Pre-impact mutual orbit of the DART target binary asteroid (65803) Didymos derived from observations of mutual events in 2003–2021

2 Abstract

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We modeled photometric observations of mutual events (eclipses and occultations) between the components of the binary near-Earth asteroid (65803) Didymos, the target of the Double Asteroid Redirection Test (DART) space mission, that were taken from 2003 to 2021 (Pravec et al. 2022, submitted). We derived parameters of the modified Keplerian mutual orbit (allowing for a quadratic drift in the mean anomaly, which is presumably caused by an interplay between the BYORP effect and mutual tides, or by differential Yarkovsky force) of the secondary, called Dimorphos, around the Didymos primary and estimated its diameter. The J2000 ecliptic longitude and 10 latitude of the orbital pole are $320.6^{\circ} \pm 13.7^{\circ}$ and $-78.6^{\circ} \pm 1.8^{\circ}$, respectively, and 11 the orbital period is 11.921624 ± 0.000018 h at epoch JD 2455873.0 (asterocentric 12 UTC; all quoted uncertainties correspond to 3σ , except the density estimate below). We obtained the quadratic drift of the mean anomaly of 0.15 ± 0.14 deg/yr². The orbital eccentricity is ≤ 0.03 . We determined the ecliptic longitude and latitude of the radius vector of Dimorphos with respect to Didymos at the nominal time of the 16 DART impact to Dimorphos (JD 2459849.46875 geocentric UTC) to be $222.8^{\circ}\pm7.0^{\circ}$ 17 and $-1.6^{\circ} \pm 4.2^{\circ}$, respectively. We also estimated the bulk density of the system to be $2.37 \pm 0.30 \text{ g cm}^{-3}$ (1 σ uncertainty).

Key words: Asteroids, satellites; Photometry; DART space mission; Hera space

21 mission

22 1 Introduction

The near-Earth asteroid (65803) Didymos, originally designated 1996 GT, was discovered by the *Spacewatch* asteroid survey from Kitt Peak Observatory in Arizona on 1996 April 11. Its binary nature was revealed by Pravec et al. (2003). Pravec et al. (2006) and Scheirich and Pravec (2009) analyzed and modeled photometric data obtained during its close approach to Earth in 2003. They reported initial estimates of the binary system properties, including parameters of the mutual orbit of the two components. The system was also observed using radar from Arecibo and Goldstone in 2003. The radar observations were published and modeled together with the photometric data by Naidu et al. (2020) who obtained a shape model of the primary and determined or constrained several parameters of the binary asteroid system.

Didymos is classified as an S-type asteroid (Cheng et al., 2018) based on vis-IR spectra obtained by de León et al. (2010), also confirmed by Dunn et al. (2013).

The secondary of the Didymos binary system, recently named Dimorphos, has been 35 selected as a target of the Double Asteroid Redirection Test (DART). It is NASA's 36 first planetary defense test mission, with the goal of demonstrating the kinetic 37 impactor mitigation technique on an asteroid. It was launched in November 2021, and it will arrive at the Didymos system on the September 26, 2022 at 23:15 UTC and impact into Dimorphos. The main benefit of targeting a binary asteroid system on a kinetic impactor mission is that it allows the main result of the test – the change in the mutual orbital period – to be measured from Earth via photometric 42 observations, assuming that the binary system exhibits mutual events seen from 43 Earth (Cheng et al., 2015). Rivkin et al. (2021) discuss the factors that led to the recognition that Didymos was the best candidate for a kinetic impactor test, and its selection as the DART target. The Didymos system will be investigated by ESA's Hera mission from the beginning of 2027 for about half a year, which will provide a thorough description of the post-impact state of the binary system (Michel et al., 2022). 49

An important part of the preparation of the DART mission has been an observational effort to precisely determine the orbit of the secondary around the primary. For that, Pravec et al. (2022) obtained photometric observations of the Didymos system taken with several large- or medium-sized groundbased telescopes from 2015 to 2021. In this paper, we present results from mutual orbit modeling using the complete photometry data for mutual events in the Didymos system from 2003 to 2021. An independent derivation of the mutual orbit based on an analysis of mutual event timings has been made by Naidu et al. (2022).

58 2 Mutual orbit model of Didymos system

2.1 Observational data

The data used in our analysis, obtained during five apparitions of Didymos from 2003 to 2021, were published in Pravec et al. (2006, 2022). We briefly summarize them in Table 1. Each row in the table represents one apparition, identified with the mid-UTC date of its first and last observing sessions (runs) rounded to the nearest tenth of a day in the first column. Subsequent columns give the number of observing runs (labeled as *No. of nights*, but we note that they were taken using several telescopes and so more than one run was sometimes taken on a single night) in the given apparition and a reference to where more information on the observations is available.

The data were analysed using the standard technique described in Pravec et al. (2006, 2022). Briefly, by fitting a two-period Fourier series to data points taken outside mutual (occultation or eclipse) events, the rotational lightcurves of the primary and the secondary, which are additive in flux units, are separated. Subtracting the rotational lightcurve of the primary from the data, a long-period (orbital) lightcurve component containing the mutual events and the secondary rotation lightcurve is obtained, which is then used for subsequent numerical modeling. We refer the reader to Pravec et al. (2022) for details of the lightcurve decomposition method.

Table 1 Photometric observations of the Didymos system

Time span	No. of nights	Reference
2003-11-20.9 to 2003-12-20.3	17	P06
2015-04-13.3 to 2015-04-14.4	2	P22
2017-02-23.3 to 2017-05-04.3	13	P22
2019-01-31.4 to 2019-03-11.1	5	P22
2020-12-12.6 to 2021-03-06.3	15	P22

References: P06 (Pravec et al., 2006), P22 (Pravec et al., 2022)

2.2 Numerical model

We constructed the model of the Didymos system using the technique of Scheirich and Pravec (2009) which was further developed by Scheirich et al. (2015, 2021). In the following, we outline the basic points of the method, but we refer the reader to the 2009, 2015, and 2021 papers for details of the technique.

The binary asteroid components were represented with spheres or oblate (for the primary) and prolate (for the secondary) ellipsoids (the ellipsoidal shapes were used to check the sensitivity of the solution to the shapes of the components, see below), orbiting each other on a circular orbit. We choose the circular orbit for simplicity,

as the upper limit on the eccentricity is low (see below). The motion was assumed to be Keplerian, but we allowed for a quadratic drift in the mean anomaly. The spin 87 axis of the primary was assumed to be normal to the mutual orbital plane of the components (i.e., we assumed zero inclination of the mutual orbit. See Appendix A for an assessment of this assumption.). When the secondary was modeled as the prolate spheroid, its long axis was kept aligned with the centers of the two bodies (i.e., in synchronous rotation with zero libration). The shapes were approximated 92 with 1016 and 252 triangular facets for the primary and the secondary, respectively. The components were assumed to have the same albedo and to be exempt from albedo features (see Kaasalainen and Torppa, 2001, for discussion on why albedo features can be neglected). The brightness of the system as seen by the observer was computed as a sum of contributions from all visible facets using a ray-tracing code that checks which facets are occulted by or are in shadow from the other body. A combination of Lommel-Seeliger and Lambert scattering laws was used (see, e.g., 99 Kaasalainen et al., 2002). 100

The quadratic drift in the mean anomaly, ΔM_d , was fitted as an independent parameter. It is the coefficient in the second term of the expansion of the time-variable mean anomaly:

$$M(t) = M(t_0) + n(t - t_0) + \Delta M_d(t - t_0)^2, \tag{1}$$

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$$\Delta M_d = \frac{1}{2}\dot{n},\tag{2}$$

where n is the mean motion, t is the time, and t_0 is the epoch. ΔM_d was stepped from -10 to +10 deg/yr² with a step of 0.01 deg/yr², and all other parameters were fitted at each step.

