <return> for immediate help.
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l.448 ...[width=\textwidth]{66391_Chi2Norm_vs_DMd}

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[12]

! LaTeX Error: File `2001sl9_RMS_vs_DMd' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.460 ...ics[width=\textwidth]{2001sl9_RMS_vs_DMd}

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[13]

! LaTeX Error: File `2001sl9_Chi2Norm_vs_DMd' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.471 ...idth=\textwidth]{2001sl9_Chi2Norm_vs_DMd}

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[14]

LaTeX Warning: Float too large for page by 43.19687pt on input line 567.

[15] [16] [17] [18] [19]

! LaTeX Error: File `66391_00-19_synth' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.677 ...hics[width=\textwidth]{66391_00-19_synth}

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[20]

! LaTeX Error: File `66391_additionalM0' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.689 ...ics[width=\textwidth]{66391_additionalM0}

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[21]

! LaTeX Error: File `66391_LB_polar' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.706 ...raphics[width=\textwidth]{66391_LB_polar}

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[22]

! LaTeX Error: File `66391_20Ba_a_PrimA_Rho' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.720 ...width=\textwidth]{66391_20Ba_a_PrimA_Rho}

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LaTeX Warning: Float too large for page by 63.59688pt on input line 793.

[23] [24] [25]

! LaTeX Error: File `2001sl9_01-15_synthA' not found.

See the LaTeX manual or LaTeX Companion for explanation.
Type H <return> for immediate help.
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l.835 ...s[width=\textwidth]{2001sl9_01-15_synthA}

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If that doesn't work, type X <return> to quit.

[26]

! LaTeX Error: File `2001sl9_01-15_synthB' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.846 ...s[width=\textwidth]{2001sl9_01-15_synthB}

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[27]

! LaTeX Error: File `2001sl9_additionalM0' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.857 ...s[width=\textwidth]{2001sl9_additionalM0}

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[28]

! LaTeX Error: File `2001sl9_01-15_LB_polar' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.879 ...width=\textwidth]{2001sl9_01-15_LB_polar}

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[29]

! LaTeX Error: File `2001sl9_a_PrimA_Rho' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.891 ...cs[width=\textwidth]{2001sl9_a_PrimA_Rho}

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[30]

! Package inputenc Error: Invalid UTF-8 byte "80.

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Try adding \UseRawInputEncoding as the first line of the file
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Alternatively, save the file in UTF-8 using your editor or another tool

! Package inputenc Error: Invalid UTF-8 byte "9C.

See the inputenc package documentation for explanation.
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Alternatively, save the file in UTF-8 using your editor or another tool

[31]

! LaTeX Error: File `KW4_coeffs_final' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.947 ...cs[width=.75\textwidth]{KW4_coeffs_final}

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! LaTeX Error: File `KW4_adot_vs_beta_density_final' not found.

See the LaTeX manual or LaTeX Companion for explanation.
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l.961 ...extwidth]{KW4_adot_vs_beta_density_final}

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If that doesn't work, type X <return> to quit.

[32]

! LaTeX Error: Unknown float option `d'.

See the LaTeX manual or LaTeX Companion for explanation.
Type H <return> for immediate help.
 ...

l.1026 \begin{table}[htdp]

Option `d' ignored and `p' used.

[33]

LaTeX Warning: File `y.pdf' not found on input line 1087.

! Package pdftex.def Error: File `y.pdf' not found: using draft setting.

See the pdftex.def package documentation for explanation.
Type H <return> for immediate help.
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l.1087 ...includegraphics[width=\textwidth]{y.pdf}

Try typing <return> to proceed.
If that doesn't work, type X <return> to quit.

[34] [35] [36]

! LaTeX Error: File `1999KW4_NIR_rev' not found.

See the LaTeX manual or LaTeX Companion for explanation.
Type H <return> for immediate help.
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l.1158 ...phics[width=\textwidth]{1999KW4_NIR_rev}

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s
Try typing <return> to proceed.
If that doesn't work, type X <return> to quit.

! Package inputenc Error: Invalid UTF-8 byte "96.

See the inputenc package documentation for explanation.
Type H <return> for immediate help.
 ...

l.1184 ...eroids II. Univ. Arizona Press, pp. 524–
                                                -556.
The document does not appear to be in UTF-8 encoding.
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or specify an encoding such as \usepackage [latin1]{inputenc}
in the document preamble.
Alternatively, save the file in UTF-8 using your editor or another tool

[37]

! Package inputenc Error: Invalid UTF-8 byte "96.

See the inputenc package documentation for explanation.
Type H <return> for immediate help.
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l.1209 ...V. University of Arizona Press, pp. 107–
                                                -128
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l.1222 Icarus 147, 487–
                          -497.
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l.1234 251–
            258.
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l.1252 Sol. Syst. Res. 38(3), 241-
                                    -248.
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in the document preamble.
Alternatively, save the file in UTF-8 using your editor or another tool

[38]

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See the inputenc package documentation for explanation.
Type H <return> for immediate help.
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l.1307 ...he Royal Astronomical Society 477, 5590-
                                                  -5604
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[39]

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See the inputenc package documentation for explanation.
Type H <return> for immediate help.
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l.1319 Icarus 190, 250-
                        -259.
The document does not appear to be in UTF-8 encoding.
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in the document preamble.
Alternatively, save the file in UTF-8 using your editor or another tool

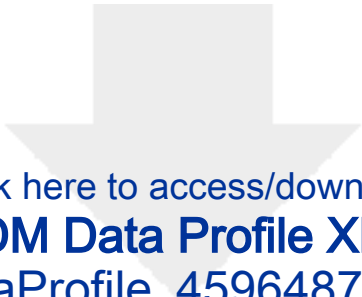Underfull \vbox (badness 4660) has occurred while \output is active []

[40] [41] (./KW4-SL9_paper_rev_v4.aux)

LaTeX Warning: Label(s) may have changed. Rerun to get cross-references
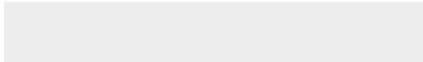right.

)
Here is how much of TeX's memory you used:
 3024 strings out of 480681
 40845 string characters out of 5908536
 278756 words of memory out of 5000000
 18816 multiletter control sequences out of 15000+600000
 545325 words of font info for 78 fonts, out of 8000000 for 9000
 1141 hyphenation exceptions out of 8191
 30i,9n,31p,1471b,290s stack positions out of
5000i,500n,10000p,200000b,80000s
<c:/TeXLive/2020/texmf-
dist/fonts/type1/public/amsfonts/cm/cmbx10.pfb><c:/TeX
Live/2020/texmf-
dist/fonts/type1/public/amsfonts/cm/cmbx12.pfb><c:/TeXLive/2020
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dist/fonts/type1/public/amsfonts/cm/cmtt12.pfb>
<c:/TeXLive/2020/texmf-
dist/fonts/type1/public/amsfonts/symbols/msam10.pfb>
Output written on KW4-SL9_paper_rev_v4.pdf (41 pages, 321663 bytes).
PDF statistics:
 210 PDF objects out of 1000 (max. 8388607)
 147 compressed objects within 2 object streams
 0 named destinations out of 1000 (max. 500000)
 1 words of extra memory for PDF output out of 10000 (max. 10000000)

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Declaration of interests

☒ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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