Since the $3-\sigma$ upper limit on the eccentricity of the mutual orbit is 0.03 only 110 (Scheirich and Pravec, 2009), we set the eccentricity equal to zero for simplicity 111 and efficiency. This assumption had a negligible effect on the accuracy of other derived parameters of the models. Scheirich and Pravec (2009) estimated the upper limit on the eccentricity using the data from the 2003 apparition. We checked that their upper limit is consistent with the data taken in 2015 to 2021, but those later 115 data do not possess the characteristics necessary to use them for constraining the 116 eccentricity more. Those characteristics include sufficient quality, time coverage, and 117 depths of the mutual events. Thus, the constraint on the eccentricity by Scheirich 118 and Pravec (2009) still applies.

Besides the data quality, constraining the eccentricity is also limited by presence of systematic modeling errors for the timings of mutual events. The model systematics are caused by the simplification of the shape of the primary (see below and Fig. 9), which can be up to 5 minutes for the Didymos system. Generally, mutual events between bodies on an eccentric orbit occur at times that are offset from the times of events for a circular orbit. For eccentricity of 0.03, these offsets are between 0 and 5 minutes (corresponding to between 0 and 2.5° in the mean anomaly of the

secondary) for near-central events occurring close to the primary's equator and be-127 tween 0 and 8 minutes (between 0 and 5° in mean anomaly) for non-central events 128 occurring close to the primary's pole. The systematic modeling errors can 129 be confused with the event time offsets caused by non-zero eccentricity 130 because they are comparable in magnitude. To reduce the effect of the systematic modeling errors on eccentricity estimation, either a high number of mutual events would have to be observed so that we get a set of event timings taken at 133 many different primary rotational phases that would average out the shape model-134 ing errors, or use a detailed shape model for the primary (which may be constructed from resolved images that will be taken by DART). 136

Across all observations, we found a unique solution for the system parameters, see Table 2. We describe and discuss these parameters in Section 3.

We estimated uncertainties of the fitted parameters using two techniques. The uncertainties of the relative semimajor axis and the orbital pole (these parameters are strongly determined by the shapes of the mutual events) were estimated using the procedure described in Scheirich and Pravec (2009). The uncertainties of the rest of the parameters, which are determined primarily by the timings of the events, were estimated using the method described in Scheirich et al. (2021), which we outline below.

The residuals of the model fitted to the observational data do not obey the Gaussian statistics because of systematic errors resulting from model simplifications. In particular, the residuals of nearby measurements appear correlated. To eliminate the effect we adopted the following strategy based on the χ^2 test.

We choose a correlation time d and for each data point (i) we calculated how many other data points, K_i , are within $\pm d/2$ from the given point. We then applied a weight of $1/K_i$ to the given data point in the χ^2 sum. We also calculated an effective number of data points as $N_{\text{eff}} = \sum_{i=1}^{N} 1/K_i$, where N is the total number of data points. For normalized χ^2 we then have $\chi^2 = 1/(N_{\text{eff}} - M) \sum_{i=1}^{N} (O - C)_i^2/(\sigma_i^2 K_i)$, where M is the number of fitted parameters of the model and σ_i is a standard deviation of the ith point. As the residuals are predominated by model rather than observational uncertainties, we assign each data point the same standard deviation $\sigma_i = \sigma$, where σ is the RMS residual (root mean square of observed magnitudes, O, minus the values calculated from the model, C) of the best fit solution. An illustration of the weights $1/K_i$ determination is shown in Fig. 1. In Fig. 2, the distribution of residuals with and without the weights applied is shown for comparison.

The procedure described above is equivalent to reducing the number of data points to one in each time interval with the length d (i.e., to reducing the total number of points to N_{eff}) and assigning $(O-C)^2$ of this point to be a mean of $(O_i-C_i)^2$ of all the points within the interval. However, our approach has the advantage that it does not depend on a particular realization of dividing the observing time span into the intervals of length d.

We choose the correlation time d to be equal to 1/2 of the mean duration of a

descending/ascending branch ¹ of the secondary mutual event, i.e., the mean time between the first and the second or between the third and the fourth contact. For the observed events in Didymos, it is d = 0.14 h. (We also tested d to be twice as long, i.e., equal to the full mean duration of the secondary event branch, but we found it to be inadequate as the longer correlation time resulted in a substantial loss of information by deweighting the datapoints too much.)

We note that the mutual orbit model fit is sensitive only to data points covering mutual events and their closest neighborhood. Therefore we limited the above analysis only to such data points; points further outside the events were not used, because they do not effectively contribute to the determination of the mutual orbit.

Upon stepping a given parameter on a suitable interval (while the other parameters fitted) and computing the normalized χ^2 for each step, we determined 3- σ uncertainty of the given parameter as an interval in which χ^2 is below the p-value of the χ^2 test, corresponding to the probability that the χ^2 exceeds a particular value only by chance equal to 0.27%.

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Plot of the normalized χ^2 vs ΔM_d is shown in Fig. 3. In order to save computing time, the plots were constructed using spherical shapes for both components. However, a neighborhood of the best solution was then revisited using ellipsoidal shapes in order to check the sensitivity of the solution to the shapes of the components. No significant change of the solution was found for the polar flattening of the primary up to 1.4 and the equatorial elongation of the secondary up to 1.5. We took these values as the upper limits from Naidu et al., 2020 (the 3σ upper limit for the flattening of the primary) and Pravec et al. 2016 (the upper limit for the elongation of the secondary based on statistics of other small binary asteroids), respectively.

The long-period (orbital) lightcurve component data together with the synthetic lightcurve of the best-fit solution are presented in Figs. 4 to 7. A close examination of the figures reveals that while most of the observed events are fitted well, there are some small or moderate discrepancies between the best-fit model and the data in several mutual events. Those include (a) inprecisely modeled shapes of some primary minima, (b) time offsets of some descending or ascending branches of the events or (c) incorrect depths/lengths of some partial events. We ascribe these discrepancies to the model simplifications, namely to the spherical or ellipsoidal approximation of the shape of the primary. Local topography features on the disc (for the case a) or on the limb (for the cases b and c) of the primary are suspected to be causes of the respective effects.

The uncertainty area of the orbital pole is shown in Fig. 8. Figure 9 shows the quadratic drift in the mean anomaly, ΔM , which was computed as follows. We generated a synthetic lightcurve using the model with parameters from the best-fit solution except ΔM_d , which was fixed at zero. Then, for each lightcurve event

¹ We define a *branch* as a part of the mutual event in the lightcurve, where the brightness of the system is rapidly decreasing or increasing, i.e., the time period during which the eclipsed/occulted body is immersing into or emerging from the shadow of, or is disappearing behind or reappearing from behind the other body.

separately, we fitted the mean anomaly of the model in order to obtain the best match between its synthetic lightcurve and the observed data. ΔM is a difference between the mean anomaly of the original model and the fitted one. For each event, we computed also a standard deviation of ΔM using the procedure described above, but with χ^2 computed only from the data points in the vicinity of the mutual event in question.

214 3 Parameters of Didymos system

In this section, we summarize the best-fit model parameters of the Didymos binary system that we obtained or took from previous publications. The parameters are listed in Table 2.

In the first part of the table, we present data derived from optical and spectroscopic observations of the system. H_V and G are the mean absolute magnitude and the phase parameter of the H–G phase relation (Bowell et al., 1989). p_V is the visual geometric albedo derived by Naidu et al. (2020) using H_V and the effective diameter of the whole system from the 3D radar model.

Didymos is classified as an S-type asteroid (Cheng et al., 2018) based on vis-IR spectra obtained by de León et al. (2010).

In the next two parts of Table 2, we give parameters for the components of the binary. The indices 1 and 2 refer to the primary and the secondary, respectively.

 $D_{1,C}$ and $D_{2,C}$ are the mean (rotationally averaged) cross-section equivalent diameters (i.e., the diameter of a sphere with the same cross-section) of the primary and secondary, respectively, at the mean aspect of observed total secondary events (see below).

To quantify the mean aspect we used an asterocentric latitude of the Phase Angle Bisector (PAB), which is the mean direction between the heliocentric and geocentric directions to the asteroid. As discussed in Harris et al. (1984), this is an approximation for the effective viewing direction of an asteroid observed at the non-zero solar phase. The average absolute value of the asterocentric latitude of the PAB for the observed total events was 9.7°. (We computed the latitude of the PAB using the nominal pole of the mutual orbit and assuming that the spin poles of both components are the same as the orbit pole.)

 $D_{1,V}$ and $D_{2,V}$ are the volume equivalent diameters (i.e., the diameter of a sphere with the same volume) of the primary and secondary, respectively. $D_{2,C}/D_{1,C}$ is the ratio between the mean cross-section equivalent diameters of the components. P_1 is the rotational period of the primary.

 $(A_1B_1)^{1/2}/C_1$ is a ratio between the mean equatorial and the polar axes of the primary. A_1/B_1 is a ratio between the equatorial axes of the primary (equatorial elongation). ρ_1 is the bulk density of the primary.

Table 2 Parameters of Didymos system

Parameter		Value	Unc.	Reference		
Whole system:						
Absolute magnitude	H_V	18.16 ± 0.04	1σ	P12		
Phase parameter	G	0.20 ± 0.02	1σ	K04		
Visual geom. albedo	$p_{ m V}$	0.15 ± 0.04	1σ	N20		
Taxon. class		\mathbf{S}		C18		
Primary:						
Volume equiv. diameter	$D_{1,\mathrm{V}}~(\mathrm{km})$	$D_{1,V} \text{ (km)}$ 0.780 ± 0.03		N20		
Cross-section equiv. diameter	$D_{1,\mathrm{C}}~(\mathrm{km})$	0.786 ± 0.05	1σ	This work/N 20^a		
Rotational period	P_1 (h)	2.2600 ± 0.0001	1σ	N20		
Oblateness	$(A_1B_1)^{1/2}/C_1$	$1.04^{+0.12}_{-0.04}$	1σ	$\mathrm{N}20^b$		
Equatorial elongation	A_1/B_1	$1.02^{+0.09}_{-0.02}$	1σ	$\mathrm{N}20^b$		
Bulk density	$\rho_1~(\mathrm{g~cm^{-3}})$	$2.17 \pm 0.35 \ / \ 2.37 \pm 0.30$	1σ	N20/This work		
Secondary:						
Cross-section equiv. diam. ratio	$D_{2,\mathrm{C}}/D_{1,\mathrm{C}}$	0.217 ± 0.004^c	1σ	This work		
Cross-section equiv. diameter	$D_{2,\mathrm{C}}\;(\mathrm{km})$	0.171 ± 0.011	1σ	This work		
Volume equiv. diameter	$D_{2,\mathrm{V}}~(\mathrm{km})$	$\geq 0.171 \pm 0.011$	see text	This work		
Mutual orbit:						
Sem. axis / primary diam.	$a/(A_1B_1)^{1/2}$	$1.56 \pm 0.20/1.51 \pm 0.22$	3σ	This work/N20 d		
Semimajor axis	a (km)	1.19 ± 0.03	1σ	N20		
Ecl. longitude of orbital pole	$L_{ m P}$ (°)	320.6 ± 13.7^e	3σ	This work		
Ecl. latitude of orbital pole	$B_{ m P}$ (°)	-78.6 ± 1.8	3σ	This work		
Drift in mean anomaly	$\Delta M_d \; ({ m deg/yr^2})$	0.15 ± 0.14	3σ	This work		
Mean motion rate	$\dot{n} (\mathrm{rad/s^2})$	$5.26 \pm 4.91 \times 10^{-18}$	3σ	This work		
Orbital period at t_0	$P_{\rm orb}$ (h)	11.921624 ± 0.000018	3σ	This work		
Orbital period at $t_{\rm imp}$	$P_{ m orb}^{ m imp}$ (h)	11.921473 ± 0.000138	3σ	This work		
Mean anomaly at t_0	$M_0\ (^\circ)$	89.1^{f}		This work		
Eccentricity	e	≤ 0.03	3σ	SP09		
Ecl. coordinates of the secondary	wrt the primary	at t_0				
	$\lambda_0 \ (^\circ)$	320.7 ± 9.8^g	3σ	This work		
	$eta_0~(^\circ)$	11.5 ± 1.9	3σ	This work		
Epoch	t_0 JD 2455873.0 (asterocentric UTC)					
Ecl. coordinates of the secondary wrt the primary at t_{imp}						
	$\lambda_{\mathrm{imp}} \; (^{\circ})$	222.8 ± 7.0^g	3σ	This work		
	eta_{imp} (°)	-1.6 ± 4.2	3σ	This work		
Epoch of impact	$t_{ m imp}$	JD 2459849.46875 (geocen	tric UTC)			

References: C18: Cheng et al. 2018; K04: Kitazato et al. 2004; N20: Naidu et al. 2020; P12: Pravec et al. 2012; SP09: Scheirich and Pravec 2009.

 $[^]a$ Derived using shape model from N20, see text for details. b Derived using DEEVE from N20, see text for details. c This is a ratio of the cross-section equivalent diameters for the average observed aspect of 9.7°. See text for details. d Derived using DEEVE from N20, see text for details. e For the actual shape $\mathfrak{D}f$ the uncertainty area, see Fig. 8. Semiaxes of the area are $1.8 \times 3.0^{\circ}$. f We do not report the uncertainty of M_0 , since it is strongly correlated with $L_{\rm P}$. Instead, we report uncertainties of λ_0 and β_0 . g For the actual shape of the uncertainty areas of λ_0 vs. β_0 and λ_{imp} vs. β_{imp} , see Fig. 10.

 $D_{1,\mathrm{V}}$ and the rotational period of the primary were taken from Naidu et al. (2020). $D_{1,\mathrm{C}}$ was computed from a mean (rotationally averaged) cross-section of the radar shape model from Naidu et al. (2020) at the mean aspect of the observed total events (asterocentric latitude of the PAB being 9.7°). We adopted a 6% relative uncertainty for $D_{1,\mathrm{C}}$. We note that Naidu et al. (2020) give three uncertainties – 4% for the volume-equivalent diameter of the primary, 6% for the extents along x and y principal axes of the primary, and 10% for the extent along z-axis. The 6% uncertainty appears relevant for our derivation of $D_{1,\mathrm{C}}$.

We derived $D_{2,\mathrm{C}}/D_{1,\mathrm{C}}$ from the depths of the observed total secondary events. For that, we used the high-quality data for the secondary events observed in November-December 2003, March 2019 and December 2020 (Pravec et al., 2022). The mean depth of the total secondary events was measured to be 0.050 ± 0.002 mag, which gives $D_{2,\mathrm{C}}/D_{1,\mathrm{C}} = 0.217 \pm 0.004$ (1- σ uncertainties).

From $D_{2,C}/D_{1,C}$ and $D_{1,C}$ we computed $D_{2,C}$. We note that Naidu et al. (2020) reported visible extents of the secondary in the radar data of 150 ± 30 m, which is consistent with our value.

To calculate the secondary volume equivalent diameter $D_{2,V}$ from the determined $D_{2,C}$, we need to use a shape model for the secondary. As Dimorphos' shape has not been determined yet, we explore a range of possible ellipsoidal shapes for it. For a 264 spherical secondary, we have $D_{2,V} = D_{2,C}$. In a case the secondary is a prolate el-265 lipsoid with $A_2/B_2 = 1.5$ and $B_2/C_2 = 1$ —we note that Pravec et al. (2016) found 266 that the equatorial axis ratios of NEA and small MBA binaries show an upper limit 267 of A_2/B_2 about 1.5, hence our choice of the extremally elongated ellipsoid here—, we obtain $D_{2,V} = 0.173 \pm 0.011$ km. While we see here that the secondary volume equivalent diameter is relatively insensitive to the equatorial axis ratio A_2/B_2 , it is more sensitive to B_2/C_2 . Unfortunately there is no formal observational or theo-271 retical constraint on the B_2/C_2 for Dimorphos. To show the sensitivity of $D_{2,V}$ on the polar flattening of the secondary, we calculate $D_{2,V}$ for an arbitrarily chosen value for B_2/C_2 of 1.5. For a case of the oblate secondary with $A_2/B_2 = 1$ and $B_2/C_2 = 1.5$ we obtain $D_{2,V} = 0.181 \pm 0.012$ km, while for a case of $A_2/B_2 = 1.5$ and $B_2/C_2 = 1.5$ we obtain $D_{2,V} = 0.183 \pm 0.012$ km.

Other quantities reported above were taken or derived using data from other sources as we describe in the following.

The mutual orbit and shapes of the Didymos components were modeled by Naidu et al. (2020) from radar observations taken in 2003. They reported the size of the primary to be close to a triaxial ellipsoid with axes $797 \times 783 \times 761$ m (1σ uncertainties of \pm 6%, 6% and 10%, respectively). The dimensions given are extents of a dynamically equivalent equal-volume ellipsoid (DEEVE; a homogeneous ellipsoid having the same moments of inertia and volume as the shape model). We used these values to derive $(A_1B_1)^{1/2}/C_1$ and A_1/B_1 .

The bulk density of the primary (which they assume is the same as the bulk density of the whole system) was taken from Naidu et al. (2020). For comparison, we derived the bulk density of the whole system from the mutual orbital elements obtained in

our work, which leads to $2.37 \pm 0.30 \text{ g cm}^{-3} (1\sigma)$. The derivation of the bulk density is as follows.

Assuming that both components have same bulk density, Kepler's third law can be written in the form (see Scheirich and Pravec, 2009)

$$\frac{4\pi^2}{GP_{\text{orb}}^2} \left[\frac{V_2}{V_1} + 1 \right]^{-1} \frac{a^3}{V_1} = \rho, \tag{3}$$

where ρ is the bulk density, G is the gravitational constant, V_2 and V_1 are volumes of the secondary and the primary, respectively, a is the semimajor axis and P_{orb} is the orbital period. If the primary shape is assumed to be homogenous oblate ellipsoid and considering the effect of the oblateness up to the J_2 term (the first zonal harmonic coefficient in the gravitational potential expansion), the form can be modified to (see Rossi et al., 1999):

$$\frac{4\pi^2 a^3}{G\mathbf{P}_{\text{orb}}^2(V_1 + V_2)} \ \epsilon = \rho,\tag{4}$$

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$$\epsilon = 1 - \frac{3}{10} \frac{A_1^2 - C_1^2}{a^2},\tag{5}$$

where A_1 and C_1 are equatorial and polar axes of the primary, respectively.

We estimated the bulk density (presented in Table 2) using the nominal value of the oblateness of the primary (1.04) taken from Naidu et al. (2020). The equation we used is

$$\rho = \epsilon \frac{24\pi}{GP_{orb}^2} \left[\left(\frac{D_{2,V}}{D_{1,V}} \right)^3 + 1 \right]^{-1} \left(\frac{a}{D_{1,V}} \right)^3.$$
 (6)

The relative semimajor axis value given in Table 2 was also derived using the value of the oblateness of the primary of 1.04. To test the effect of oblateness of the primary on the derivation of a and ρ , we also fitted the data with $(A_1B_1)^{1/2}/C_1$ fixed on three other values: 1.00, 1.16 and 1.40 (the last two values are 1σ upper limit and 3σ upper limit of the oblateness, respectively, taken from Naidu et al., 2020.). The obtained results are given in Table 3. (We note that for spherical shapes $D_{1,\mathrm{V}} = D_{1,\mathrm{C}} = (A_1B_1)^{1/2}$, $D_{2,\mathrm{V}} = D_{2,\mathrm{C}}$ and $\epsilon = 1$ in equation 6.)

We note that the native parameters in our model are the relative dimensions $D_{2,\mathrm{C}}/D_{1,\mathrm{C}}$ and $a/(A_1B_1)^{1/2}$, not the absolute values of $D_{1,\mathrm{V}},D_{2,\mathrm{V}}$ and a. Though we report the volume equivalent diameter of the primary and the mutual semimajor axis estimated by Naidu et al. (2020) in Table 2 as well, our density estimate is completely independent to the

result by Naidu et al. (2020). For completeness, in Table 3 we also give values of the ratios $a/D_{1,\rm V}$ and $D_{2,\rm V}/D_{1,\rm V}$, which appear in Eq. 6, for the tested oblateness values. Those values were derived from fitted values of $D_{2,\rm C}/D_{1,\rm C}$ and $a/(A_1B_1)^{1/2}$.

To compare our Didymos' bulk density estimate with densities of other asteroids with similar composition, we computed a weighted mean of published bulk density estimates for mid- and small-sized S and Q-type asteroids, and got a value of 2.31 g cm⁻³. The data are presented in Table 4. (We did not include the bulk density of 3749 Balam to the weighted mean computation, since the value reported by Marchis et al., 2008, is only approximate and they did not estimate its uncertainty.)

Table 3
The mutual semimajor axis and the bulk density of the Didymos system derived for different values of the oblateness of the primary.

$(A_1B_1)^{1/2}/C_1$	$a/(A_1B_1)^{1/2}$	$a/D_{1,\mathrm{V}}$	$D_{2,\mathrm{V}}/D_{1,\mathrm{V}}$	Density
	3σ unc.	3σ unc.	1σ unc.	$(g cm^{-3}), 1\sigma unc.$
1.00	$\boldsymbol{1.59 \pm 0.20}$	$\boldsymbol{1.59 \pm 0.20}$	$\boldsymbol{0.217 \pm 0.004}$	2.44 ± 0.30
1.04	$\boldsymbol{1.56 \pm 0.20}$	$\boldsymbol{1.58 \pm 0.20}$	$\boldsymbol{0.216 \pm 0.004}$	$\boldsymbol{2.37 \pm 0.30}$
1.16	$\boldsymbol{1.48 \pm 0.19}$	$\boldsymbol{1.56 \pm 0.20}$	$\boldsymbol{0.212 \pm 0.004}$	2.20 ± 0.28
1.40	$\boldsymbol{1.34 \pm 0.13}$	$\boldsymbol{1.50 \pm 0.15}$	$\boldsymbol{0.205 \pm 0.004}$	$\boldsymbol{1.87 \pm 0.18}$

Table 4
Published estimates of the bulk density of mid- and small-sized S and Q-type asteroids

Name or designation	Tax. class	Density	Reference
		$(g cm^{-3}), 1\sigma unc.$	
(243) Ida	S	2.6 ± 0.5	Belton et al. (1995)
(433) Eros	\mathbf{S}	2.67 ± 0.03	Yeomans et al. (2000)
(5381) Sekhmet	\mathbf{S}	1.98 ± 0.65	Neish et al. (2003)
(25143) Itokawa – "head"	\mathbf{S}	2.45 ± 0.23	Kanamaru et al. (2019)
(25143) Itokawa – "body"	\mathbf{S}	1.93 ± 0.05	Kanamaru et al. (2019)
(35107) 1991 VH	$\mathbf{S}\mathbf{q}$	1.5 ± 0.17	Pravec et al. (2006)
$(66063)\ 1998\ RO1-from\ 2003\ data$	\mathbf{S}	$1.5_{-0.20}^{+0.57}$	Scheirich and Pravec (200
$(66063)\ 1998\ RO1-from\ 2004\ data$	\mathbf{S}	$4.1_{-0.93}^{+0.27}$	Scheirich and Pravec (200
$(66391)~{ m Moshup-primary}$	${f Q}$	1.97 ± 0.24	Ostro et al. (2006)
(3749) Balam	\mathbf{S}	~ 2.6	Marchis et al. (2008)

Carry (2012) made a statistical analysis of published estimates of the bulk densities of S-type asteroids and got an average value of 2.72 ± 0.54 g cm⁻³ from the estimates that he considered to be more accurate than 20%. His value, however, is influenced by densities of large asteroids, which he also included in his statistics.

We note that our estimate of the bulk density of the Didymos system is consistent with that by Naidu et al. (2020) within the uncertainty inter-

vals. It is possible that the value of the bulk density of 2.17 ± 0.35 g cm⁻³ estimated by Naidu et al. (2020) is slightly underestimated while our value is slightly overestimated.

In the last part of Table 2, we summarize the parameters of the mutual orbit of 342 the binary components. $L_{\rm P}, B_{\rm P}$ are the ecliptic coordinates of the orbital pole in the equinox J2000, and M_0 is the mean anomaly of the secondary, measured from the ascending node (as pericenter is not defined for circular orbit) for epoch $t_0 =$ 2455873.0 (asterocentric UTC, i.e., light-time corrected). Since M_0 is strongly cor-346 related with $L_{\rm P}$, we report only its value for the nominal solution and do not report 347 its uncertainty (which is on the same order as the uncertainty of $L_{\rm P}$). Instead, to 348 describe the uncertainty of the position of the secondary in its orbit as an inde-349 pendent parameter, we report its relative ecliptic coordinates with respect to the 350 primary (see below).

e is the orbit eccentricity (only its upper limit is given, reported by Scheirich and Pravec 2009), and ΔM_d is the quadratic drift in the mean anomaly. Since the orbital period $P_{\rm orb}$ changes with time, the value presented in Table 2 is for the epoch t_0 . For this epoch, which is approximately the mean time of all observed events, a correlation between $P_{\rm orb}$ and ΔM_d is zero. We also give the time derivative of the mean motion \dot{n} , derived from ΔM_d , and the value of the orbital period at the nominal time of the DART impact $P_{\rm orb}^{\rm imp}$. All periods presented in Table 2, i.e., P_1 , $P_{\rm orb}$ and $P_{\rm orb}^{\rm imp}$, are sidereal.

The uncertainty area of the orbit pole is shown in Fig. 8.

Naidu et al. (2020) give the value of the mutual semimajor axis to be 1.19 ± 0.03 km (1 σ). To compare their result with our value, we computed $a/(A_1B_1)^{1/2}$ using their DEEVE for the primary and their semimajor axis of the mutual orbit. The result is given in Table 2.

365 λ_0 and β_0 are relative ecliptic coordinates of the secondary with respect to the 366 primary at the epoch t_0 . For the nominal time of the DART impact ($t_{\rm imp} = 2022$ -367 09-26.96875 geocentric UTC), these coordinates are given by $\lambda_{\rm imp}$ and $\beta_{\rm imp}$.

Note that the uncertainty of λ_{imp} is smaller than the uncertainty of λ_0 . This is 368 because of the following: The time evolution of the uncertainty of λ is governed 369 primarily by two factors: a) at the epochs covered with the data, it is restricted by their amount and quality; b) it grows quadratically into the future from the last observed apparition. Therefore, the uncertainty is small at the first and the last 372 apparition (panels a and c on Fig. 10), while at t_0 , which is not covered by the 373 data, the uncertianty is larger (panel **b** on Fig. 10). The last panel (**d**) of Fig. 10 374 shows the uncertainty at the nominal time of the DART impact. To demonstrate 375 the change of the uncertainty more illustratively, we constructed Fig. 11 showing 376 an evolution of the 3- σ uncertainty of λ in time.

Although assuming that the Dimorphos orbit is coplanar with the primary's equator throughout the modeling presented above, we also examined the possibility that this assumption is not held. We obtained that the inclination of the Dimorphos orbit to

the primary's equator is $\lesssim 3^{\circ}$ (see Appendix A).

3.1 The inward drift of the mutual orbit

The mean anomaly of a changing orbit expanded to the second degree in time is expressed by Equations (1) and (2). ΔM_d can be expressed using the semimajor axis of the mutual orbit and its time derivative as

$$\Delta M_d = \frac{1}{2}\dot{n} = -\frac{3n\dot{a}}{4a}.\tag{7}$$

The observed value of $\Delta M_d = 0.15 \pm 0.14 \text{ deg/yr}^2$ therefore imply an inward semimajor axis drift at the rate of $\dot{a} = -0.09 \pm 0.08 \text{ cm/yr}$ (3σ uncertainty).

Didymos system is the fourth binary for which we now have a long-term dynamical evolution inferred. The other three are (175706) 1996 FG3 that has a mean anomaly drift consistent with zero ($\Delta M_d = 0.04 \pm 0.20 \text{ deg/yr}^2$, Scheirich et al., 2015), (66391) Moshup that shows an outward drift of the mutual orbit ($\Delta M_d = -0.65 \pm 0.16 \text{ deg/yr}^2$, Scheirich et al., 2021), and (88710) 2001 SL9 that shows an inward drift of the mutual orbit (two solutions for ΔM_d : 2.8 ± 0.2 or 5.2 ± 0.2 deg/yr², Scheirich et al., 2021).

In the following, we discuss two possible mechanisms that can explain the slow inward drift of the Didymos system.

398 a) BYORP and tides

386

The binary YORP (BYORP) effect is a secular change of the mutual orbit of a binary asteroid system with a synchronous satellite due to the emission of thermal radiation from the asymmetric shape of that satellite. It was first hypothesized by Ćuk and Burns (2005). McMahon and Scheeres (2010a,b) built a detailed theory of the secular evolution of the mutual orbit due to the BYORP effect, which predicts that it causes the orbit to expand or contract on a timescale of thousands of years, as long as the satellite remains synchronous.

Adapting the method derived by McMahon and Scheeres (2010b), Pravec and Scheirich (2010) predicted the quadratic drift of (65803) Didymos caused by BY-ORP to be 2.51 deg/yr². Our detected value, 0.15±0.14 deg/yr² is much lower than this estimate. More recently, Jacobson and Scheeres (2011) presented an improved theory that incorporates both the BYORP effect and mutual tides between the two components. They showed that a stable long-term equilibrium may exist between these two torques if the BYORP effect is removing angular momentum from the orbit. Since the rotation period of Didymos is shorter than the orbital period of Dimorphos, the satellite raises a tidal bulge on the primary that removes energy from the rotation of the primary and transfers angular momentum to the mutual orbit.

² This value of ΔM_d is based on a shape model of a secondary of another NEA binary – (66391) Moshup – and it is only a magnitude, not directional estimate.

- These two torques are opposite in sign and can balance one another because they depend differently on the mutual orbit semi-major axis. They evolve the mutual orbit to an equilibrium semi-major axis, where the mutual orbit no longer evolves (Scheirich et al., 2015, reported the first binary system observed to be in or very close to this equilibrium state).
- The observed low positive value of the mean anomaly drift of Didymos may indicate that the system is evolving into and it is very close to, however not yet exactly at, such equilibrium.
- b) Differential Yarkovsky force in binary asteroid system
- Another effect causing a drift of the mutual semimajor axis is the Yarkovsky force, which affects not only the motion of the center of mass of the whole binary system but also the relative motion of components (Vokrouhlický et al., 2005). For NEA binaries, the semimajor axis drift is on the order from ~0.1 mm/yr to several mm/yr (Scheirich et al., 2021), i.e., on the same order as the drift observed in the Didymos system. Besides the BYORP, the differential Yarkovsky force is therefore another possible mechanism explaining the drift.

432 4 Mutual events prediction for the 2022–2023 apparition

- In order to facilitate planning ground-based observations before and after the DART impact, we computed times of mutual events that will occur in the 2022–2023 apparition using the nominal solution presented in Section 3. It is available at https://asu.cas.cz/~asteroid/Didymos_2022-2023_events.htm.
- The list also includes the events for a period after the DART impact. Since the prediction in this period is made using the assumption that none of the orbital parameters will change, it has an informative character only.

440 5 Conclusions

The near-Earth asteroid (65803) Didymos is among the best characterized small asteroid binary systems. It is a typical member of the population of near-Earth asteroid binaries for most of its parameters. With the photometric data taken during five apparitions over the time interval of 17 years, we constrained its binary orbit and determined the relative position of its secondary (Dimorphos) at the time of the DART impact to within $\pm 7.0^{\circ}$ (3σ uncertainty) with respect to the primary.

We found that the mean motion of Dimorphos is increasing with a rate of $\dot{n} =$ $5.26 \pm 4.91 \times 10^{-18} \text{ rad/s}^2$ (3 σ uncertainty), implying that the mutual semimajor 448 axis is shrinking in time. After the near-Earth binary asteroid (88710) 2001 SL9 449 (Scheirich et al., 2021), this is the second case with this observed property. As the 450 inward drift of its orbit can not be explained by mutual tides for the system with 451 the rotation period of the primary shorter than the orbital period of the secondary 452 (assuming the same sense of primary rotation and the mutual orbital motion), it suggests that either an interplay between the binary YORP (BYORP) effect and mutual tides, or the differential Yarkovsky force, or a combination of these effects, 455 acts in the Didymos system. 456

457 Appendix A. Assessment of the mutual orbit nodal precession

In Section 2.2, the spin axis of the primary was assumed to be normal to the mutual orbital plane of the components. Here we examine if this assumption is reasonable and how the primary spin axis orientation affects the results.

In the case of spherical primary, the orientation of its spin axis has no effect either 461 on the model lightcurve nor the results. In the case of an oblate primary, the main 462 issue is that the orbital pole precedes around the spin pole of the primary when the two poles are not same. The nodal precession rate depends on the oblateness of 464 the primary and other system parameters (see, e.g., Rossi et al., 1999). We tested 465 three values of the primary oblateness: 1.04, 1.16 and 1.40 (i.e. the nominal value 466 from Naidu et al. 2020 and its 1σ and 3σ upper limits, respectively). For these three 467 values, the nodal precession rates are -1.61, -5.50 and -10.57° /day, respectively 468 (we neglect the dependence of the nodal rate on the inclination of the satellite's orbit to the primary's equator because it is negligible for small angles).

We tested twelve orientations of the spin axis with respect to the orbital axis: four different orientations with an inclination between the axes of 1°, four with the inclination of 2°, and four with 4°. (The four orientations of the spin axis correspond to four different values of the length of ascending node of the satellite's orbit with respect to the primary's equator at the reference epoch.) For each combination of the orientation of the spin axis and the oblateness of the primary (the corresponding nodal rate was used for each oblateness), we then re-run the analysis.

From the best-fit solutions with inclinations of 1°, the largest absolute differences in parameters with respect to the nominal solution were: the difference in the mutual semimajor axis $\delta a/(A_1B_1)^{1/2} = 0.07$, the difference in the orbital period $\delta P_{\rm orb} =$

- 0.00000072 h, the difference in the mean anomaly drift rate $\delta \Delta M_d = 0.016$ deg/yr²,
- the differences in the relative ecliptic coordinates of the secondary with respect to
- the primary at the nominal time of the DART impact $\delta \lambda_{\rm imp} = 1.2^{\circ}$, $\delta \beta_{\rm imp} = 0.7^{\circ}$.
- From the best-fit solutions with inclinations of 2°, the largest absolute differences
- in parameters with respect to the nominal solution were: $\delta a/(A_1B_1)^{1/2}=0.11$,
- 486 $\delta P_{\text{orb}} = 0.00000096 \text{ h}, \ \delta \Delta M_d = 0.016 \text{ deg/yr}^2, \ \delta \lambda_{\text{imp}} = 1.0^{\circ}, \ \delta \beta_{\text{imp}} = 1.5^{\circ}.$
- The best-fit solutions with inclinations of 4° are all inconsistent with the observed
- data. We obtain that the inclination of the Dimorphos orbit to the primary's equator
- 489 is $\leq 3^{\circ}$.

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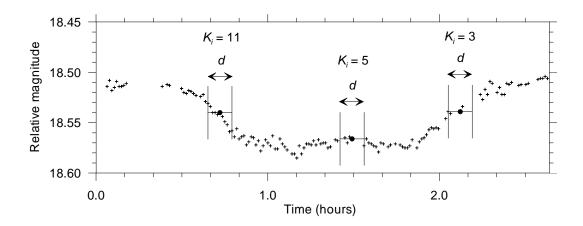


Fig. 1. An example of the determination of the weights applied to individual data points, as described in Section 2.2. The observed data are marked as crosses. For each data point, the number K_i of all data points that are within $\pm d/2$ from the given point is calculated (for the three examples shown, $K_i = 11$, 5 and 3). d is the correlation time, which we set equal to 0.14 h. A contribution of each data point to the χ^2 sum is then weighted by $1/K_i$.

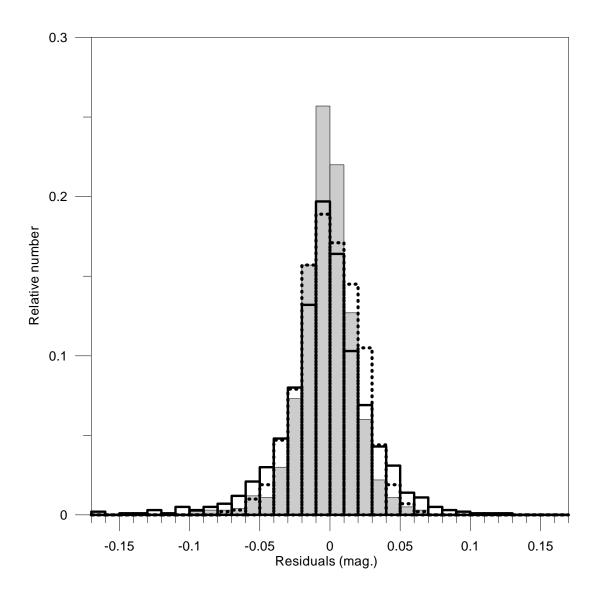


Fig. 2. Distribution of residuals of the model fitted to the observational data without the application of weights described in Section 2.2 (grey area) and with the weights applied (thick solid line). A histogram of a set of randomly generated values with normal distribution and standard deviation of 0.0216 mag. (thick dotted line) is shown for comparison.

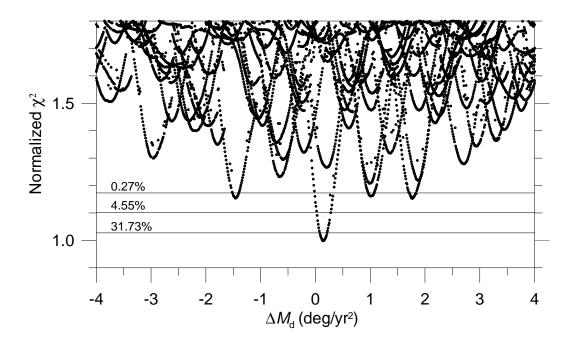


Fig. 3. The normalized χ^2 vs. ΔM_d for solutions of the model presented in Section 2.2. The three horizontal lines give the p-values – the probabilities that the χ^2 exceeds a particular value only by chance, corresponding to 1-, 2- and 3σ interval of the χ^2 distribution with 567 degrees of freedom. See text for details.

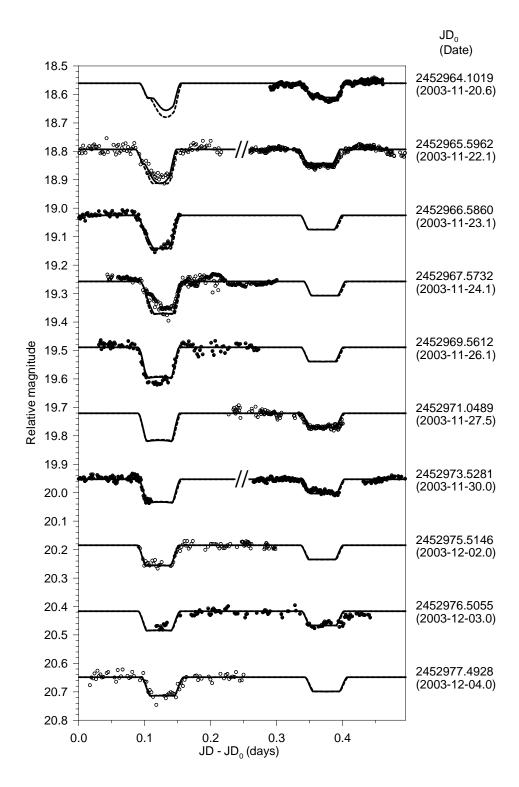


Fig. 4. The orbital lightcurve component of the Didymos system. The observed data are marked as points. (To avoid confusion between different data sets, solid and empty symbols are used alternating on each plot.) The solid curve represents the synthetic lightcurve for the best-fit solution. For comparison, the dashed curve is the model with ΔM_d fixed at 0.0 deg/yr² and all other parameters varied to obtain the best fit. The primary and secondary events (the terms refer to which of the two bodies is occulted or eclipsed) are always shown on the left and right side of the plots, respectively. In some cases, the observations of a secondary event precede that of a primary event (i.e., their order in the dataset is inverse of that shown on the plot). In order to save space in the plot, we present these events in reverse order to how they were observed. They are separated by "//" symbol in the plot and one orbital period (0.496 d) is to be subtracted from x coordinate of data points to the right from this separator.

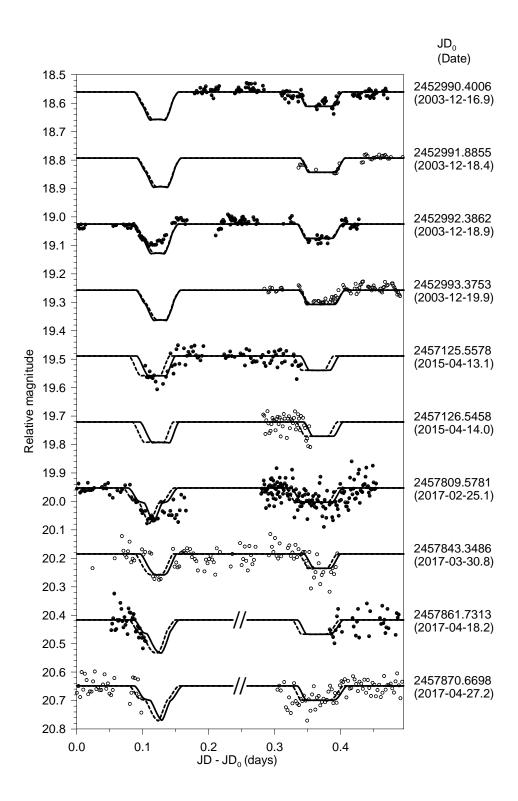


Fig. 5. Continuation of Fig. 4.

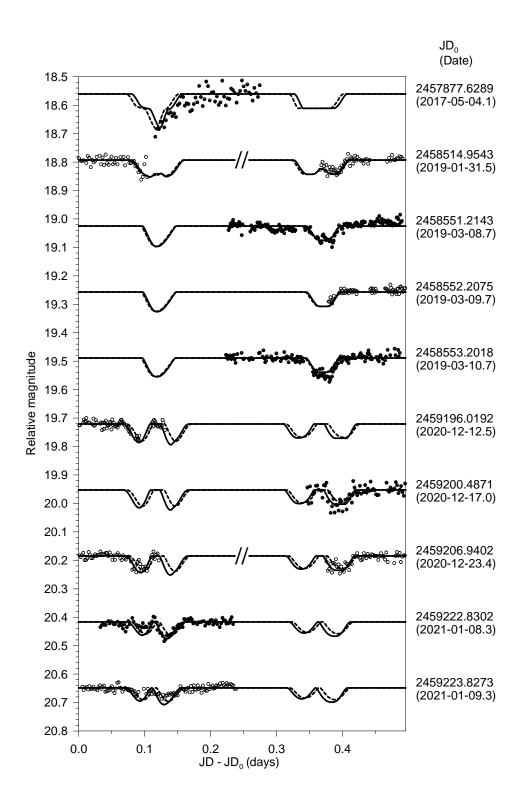


Fig. 6. Continuation of Fig. 4.

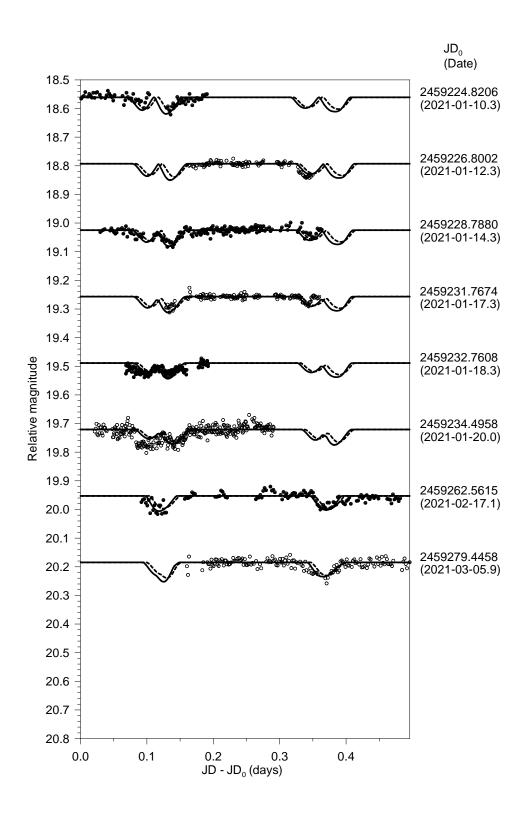


Fig. 7. Continuation of Fig. 4.

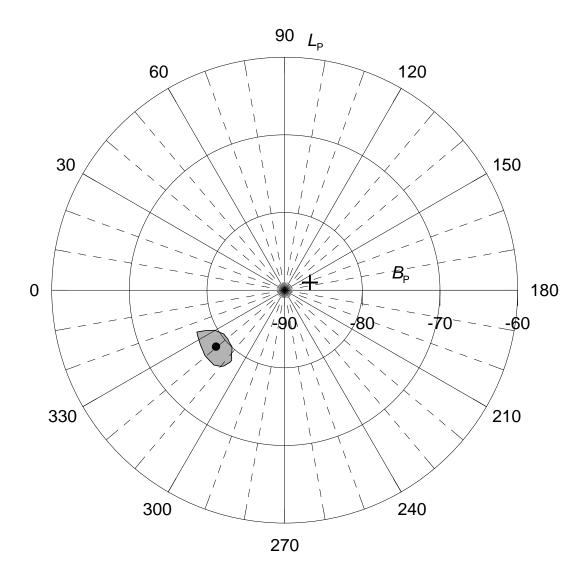


Fig. 8. Area of admissible poles for the mutual orbit of Didymos in ecliptic coordinates (grey area). The dot is the nominal solution given in Table 2. This area corresponds to 3σ confidence level. The south pole of the current asteroid's heliocentric orbit is marked with the cross.

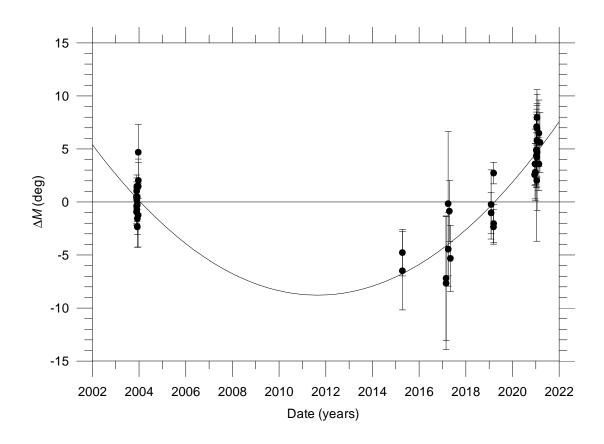


Fig. 9. Time evolution of the mean anomaly difference ΔM with respect to the solution with $\Delta M_d = 0$. See text for details. Each point corresponds to a mutual event covered by the observed data. Vertical error bars represent estimated 1σ uncertainties of the event times, expressed in the mean anomaly. A quadratic fit to the data points, represented by the solid curve, gives the quadratic term of $0.152 \, \mathrm{deg/yr^2}$.

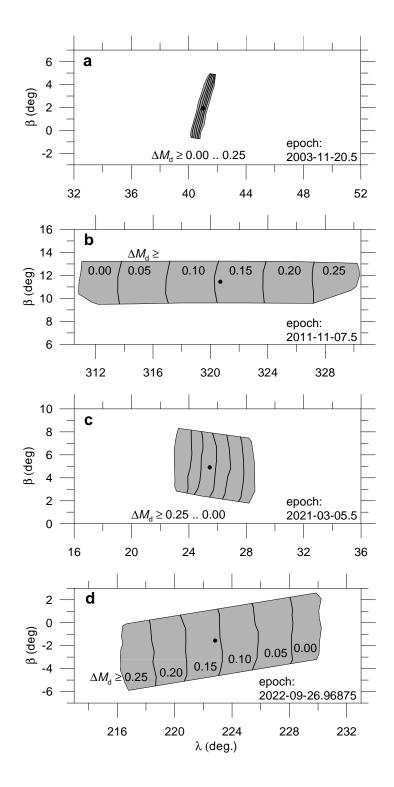


Fig. 10. 3- σ uncertainty area of Dimorphos relative position with respect to Didymos expressed in ecliptical coordinates λ , β (grey areas). To demonstrate the change in size of the uncertainty area with time, we plotted the area for four epochs (2003-11-20.5 – the beginning of the first apparition in 2003; 2011-11-07.5 – epoch JD0; 2021-03-05.5 – the end of the last apparition in 2021; 2022-09-26.96875 – the nominal epoch of the DART impact; panels a, b, c, d, respectively) with the same scale of the axes on all four panels. To show a correlation between λ and ΔM_d , the approximately vertical lines divide areas with $\Delta M_d \geq 0.00; 0.05; 0.10; 0.15; 0.20; 0.25 \text{ deg/yr}^2$, respectively (the inequality is used becease ΔM_d is correlated with other parameters as well and therefore strict boundaries for its values cannot be given). The dots denote the nominal solution given in Table 2.

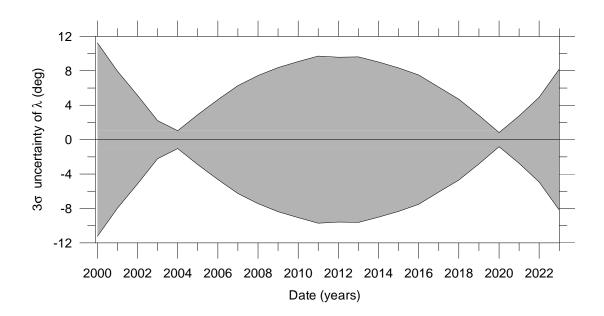


Fig. 11. Evolution of the 3- σ uncertainty of the ecliptic longitude (λ) of the radius vector of Dimorphos with respect to Didymos in time.